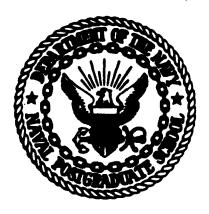
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# NAVAL POSTGRADUATE SCHOOL Monterey, California





## **THESIS**

CONICAL LENS FOR 5"/54 GUN LAUNCHED MISSILE

by

James M. Terrell

June 1981

Thesis Advisor:

Allen E. Fuhs

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Prepared for:
Defense Advanced Research Projects Agency
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Conical Lens for 5"/54 Gun Launched Missile

by

James M. Terrell Lieutenant, United States Navy B.S., University of Oklahoma, 1975

Submitted in partial fulfillment of the requirements for the degree of

MASTER OF SCIENCE IN PHYSICS

from the

NAVAL POSTGRADUATE SCHOOL

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#### **ABSTRACT**

Under the sponsorship of the Defense Advanced Research Projects Agency (DARPA), a conical lens for a 5"/54 ramjet propelled, optically guided projectile was investigated.

The resulting conical lens for the gun-launched missile (GLM) will focus parallel incident light through the lens to a design focal point. A conical lens was designed using an algorithm written for the HP-9845T desktop minicomputer. The examples illustrate the automated design procedure, selection of possible lenses and final lens design.

Recommendations for further research are discussed.

#### TABLE OF CONTENTS

I.	INTRO	DUCTION	19
	A. T	HE PROBLEM	19
	B. A	SSUMPTIONS AND SIGN CONVENTION	23
II.	FIRST	SURFACE	24
III.	SECONI	SURFACE GENERATION: DIRECT SOLUTION	32
IV.	RECOM	MENDATIONS FOR FUTURE WORK	59
v.	CONCL	JSIONS	60
APPENDI	IX A:	CHART SAMPLE OUTPUT AND PROGRAM LISTING	61
APPENDI	X B:	TRACE PROGRAM DESCRIPTION AND PROGRAM LISTING	163
APPENDI	X C:	POLYNOMIALS USED FOR THE SECOND SURFACE	212
APPEND1	X D:	THE USE OF A GENERAL BLOCK OF MATERIAL AS A LENS	243
APPENDI	X E:	GRADIENT INDEX OPTICS	253
APPENDI	X F:	SECOND SURFACE GENERATION: ITERATIVE SOLUTION	268
APPENDI	IX G:	LIMIT PROGRAM DESCRIPTION AND LISTING	286
LIST OF	REFEI	RENCES	293
INITIAL DISTRIBUTION LIST 29			294

#### LIST OF TABLES

A-I	SUBROUTINES DERIVED FROM THE HP-9845B UTILITIES LIBRARY	63
A-II	INITIAL PARAMETER VALUES	64
A-III	CALCULATED DATA USED TO CONSTRUCT THE DESIGN CHART IN FIGURE 16	65
A-IV	SECOND SURFACE COORDINATE (X, Y) VALUES, S, ALPHA2 and RHO2 FOR THE FAMILY OF SURFACES IN FIGURES 17 AND 18. THE COLUMN LABELED BEGIN RAY CORRESPONDS TO THE FAMILY MEMBER	83
A-V	COMPARISON OF THE MAXIMUM ALLOWED LENGTHS OF THE RAY IN THE LENS, QA, AND THE ACTUAL VALUE USED S <sub>MAX</sub> FOR EACH OF THE SURFACES IN	
	FIGURES 17 AND 18. ALPHA2 AND RHO2 ARE THE VALUES AT S <sub>MAX</sub> .	85
A-VI	CALCULATED VALUES OF S AND ALPHA2 USED TO CONSTRUCT THE DESIGN CHART IN FIGURE 19 FOR THE FINAL DESIGN OF SURFACE NUMBER 1 IN FIGURE 20.	86
A-VII	COORDINATE (X, Y) VALUES, S, ALPHA2 AND RHO2 FOR THE FINAL DESIGN OF SURFACE NUMBER 1 IN FIGURE 20	127
A-VIII	COORDINATE VALUES FOR THE RAY DIAGRAM IN FIGURE 22	128
B-I	SUBROUTINES DERIVED FROM THE HP-9845B UTILITIES LIBRARY	178
C-I	DATA POINTS FOR CURVE A	215
C-II	POLYNOMIAL COEFFICIENTS FOR CURVE A	216
C-III	DATA POINTS FOR CURVE B	222
C-IV	POLYNOMIAL COEFFICIENTS FOR CURVE B	223
C-V	DATA POINTS FOR CURVE C	230
C-VI	POLYNOMIAL COEFFICIENTS FOR CURVE C	231

E-I	BOUGUER'S GRIN CONSTANT	262
E-II	INITIAL PARAMETER VALUES	266
E-III	RAY DIAGRAM DATA CALCULATED FOR	267

#### LIST OF FIGURES

1	Spiked vs. Blunt Ramjet Inlets	25
2	Dimensions of 15° Tip Axisymmetric Isentropic Inlet Designed for Mach 3	26
3	Schematic Diagram of a Conical Shock (Oswatitsch Type) Supersonic Diffuser	28
4	Scheme of Using a REVERSED Converging- Diverging Isentropic Nozzle as a Supersonic Diffuser	29
5	Different Conical Shock Supersonic Diffuser Configurations Tested by Oswatitsch	30
6	Direct Solution: Low Region Geometry for n <sub>2</sub> > n <sub>3</sub>	33
7	Direct Solution: High Region Geometry for n <sub>2</sub> > n <sub>3</sub>	34
8	Sample Design Chart for a Conical Lens Design	37
9	Geometric Relationship for the Calculation of $\alpha_2$ vs. s	39
LO	Light Rays Refracted Through the Design Focal Point	40
11	Example of a Family of Second Surfaces Calculated from the Design Chart in Figure 8. The Surface Numbers 1, 2, 3 and 4 are Correlated Between the Curve Numbers in this Figure and Figure 8	41
L2	Example Design Chart for the Final Design of the Second Surface Using a Particular Surface Chosen in Figure 11	43
L3	Example of the Final Design of the Second Surface for the Surface Chosen in Figure 11	44
L4	Example Ray Diagram Showing the Results of the Lens Design Procedure	46
L5	Example of the Histogram of the Ray Distribution on the Image Plane in Figure 10. Compare with Figures C-3, C-7, C-13 and C-14 of Appendix C	48
	AT UPPERMEN A	40

16	Initial Design Chart Showing the Angle of the Tangent Line at the Second Surface, $\alpha_2$ , as a Function of Distance Along the Ray in the
	Lens, s 49
17	Family of Second Surfaces Calculated from the Design Chart in Figure 16 50
18	Family of Second Surfaces Generated from the Design Chart in Figure 16. The Rays are Included to Provide a Geometric Perspective 51
19	Final Design Chart Used to Calculate the Surface Number 1 in Figures 17 and 18 53
20	Final Design of the Second Surface of the Conical Lens Calculated from the Design Chart in Figure 19 54
21	Final Lens Design Illustrating the Symmetry and Position of the Lens in the GLM 55
22	Ray Diagram Showing the Trajectories of the Light Rays Through the Final Lens Design 57
23	Histogram Showing the Distribution of Rays on the Image Plane in Figure 22 58
B-1	Symbol Definition for the GLM164
B-2	Geometry and Symbol Definition for the Application of Snell's Law at the First Surface of the Conical Lens
B-3	Geometry and Symbol Definition for the Application of Snell's Law at the first Surface of the Conical Lens for $\theta_{\rm I} < 0$ 167
B-4	Geometry and Symbol Definition for the Application of Snell's Law at the Positive Branch of the Second Surface of the Conical Lens
B-5	Geometry and Symbol Definition for the Application of Snell's Law at the Positive Branch of the Second Surface of the Conical Lens and $\theta_{\rm I}$ < 0170
B-6	Geometry and Symbol Definition for the Application of Snell's Law at Negative Branch of the Second Surface of the Conical Lenguerrantial

B-7	Illustration of the Bisection Method Used in Subroutine BINARY SEARCH	172
B-8	Illustration of Dividing the Image Plane Into a Set of N-Increment Intervals Used to Generate a Histogram of a Ray Diagram	176
C-1	Conical Lens with the Second Surface Defined by Curve A	213
C-2	Ray Diagram for a Conical Lens Using Curve A as the Second Surface	218
C-3	Histogram of the Ray Distribution on the Image Plane Shown in Figure C-2	219
C-4	Conical Lens with the Second Surface Defined by Curve B	221
C-5	Ray Diagram for a Conical Lens Using Curve A as the Second Surface	224
C-6	Ray Diagram Using Curve B with Image Plane at 3.25 Inches	225
C-7	Histogram of the Ray Distribution on the Image Plane in Figure C-6	227
C-8	Conical Lens with the Second Surface Defined by Curve C	229
C-9	Ray Diagram for a Conical Lens Using Curve C as the Second Surface	232
C-10	Ray Diagram Using Curve C with the Image Plane at 3.46 Inches	234
C-11	Ray Diagram Using Curve C with the Image Plane at 3.25 Inches	235
C-12	Histogram of the Ray Distribution on the Image Plane in Figure C-10	236
C-13	Histogram of the Ray Distribution on the Image Plane in Figure C-11	237
C-14	The Angle of the Tangent Line of the Second Surface $\alpha_2$ as a Function of the Angle of the Tangent Line at the First Surface $\alpha$ for Total Reflection at the Second Surface	239

C-15	Ray Diagram for a Conical Lens Using Curve D as the Second Surface	240
C-16	Histogram of the Ray Distribution on the Image Plane in Figure C-15	241
D-1	Rhombus Lens	244
D-2	Shape, Geometry and Symbol Definition for a General Block Lens	246
D-3	Angular Relationships for the General Block Lens in Figure D-2	247
D-4	Parallelopiped Block Lens	251
D-5	Position of a Block Lens in the GLM	252
E-1	Illustrating Bouguer's Formula nd = constant, for Rays in a Medium with Spherical Symmetry	255
E-2	Illustration of Bouguer's Formula in the GLM Conical Lens	256
E-3	Illustration of the Relationship Between	
	# and p Between Adjacent Rays in the     GLM GRIN Lens	257
E-4	Illustration of a GLM Lens as a Section of GRIN Material Exhibiting Spherical Symmetry	258
E-5	Index of Refraction Profile as a Function of Radius from the Origin	259
E-6	Index of Refraction as a Function of Distance Along the First Surface of the GLM Lens	261
E-7	Bouguer's Constant as a Function of Radius from the Origin	263
E-8	Ray Diagram Showing the Change in Refracted Ray Angle at the First Surface of the GLM Lens Using GRIN Material for the Lens	264
F-1	Geometry and Symbol Definition Used for the Iterative Solution Method of Second Surface Generation	271

F-2	Geometry and Symbols Used for Snell's Law in the Low Region as Applied to the Iterative Solution Method for Second Surface Generation	273
F-3	Geometry and Symbols Used for Snell's Law in the Low Region as Applied to the Iterative Solution Method for Second Surface Generation	276
F-4	Geometry and Symbols Used for Snell's Law in the High Region as Applied to the Iterative Solution Method for Second Surface Generation	277
F-5	Illustration of the Result of the Solution of the Simultaneous Equations Used to Predict Point T2 on the Second Surface Using the Iterative Method	281
F-6	Three Undesirable Characteristics in Functions $f(\theta_I)$ which Cause Newton's Method to Diverge	283
F-7	A Desirable Function $f(\theta_{\underline{I}})$ to Use with Newton's Method	285
G-1	Geometry and Symbol Definition for the Relationship of the Slope of the Second Surface as a Function of the Slope of the First Surface	287
G-2	The Slope of the Second Surface as a Function of the Slope of the First Surface for Various Values of the Lens Index of Refraction and the Case of Total Relfection at the Second Surface	289

#### LIST OF SYMBOLS

Symbol	Explanation	Units
A	GLM (x-axis) intercept	Inches
F	Focal point on the GLM axis	Inches
NORM	Acute angle of the normal to the surface measured with respect to the GLM axis	Degrees, radians
0	Origin; located at the vertex of the GLM conical lens	Inches
OP	Length of the line segment connecting point 0 and point P	Inches
P	Focal point on the GLM axis intersection of the light ray and the radius vector in the GRIN lens	Inches
Q	Point of intersection of the light ray and the first surface	
QA	Length of the line segment connecting point Q and point R	Inches
QP	Length of the line segment connecting point Q and point P	Inches
r	Radial distance from the origin	Inches
Rho-initial	Angle the incident ray in medium 1 makes with the GLM axis	Degrees, radians
(REF)	Reference direction defined as the GLM axis	
RT	Length of the line segment connecting point R and point T	Inches

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Symbol	Explanation	Units
RO-max	Radius from the origin at which the index of refraction is maximum	Inches
T	Point of refraction of the ray in the lens	
Theta (critical)	Angle of incidence $\theta_{I}$ at which $\sin(\theta_{R})=1$	Degrees, radians
21	Point at which the lens intercepts the GLM axis	Inches
<b>Z</b> 3	Intercept of the first, movable, image plane and the GLM axis	Inches
24	Intercept of the second, fixed, image plane and the GLM axis	Inches
<sup>n</sup> ı	Index of refraction of medium 1	
<sup>n</sup> 2	Index of refraction of medium 2	
<sup>n</sup> <sub>3</sub>	Index of refraction of medium 3	
n=f(r)	Index of refraction is a function of the radius from the origin	
ĥ	Normal direction to a surface	
<sup>n</sup> 23	Ratio of n <sub>2</sub> /n <sub>3</sub>	
s	Distance along the ray in the lens	Inches
x	Distance along the GLM axis	Inches

Symbol	Explanation	Units
У	Radial distance from the GLM axis	Inches
y <sub>b</sub>	Upper bound of the aperture	Inches
Ya	Lower bound of the aperture	Inches
(x <sub>i</sub> ,y <sub>i</sub> )	Coordinate values of the intercept of the ray and a refracting surface or an image plane	Inches
(x <sub>c</sub> , y <sub>c</sub> )	Coordinate values of the intercept of the ray and the GLM axis	Inches
x=f(y)	Distance along the GLM axis is a function of the radial distance from the GLM axis	
y≖f(x)	Radial distance from the GLM axis is a function of the distance along the GLM axis	
<b>x</b>	Absolute value of x	Units of x
f	Focal length	Inches
1	Length of line segment QP	Inches
α	Cone half-angle	Degrees, radians
<b>a</b> <sub>2</sub>	$tan(\alpha_2)$ = slope of the second surface	Degrees, radians
β	Angle formed by QP with respect to the GLM axis	Degrees, radians
Υ	Complementary angle of $\theta_{R_4}$	Degrees, radians
δ	Angular difference between two surface normals	Degrees, radians

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Symbol	Explanation	Units	
θ*	Angle between two successive rays in GRIN	Degrees, radians	
θ <b>*</b>	General angle	Degrees, radians	
<sup>θ</sup> <b>ι*</b>	Angle of incidence with respect to the local normal	Degrees, radians	
θ <sub>R</sub> *	Angle of refraction with respect to the local normal	Degrees, radians	
π	Number of radians in semi-circle	Radians	
<sup>ρ</sup> Ι' <sup>ρ</sup> 0	Angle of incident rays in medium 1 with respect to the GLM axis	Degrees, radians	
ρ <sub>1</sub> *	Angle of the ray in the lens with respect to the GLM axis	Degrees, radians	
ρ <sub>2</sub>	Angle of the ray in medium 3 with respect to the GLM axis	Degrees. radians	
ф	Angle between the radius vector and the refracted ray in the GRIN lens	Degrees, radians	
1	Surface number		
	Step of a sequence		
(32.5,45.6)	(x,y) coordinate position	Inches	
Subscripts not already shown:			
1,2,3,	Point number		
	Iteration number		
i	Iteration number		
	Surface number		

Symbol	Explanation	Units
n	Iteration number	
max	Maximum value of the symbol	
next	Next quantity in the sequence	

<sup>\*:</sup> Indicates the symbol can be used with additional subscripts.

#### **ACKNOWLEDGEMENTS**

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#### I. INTRODUCTION

#### A. THE PROBLEM

Since World War II the presence of two conflicting requirements in missile sensor design has forced unsatisfactory compromises to be made in either the optical system, airframe or both. Examples of this are the Sidewinder air to air (AAM) and Chapparal surface to air (SAM) missile. The operational requirements are simple: from a "long" range, fly fast enough to pursue and overtake an adversary, destroy or disable the adversary and perform all of the guidance and tracking functions without assistance from the firing platform. The guidance decisions in the Sidewinder AAM are made by tracking the thermal radiation emitted from enemy aircraft. The radiation enters the missile optical system via a hemispherical dome on the nose of the missile.

Long range and high speed require sleek, low-drag airframes and efficient, high power engines. In the visible or
infrared, accurate measurement of the line of sight (LOS)
from the missile to the target requires optical lenses which
routinely come in the shape of spheres. Spheres and similar
blunt shapes have very high drag coefficients compared to
conical or ogive nose shapes. Thus the Sidewinder and
Chapparal missiles contain excellent optics, yet suffer in
range and operational capability.

The targets expected to be encountered in surface AAW are the Soviet anti-ship missiles (ASM). These weapons have evolved from simple straight line weapons to those with large warheads, multiple seekers and flight profiles which sometimes require operational tracking systems to perform beyond their design limits.

The fleet AAW battle doctrine of today is based on a "defense in depth" concept. According to this concept the E-2C/F-14/Phoenix combat system will be the first unit to engage enemy ASM, hopefully at maximum range. The next units able to engage the ASM at extended range, assuming the target is above the radar horizon, are the units employing the SM-2 (ER) and SM-1 (ER) missiles. While within the SM-2/1 (ER) engagement envelope, the SM-1 (MR) missile enters the engagement at medium range. Finally, once the ASM has penetrated this missile cover, the defense in depth concept reduces to a "defend each unit, especially the carrier" concept. In this region the 5"/54 gun system, Basic Point Defense System, NATO Sea Sparrow and Phalanx system are brought to bear.

The battle group could conceivably consist of an aircraft carrier, three Aegis cruisers, two SM-1 (ER) cruisers, two guided missile destroyers, two guided missile frigates, two fast frigates and three destroyers; or a total of fifteen units not including logistics ships. The capital assets for the ships, aircraft and equipment are in the tens of billions of dollars and perhaps 10,000 men. These assets demand

protection. However, with three exceptions the AAW combat systems presently in the fleet, or near operational status are not designed to engage a low-flying ASM in a timely manner. The exceptions are the Aegis cruiser, NATO Sea Sparrow system and Phalanx system; even with these three systems, there exists a gap in the 1-10 nautical mile range in the defense in depth concept.

A possible attack scenario is with the battle group steaming in an AAW formation when the Soviet commander launches a series of three saturation raids of ASM's against the battle group. The second and third raid are launched to arrive at the moment when the U.S. forces are totally engaged with the previous raid. Hence, the second and third raid will substantially penetrate the battle group, with perhaps the carrier and several of the major escorts at least mission disabled. The Soviet commander can now operate at will.

Two factors are critical to the battle group commander: munition assets and engagement time. Compared to the number of threats in a saturation attack, the battle group's missile assets are limited in number with limited reload capability. The battle group commander's gun ammunition assets are large, compared to the available missiles. However, with the current gun systems the engagement time per round is extremely long, on the order of 60 seconds. If the gun engagement time could be reduced by a factor of 2, then each gun barrel could be twice as effective.

Unguided, ballastic projectiles can be replaced by gun launched missiles (GLM). The GLM flying at Mach 3.0 can intercept in 15 seconds an inbound ASM flying at Mach 1.0 at a range of 20,000 yards. This engagement time and range are superior to any close-in system presently in the fleet. Therefore the GLM enhances the battle group's capability to survive a raid which saturates the group's long range combat systems. The GLM is not designed to replace any existing systems but complement them by providing the ability to strike out and defeat the enemy in the region from 1 to 10 nautical miles. In this range interval, defense capability presently exists; however, the magazine capacity is limited. The GLM will accomplish the ASMD task by marrying existing ramjet technology and a new generation of missile optics to provide a missile which is able to defeat the Soviet ASM at a range far greater than is realizable with today's gun systems.

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This thesis involved the writing of and the application of computer algorithms to accomplish the following:

- 1) Compute and trace monochromatic light rays through a conical lens.
- 2) Compute a refracting surface to focus monochromatic light rays to a point on the GLM axis.
- 3) Apply an optimization computer algorithm to the lens design problem.
- 4) Apply gradient index optics (GRIN) to the lens design.

#### B. ASSUMPTIONS AND SIGN CONVENTION

The computer algorithms are written based on Snell's law without approximations. All rays are assumed to be transmitted without loss of energy in the medium. When total internal reflection occurs, the ray is assumed to stop at the point of reflection. The algorithms are written to provide a basic understanding of the optics involved. Flexible computer programs have been written with the capability of adding ray tracing ability by adding subroutines.

The medium ahead of the GLM is assumed to be air.

Flying at Mach 3.0 the GLM will produce shock waves which will act like a refracting surface [1]. This thesis assumes the air to be homogenous, isotropic, linear, time independent (HILT) and free of shock waves in order to investigate the fundamental problem of designing a conical lens. The lens medium and the medium after the lens are assumed to be composed of an HILT material unless otherwise noted.

The sign convention used is a right-handed system with distances positive to the right and up as seen by the reader. All angles are positive for a counterclockwise rotation from the horizontal axis to the point in question. When used in derivation of geometrical relationships, the absolute values of angles are used in all trigonometric expressions.

All linear dimensions are inches unless otherwise noted.

#### II. FIRST SURFACE

A spiked nose used as a ramjet inlet optimizes the aerodynamic qualities yet degrades the optical qualities. Figure 1 [2] illustrates the inability in the past of a spiked nose to focus light rays while a sperical lens accomplishes an excellent focus. Thus, optimizing the aerodynamic qualities degrades the optical qualities and vice versa.

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Replacing the solid propellant rocket motor now used on most missiles with a ramjet engine further complicates the compromise between optical quality and aerodynamic efficiency. Replacing the rocket with an air-breathing ramjet is motivated by fuel economy and the ability to throttle the ramjet. The ability to throttle allows the missile to fly a thrust equal drag trajectory. This type of trajectory results in a vacuum-like trajectory with less sensitivity to wind and a marked increase in maximum range [3].

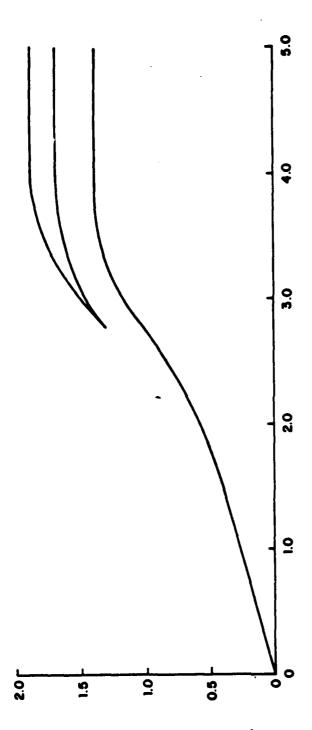
Ramjets operate with inlets configured for cruise performance at the design Mach number. The configuration of the inlet shown in figure 2 is based on a design Mach number of 3.0 [3]. The spike of the inlet is a combination of a cone and curved geometry to provide high pressure recovery during supersonic operation [3].

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Blunt nose having poor aerodynamic qualities and good optical qualities.

Figure 1. Spiked vs. Blunt Ramjet Inlets. (Reproduced from Ref. 2, p 19)



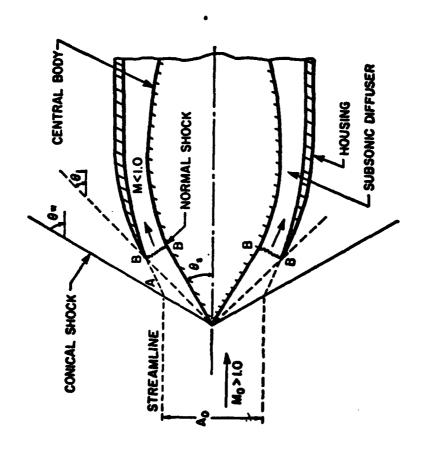
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Figure 2. Dimensions of 15° Tip Axisymmetric Isentropic Inlet Designed for Mach 3. (Reproduced from Ref. 3, p 37).

The inlet spike geometry is a complex surface which further complicates the task of the lens system which is to form an image of the target on the GLM axis. The inlet is a fluid mechanical device, called a diffuser, used to decelerate the air flow to a subsonic Mach number. The diffuser converts the kinetic energy of the flow into an increase in pressure of the air, known as pressure recovery, and decelerates the flow to a subsonic Mach number. Diffusers are required because the combustion of fuel is more efficient at high pressure and low velocity.

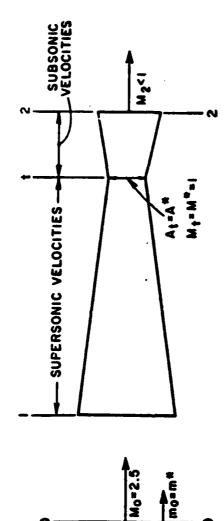
A desirable inlet is one which decelerates the flow at constant entropy, produces no shocks, creates zero drag exclusive of ram drag, and is insensitive to angle of attack. Inlets which operate off the design Mach number may have additive drag. Additive drag is the sum of the forces acting along the streamline A-B shown in figure 3 [4]. The pressure multiplied by the area of the streamtube A-B is a force which is in a direction opposite to that of flight and therefore is drag. Examples of other types of supersonic diffusers are shown in figures 4 and 5 [4].

The marriage of missile optics and a controllable engine promises a potent weapon. Preliminary feasibility studies have shown that ramjet engines, control systems, guidance laws and warhead designs can be integrated into a 5"/54 projectile [2,3,5,6]. The optical system has been identified as a major subsystem which requires additional investigation.



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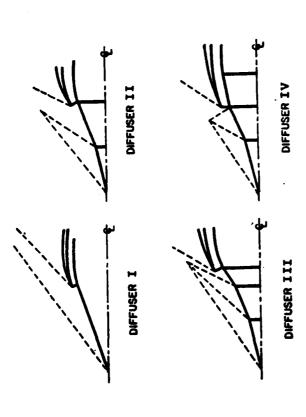
Figure 3. Schematic Diagram of a Conical Shock (Oswatitsch Type) Supersonic Diffuser. (Reproduced from Ref. 4, p. 245)



\* \*

Scheme of Using a REVERSED Converging-Diverging Isentropic Nozzle as a Supersonic Diffuser. (Reproduced from Ref. 4, p. 239) Figure 4.

\*E ...



DIFFUSER YI

Figure 5. Different Conical Shock Supersonic Diffuser Configurations Tested by Oswatitsch. (Reproduced from Ref. 4, p. 247)

Specifically, the lens, which is required to focus the image of the target, is the stumbling block to an efficient ramjet design. A blunt nose cannot be used because of poor pressure recovery and large additive drag. Therefore, some type of an inlet using a spike must be used. The spike must also be a lens capable of forming an image on the GLM axis. The lens must have a large enough aperture and field of view to provide the GLM with sufficient data to maintain and accurately measure the line of sight.

This thesis is based on an inlet design by Brown [3] using data from Faro [7] shown in figure 2. The inlet is a  $15^{\circ}$  conical tip, axisymmetric, isentropic spike for a design Mach number of 3.0. The spike studied in the thesis is a cone having approximately the same length-to-diameter ratio as the inlet in figure 2 [3]. Hence, the first optical surface used for ray tracing is a cone with a  $21^{\circ}$  half-angle.

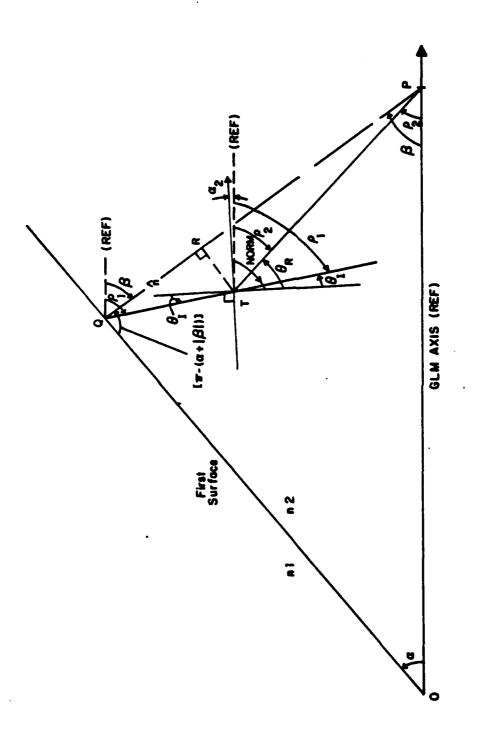
#### III. SECOND SURFACE GENERATION: DIRECT SOLUTION

The direct solution to designing a conical lens consists of solving Snell's Law at a point T shown in figures 6 and 7 along the refracted ray within the lens. Point T is located below the line QP in figure 6. When T is in this position relative to QP, the geometry is referred to as the low region. When T is in the position shown in figure 7, the geometry is referred to as the high region. When T is on the line QP, i.e.  $\rho_1 = \beta$ , the low region geometry is assumed.

The following discussion is the derivation of expressions for  $\rho_2$ , the angle with respect to the GLM axis of the ray refracted at T which passes through the design focal point P, and  $\alpha_2$ , the angle which the tangent line at T makes with respect to the GLM axis. The derivation will only discuss the low region, because the procedure for the high region is identical and only the results for the high region will be given. The magnitude of a line segment is shown by stating the endpoints of the line segment in uppercase letters or by a single lower case letter.

Let QP= $\ell$ , QT=s and OP=f; then according to the law of sines  $\sin\alpha/\ell = (\sin(\pi-[\alpha+|\beta|]))/f$ . This relation simplifies to

$$\ell = \frac{f \sin \alpha}{\sin (\alpha + |\beta|)} \tag{1}$$



Direct Solution: Low Region Geometry for n2 > n3. Figure 6.

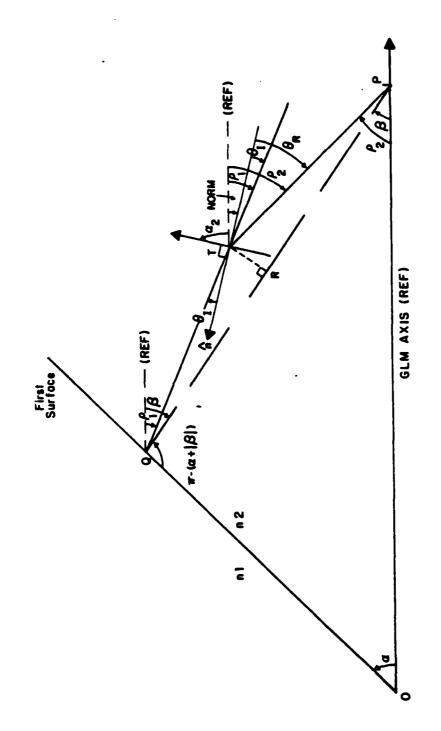


Figure 7. Direct Solution: High Region Geometry for  $n_2 > n_3$ .

Next, note that

$$RT = s \sin(|\rho_1| - |\beta|)$$
 (2)

and

$$RT = (PQ-QR) \tan(|\beta|-|\rho_2|)$$
 (3)

Now PQ-QR= $\ell$ -s cos( $|\rho_1|$ - $|\beta_1|$ ). Substituting this into equation (3) and solving for tan( $|\beta|$ - $|\rho_2|$ ) yields

$$\tan(|\beta|-|\rho_2|) = \begin{cases} \frac{s \sin(|\rho_1|-|\beta|)}{\frac{f \sin\alpha}{\sin(\alpha+|\beta|)}} - s \cos(|\rho_1|-|\beta|) \end{cases}$$
(4)

Consequently the formula for  $|\rho_2|$  becomes  $|\beta|$  - arctan $\{\}$ . Using equation (4),  $\rho_1$ , the angle with respect to the GLM axis of the ray refracted at Q, apply Snell's Law at T. Thus, referring to figure 6

$$\sin\theta_{R} = \frac{n_{2}}{n_{3}} \sin\theta_{I} = n_{23}\sin\theta_{I}$$
 (5)

where  $\theta_R = |NORM| - |\rho_2|$  and  $\theta_I = |NORM| - |\rho_1|$ . Substituting these expressions into equation (5) yields a relation involving the sine of two angles. Expanding the sine expressions and solving for tan |NORM| yields

$$tan|NORM| = \begin{cases} \frac{\sin|\rho_2| - n_{23}\sin|\rho_1|}{\cos|\rho_2| - n_{23}\cos|\rho_1|} \end{cases}$$
 (6)

and |NORM| = arctan{ }. Equation (6) must be greater than or equal to zero for the expression to be valid. Then

$$\alpha_2 = \frac{\pi}{2} - |NORM| \tag{7}$$

The result of the derivation for the high region yields

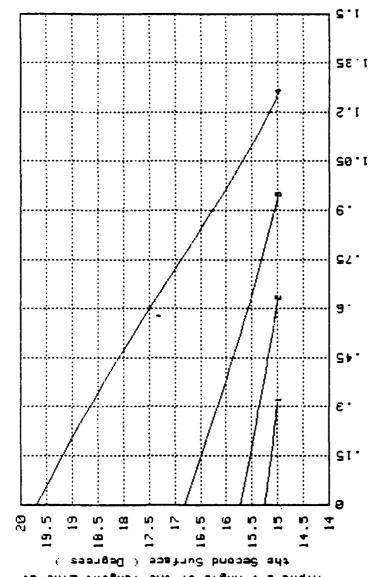
$$\tan(|\rho_2|-|\beta|) = \begin{cases} \frac{\sin(|\beta|-|\rho_1|)}{\int \frac{\sin(\alpha+|\beta|)}{\sin(\alpha+|\beta|)} - \sin(|\beta|-|\rho_1|)} \end{cases}$$
(8)

$$tan |NORM| = \frac{n_{23} \sin |\rho_1| - \sin |\rho_2|}{n_{23} \cos |\rho_1| - \cos |\rho_2|}$$
(9)

and solving for  $\alpha_2$  gives

$$\alpha_2 = \frac{\pi}{2} - |NORM| \tag{10}$$

Therefore,  $\alpha_2$  is a complicated relationship involving incident ray position, denoted by  $\beta$ , cone half angle  $\alpha$ , design focal point P, the refractive indices  $n_1$ ,  $n_2$ , and  $n_3$  and position s along the ray within the lens. In order for a systematic study to be conducted, the parameters  $\alpha$ , f,  $n_1$ ,  $n_2$  and  $n_3$  are assigned specific values. The parameter  $\beta$  is determined by the position of point Q on the first surface. The angle of  $\rho_1$ , is determined by the incident ray angle with respect to the first surface,  $n_1$ , and  $n_2$ . Therefore, with the values for the parameters, either fixed or calculated, a design chart relating  $\alpha_2$  with the position along the ray in the lens s shown in figure 8 can be generated. The numbered curves correspond to numbered rays entering the lens. The rays are numbered consecutively beginning with the one nearest the GLM axis.



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S : Distance Along Refracted Ray in the Lens (Inches)

Design Facal Point : 6.88 inches Number of Rays : 4

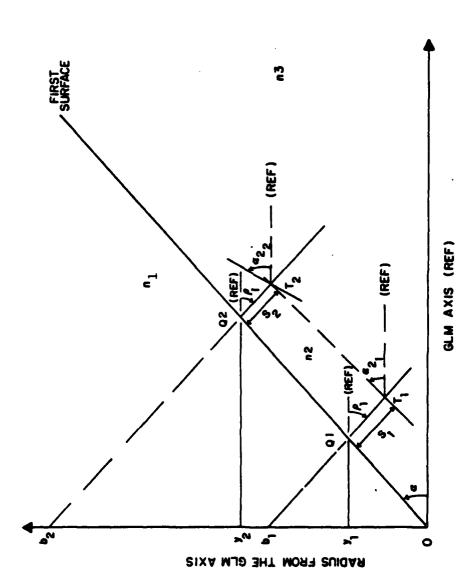
Figure 8. Sample Design Chart for a Conical Lens Design.

The actual design process involves selecting a starting point, Tl, on a given ray and noting the magnitude of s1 as shown in figure 9. With that value of  $s_1$ , enter the design chart in figure 8 and read the value of  $\alpha_2$  from curve number 1. Returning to figure 9 extend a line from Tl using  $\alpha_2$  until that line intercepts the next ray at T2. Measure the value of  $s_2$  and enter figure 8 to obtain the value of  $\alpha_2$  from curve number 2. Return to figure 9 and extend a line from T2 to intercept the next ray, etc. This process continues until all of the rays are intercepted or the first surface is intercepted. Once the intercept point T and the angle of the tangent line  $\alpha_2$  is known, the ray can be refracted at T. Equations (4) and (7) for the low region and equations (8) and (10) for the high region accomplish the refraction. The result of each refraction by design result in a refracted ray through the focal point P as shown in figure 10.

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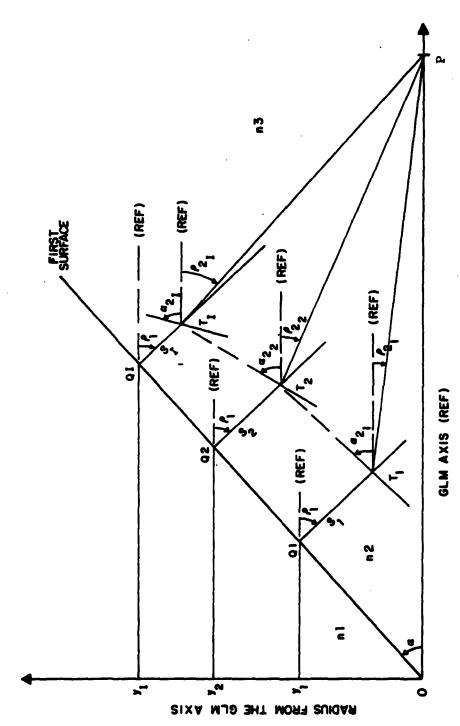
The design procedure does not produce a single surface which can be used to refract light through the focal point. The surface designed depends on which ray was chosen as the initial ray and the value of s along that ray where Tl is positioned. Thus, a small family of surfaces illustrated in figure 11 can easily be calculated to provide a choice of lens second surfaces to the optical engineer.

The lens designer must choose from the family of second surfaces generated by the design procedure. In order for a



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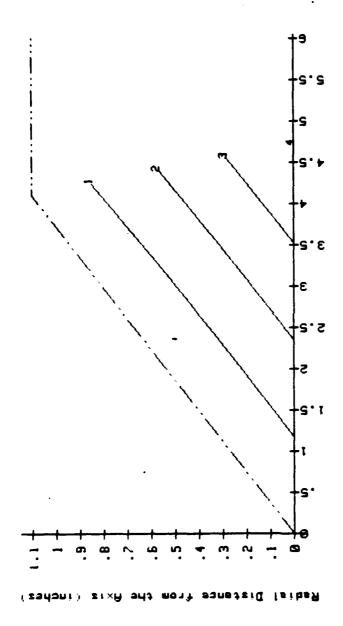
Geometric Relationship for the Calculation of Figure 9.



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Figure 10. Light Rays Refracted Through the Design Focal Point.



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Design Facal Paint: 6.80 inches Number of Reys: 4
Riphe: 15.88 deg

Distance Alang GLM Axis (inches)

FAMILY OF SURFACES

Example of a Family of Second Surfaces Calculated from the Design Chart in Figure 8. The Surfaces Numbers 1, 2, 3 and 4 are Correlated Between the Curve Numbers in this Figure and Figure 8. Figure 11.

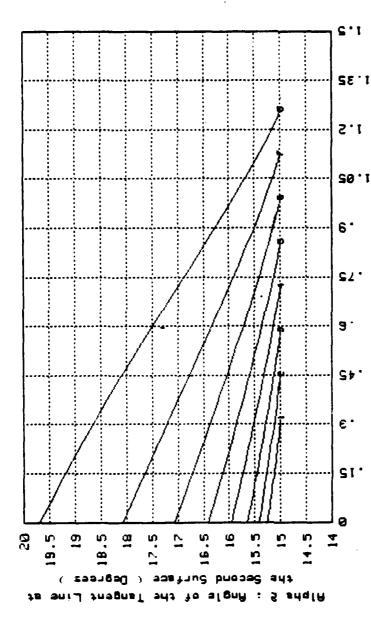
consistent set of decisions to be made a set of design criteria for this thesis are:

- 1) that the lens must be as thin as possible.
- 2) that the lens have as large an aperture as possible.

  The aperture is defined to be the difference in radius between the maximum and minimum radii from the GLM axis at which light rays enter the lens and are refracted through the focal point.
- 3) that the focal length to diameter ratio, f/d, is a minimum and in no case greater than 4.

Using the stated design criteria, surface number 1 in figure 11 is the logical choice because it is the thinnest and has the maximum aperture of the 5 surfaces provided. All of the surfaces have the same f/d ratio of 2.73.

Each member of the family of surfaces is generated by using straight lines. Since a real surface will not be a series of flat surfaces but a smooth continuous surface with no discontinuities, an inherent error exists in the design. The error can be reduced substantially by using a large number of rays to provide a large number of line segments to approximate a continuous surface. The designer must now choose the number of rays to be used, repeat the design process and generate the design chart for the final lens design using, for example, 26 rays in figure 12. Using figure 12, the designer calculates the final lens design in figure 13 beginning with the starting point which is the



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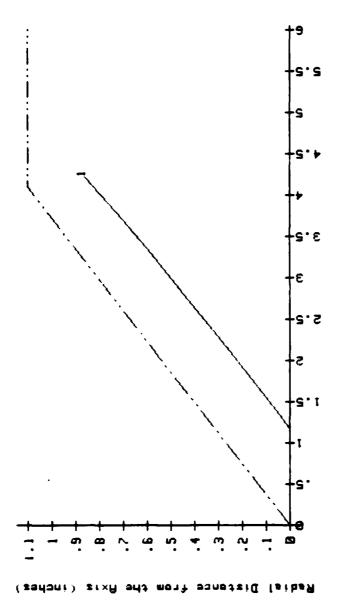
C

Example Design Chart for the Final Design of the Second Surface Using a Particular Surface Chosen in Figure 11. Figure 12.

S : Distance Along Refracted Ray in the Lens ( Inches

Besign facel Point : 6.88 inches

Alpha : 15.88 deg



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Bixtance Along GLM Axix (inchex)

SURFACE NUMBER 1

Design Facel Paint i 6.80 inches Riphe i 15.80 deg Apertura i 825 inch

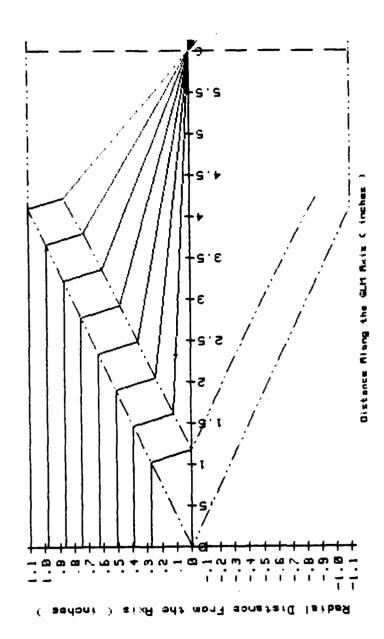
Example of the Final Design of the Second Surface for the Surface Chosen in Figure 11. Figure 13.

end of a curve number 1 in figure 12. Thus T1 is near the GLM axis and  $\alpha_2 = 21^{\circ}$ .

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A ray diagram shown in figure 14 illustrates the paths of the light rays through the lens generated using the design chart in figure 12. A histogram showing the distribution of light rays on the image plane reveals that the light rays do pass through one design focal point plus or minus an half-increment width. The width of an increment is defined as the maximum radius of the GLM divided by the desired number of intervals. For example, if the maximum radius of the GLM is 1.1 inch and 100 intervals from the GLM axis to a radius of 1.1 inch then the increment width is 0.011 inch. In order to position an interval on the origin, an increment is centered on the origin. The effect of this operation is to add a half-increment at the maximum value of the radius. Therefore, for the entire GLM a total of  $2 \times 100 + 1 = 201$  increments are used to generate a histogram. The fact that all of the rays intersect the focal point shows the calculations are correct for this particular lens.

An automated computer algorithm, CHART, has been written to construct a design chart and calculate a family of surfaces from that design chart. CHART waits until the operator chooses a particular surface from the presentation and the number of rays desired to calculate a final surface. Next, CHART will compute the final surface and present it to the



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SURFACE NUMBER 1

Ingident Ray Angle: 8.08 deg Number of Reys: 8
Resture: 825 inch Riphs: 15.86 deg Enage Plane: 6.88 inch

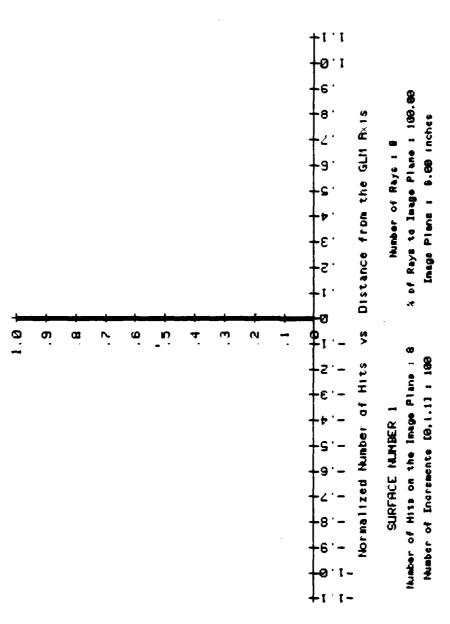
Figure 14. Example Ray Diagram Showing the Results of the Lens Design Procedure.

operator. The operator can choose to stop or draw a ray diagram to show the effectiveness of the design. If the ray diagram is chosen a histogram of ray distribution on the image plane is presented to the operator. If the operator wants to design a lens using another surface, the entire procedure must be repeated.

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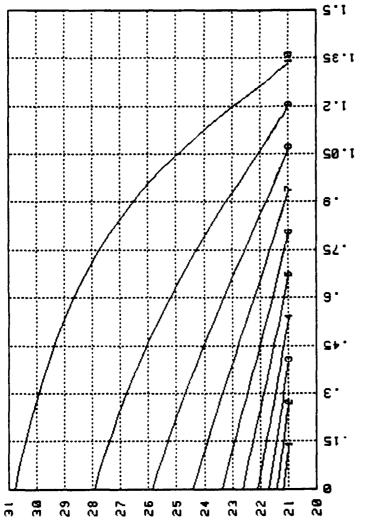
1

The following figures are a sample run of CHART to design Tables containing the initial parameter values and calculated data are located in Appendix A. The design chart in figure 16 was generated using the initial parameter information in Table A-II. The family of second surfaces in figures 18 and 19 were calculated using the end of each numbered curve in figure 16 as the starting point Tl for each numbered second surface in figures 17 and 18. information used to draw figures 17 and 18 is in Table A-III. The rays shown in figure 18 were used to generate the design chart and family of second surfaces figures 17 and 18. maximum length of a ray in the lens is defined as QA, the distance from the intercept of the incident ray and the first surface to the GLM axis. The calculated information used to draw the family of second surfaces in figures 17 and 18 is found in Table A-IV. A comparison of QA and the value of s used as the starting point Tl for each family, s<sub>max</sub>, is found in Table A-V.



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Compare with Figures C-3, C-7, Example of the Histogram of the Ray Distribution on the Image Plane in Figure 10. Cc C-13 and C-14 of Appendix C. Figure 15.



( Degrees

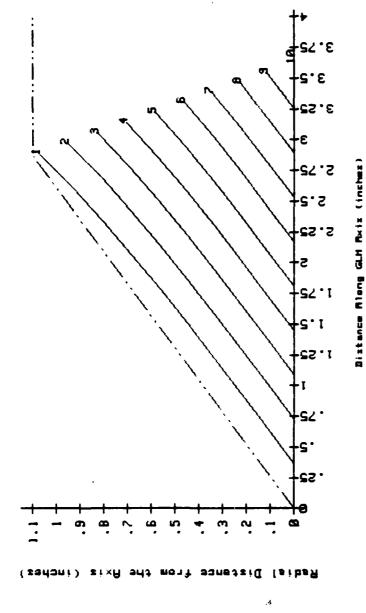
(

Distance Along Refracted Ray in the Lens (Inches)

Dezign Facel Point i 4.8d inches Number of Rays i 18 Ripha : 21.88 deg

Initial Design Chart Showing the Angle of the Tangent Line at the Second Surface,  $\alpha_2$ , as a Function of Distance Along the Ray in the Lens, s. Figure 16.

Slope of Second Surface



(

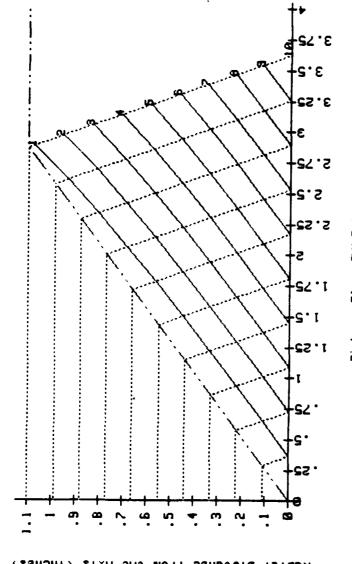
Design Focal Point: 4.80 inches

Riphs: 21.80 deg

n2: 4.80800

Rigure 17. Family of Second Surfaces Generated from the Design Chart in Figure 16.

FANILY OF SURFACES



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Bixtance Along GLM Axis (inches)

FANILY OF SURFACES

Design Facal Paint : 4.88 inches Number of Rays : 18 Riphs : 21.88 deg n2 : 4.88888 Family of Second Surfaces Generated from the Design Chart in Figure 16. The Rays are Included to Provide a Geometric Perspective. Figure 18.

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Surface number 1 was chosen because the surface satisfied all of the design criteria. The final design chart shown in figure 19 was generated using 26 rays. The number of rays actually entered into the computer was 25, CHART then calculates the aperture of the lens using the chosen surface. If the lower limit of the aperture is not the GLM axis, CHART adds one ray to the number entered to use as the starting ray. This method insure a ray will be drawn at the maximum and minimum boundaries of the aperture. The calculated data used to generate the design chart in figure 19 is listed in Table A-VI.

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The final lens design shown in figure 20 consists of a surface defined by 26 points rather than 10 with the initial design. The coordinate values for the final surface are found in Table A-VII. The refinement of the surface obtained by using 26 rays is illustrated by comparing the end points of the surfaces listed in Tables A-VII and A-IV. The changes in x, y are (-0.009, 0.013) inch. The change in s is (-0.016) inch. Hence, the lens designer should be aware of the tendency of the final surface to move towards the first surface, possibly resulting in the design surface intercepting the first surface prior to the GLM wall at the maximum radius from the axis. This effect results in a decrease in aperture, a violation of the design criteria.

The final design surface is then drawn within an outline of the GLM shown in figure 21 illustrating the symmetry of

Angle of the Tangent Line

C

Distance Along Refracted Ray in the Lens (Inches)

Design Facal Point i 4.88 inches

Alpha : 21.88 deg

Alpha : 21.88 deg

Righte 19. Final Design Chart Used to Calculate the Surface Number I in Figures 17 and 18.

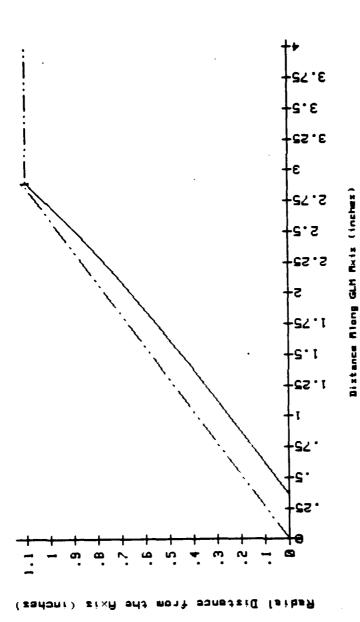
5.1

38.1

1.2

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Number of Rays 1 26 n2 : 4. Babaa Aperture 1 . 898 inch Design Facel Point : 4.80 inches Alpha : 21.89 deg Figure 20.

SURFRICE NUMBER 1

Final Design of the Second Surface of the Conical Lens Calculated from the Design Chart in Figure 19.

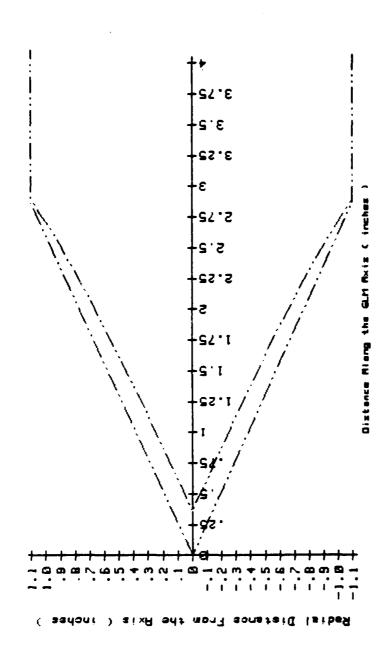


Figure 21. Final Lens Design Illustrating the Symmetry and Position of the Lens in the GLM.

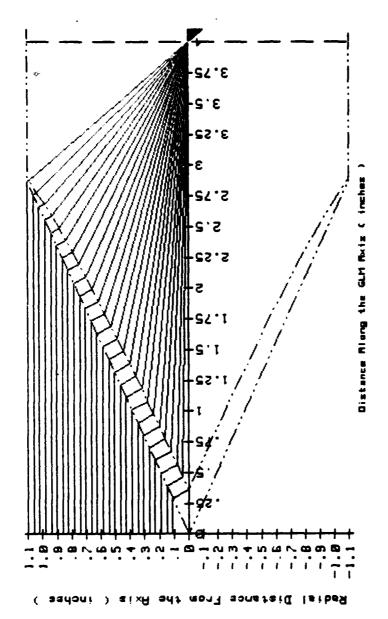
SURFRICE NUMBER 1

Aparture : .996 inch Riphe : 21.86 deg

Incident Ray Rngle :

the design and the location of the lens within the missile. A ray diagram using the final lens design shown in figure 22 with the distribution of the rays on the image plane shown in figure 23. The coordinate values used to draw the ray diagram in figure 22 are listed in Table A-VIII.

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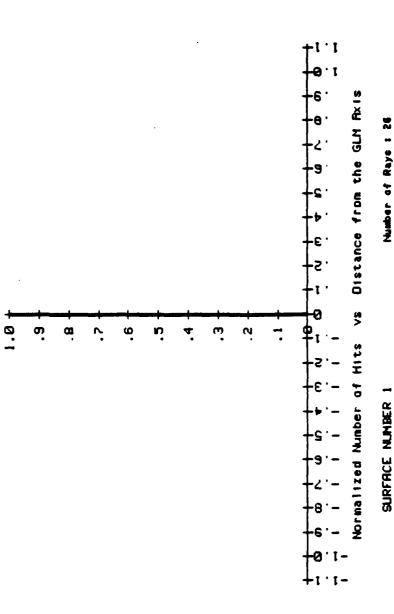


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SURFACE NUMBER 1

Encident Ray Rogle : 8.08 deg Number of Rays : 26 Rperture : .998 inch Ripha : 21.98 deg Ench Figure 22. Ray Diagram Showing the Trajectories of the Light Rays Through the Final Lens Design.



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Figure 23. Histogram Showing the Distribution of Rays on the Image Plane in Figure 22.

% of Rays to Image Plane : 188.88

Number of Hits on the Jasge Plane : 26 Number of Indrements [8,1.1] : 188

Image Plans : 4.88 inches

## IV. RECOMMENDATIONS FOR FUTURE WORK

This thesis investigated part of the properties of a conical lens. Future studies should investigate:

a) the effect of skew rays on the image.

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- b) the effect of total internal reflection on the image.
- c) the calculation of monochromatic and chromatic aberrations for the conical lens.
- d) the availability and applicability of materials to use for a lens.
- e) the effect on the incident rays of the shock wave in the air ahead of the GLM.
- f) the effect on the image of an object not on the lens axis.
- g) the effect on the image when the object is no longer in the far field and the curvature of the ray front must be taken into account.
- h) the ability of a conical lens to focus coherent and incoherent light.

# V. CONCLUSIONS

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The completed design of figure 22 indicates that a conical lens can focus incident light which is parallel to the GLM axis. The conical lens design is compatible with the aerodynamic requirements of high pressure recovery and low drag. The ability to provide optical guidance information to the GLM powered by an integral rocket ramjet may provide the battle group commander with an inexpensive ASMD weapon for shipboard use.

#### APPENDIX A

## CHART SAMPLE OUTPUT AND PROGRAM LISTING

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This appendix contains the program listing for CHART.

The subroutines listed in Table A-I were copied or derived from the HP-9845 utilities library, cassette number 2,

Ser. No. 09845-10205, program REGPLT.

Subroutines DRIVER, POLYNOMIAL and PLOT-CUBIC are not implemented in the present version of CHART because of time constraints. They are designed to be used to fit a polynomial of degree 3, a cubic, between four points to estimate the shape of the second surface. The requirement to fit a curve stems from the fact that the trajectory of a ray cannot be calculated if the ray does not coincide with a known ray trajectory. Hence, two options are open. The first is to calculate an infinite number of points on the second surface which is not practical. The second option is to estimate the actual shape of the second surface with an analytic expression, a cubic in this application. The error of the estimate can be reduced by designing a second surface with a large number of points. CHART has been written to design a lens with a maximum number of 250 points.

CHART, as implemented on the HP-9845T is a slow program. The design procedure described in chapter III requires approximately fifteen minutes for an experienced operator.

Therefore, if the initial and final design charts used more or less rays then the computation time should be scaled accordingly.

TABLE A-I

SUBROUTINES	DERIVED	FROM	THE	HP-9845B	UTILITIES	LIBRARY

Name	Line Number
Plot	3710
Laxes	5280
Driver	13910
Polynomial	14400
Plot-Cubic	14910
Min	21040
Max	21160

## TABLE A-II

#### INITIAL PARAMETER VALUES

Alpha = 21.00 degrees TAN(Alpha) = .38

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RHG1 = -55.50 degrees

GLN Radius = 1.10 inches Aperture = 1.10 Ya

Ya = 0.00 inch n2 = 4.00000 n1 - 1.00000

Number of Rays = 18

Design Focal Point = 4.00 inches

Rho-initial = 0.00 TAN(RHO-INITIAL) = 0.00

Theta(critical) = 14.48 degrees

Yb = 1.18 inches

n3 1.00000

TABLE A-III
CALCULATED DATA USED TO CONSTRUCT THE DESIGN CHART IN FIGURE 16.

RAY	BETA	THETA(RAY)	NORMAL	\$ 	ALPHA2	RHO 2
				•		
1	-1.697	13.317	-68.820	0.000	21.180	-1.697
i	-1.697	13.326	-68.829	.007	21.171	-1.614
i	-1.697	13.335	-68.838	.013	21.162	-1.530
i	-1.697	13.344	-68.847	. 020	21.153	-1.447
i	-1.697	13.354	-68.856	. 027	21.144	-1.363 -1.279
1	-1.697	13.363	-68.866	.033	21.134	-1.195
1	-1.697	13.372	-68.875	. 848	21.125 21.116	-1.111
1	-1.697	13.381	-68.884	. 047	21.116	-1.027
1	-1.697	13.398	-68.893	. 053	21.107	942
1	-1.697	13.399	-68.902	. 060	21.089	957
1	-1.697	13.408	-68.911	. 067	21.089	772
1	-1.697	13.417	-68.920	.073 .080	21.071	687
ı	-1.697	13.426	-68.929 -68.938	. 887	21.062	602
1	-1.697	13.435	-68,947	. 993	21.053	517
ı	-1.697	13.444	-68.956	. 100	21.044	431
1	-1.697	13.453	-68,963	.107	21.035	345
1	-1.697	13.462	-68.974	.113	21.026	259
L	-1.697	13.471 13.479	-68.982	. 120	21.018	173
1	-1.697	13.479	-68.991	.127	21.009	087
1	-1.697	13.479	-68.982	.120	21,018	173
1	-1.697 -1.697	13.480	-68.983	. 121	21,017	164
1	-1.697	13.481	-68.984	. 121	21.016	156
1 1	-1.697	13.482	-68,985	. 122	21.015	147
1	-1.697	13.483	-68.986	.123	21.014	138
1	-1.697	13.484	-68,987	.123	21.013	130
i	-1.697	13.485	-68,988	.124	21.012	121
i	-1.697	13.486	-68,989	. 125	21.011	112
ì	-1.697	13.486	-68.989	, 125	21.011	104
i	-1.697	13.487	-68.998	.126	21.010	095
i	-1.697	13.488	-60.991	.127	21.009	087
i	-1.697	13.489	-68.992	. 127	21.008	078
ī	-1.697	13.490	-68.993	.128	21.007	069
1	-1.697	13.491	-68.994	. 129	21.006	961
1	-1.697	13.492	-68.995	. 129	21.005	052
1	-1.697	13.493	-68.996	. 130	21.004	843
1	-1.697	13.494	-68.996	. 131	21.604	03
1	-1.697	13.494	-68.997	.131	£1.003	020 01
ı	-1.697	13.495	-68.998	. 132	21.002	00
1	-1.697	13.496	-68.999	.133	21.001	01
ı	-1.697	13.495	-68.998	. 132	21.662	01
1	-1.697	13.495	-68.998	, 132	21.002	01
1	-1.697	13.495	-68.998	. 132	21.002 21.001	01
1	-1.697	13.496	-68.999	. 132	21.001	01
1	-1.697	13.496	-68.999	. 132	21.001	01
1	-1.697	13.496	-68.999	. 132	<1.00t	•

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TABLE A-III (CONT)

PAY	BETA	THETA(RAY)	NORMAL	\$ 	ALPHA2	RHO 2
1	-1.697	13.496	-68.999	. 133	21.001	012
ı	-1.697	13.496	-68.999	.133	21.901	01:
1	-1.697	13.496	-68.999	. 133	21.001	016
1	-1.697	13.496	-68.999	. 133	21.001	016
t	-1.697	13,496	-68.999	. 133	21.001	009
1	-1.697	13,496	-68.999	. 133	21.001	008
1	-1.697	13.496	-68.999	. 133	21.001	007
1	-1.697	13,496	-68.999	. 133	21.001	006
1	-1.697	13,497	-68.999	. 133	21.001	~.005
1	-1.697	13,497	-69.000	. 133	21.000	~.004
1	-1.697	13,497	-69.000	. 133	21.000	~.803
1	-1.697	13.497	-69.000	. 133	21.000	~.003
1	-1.697	13,497	-69.000	. 133	21.000	~.002
1	-1.697	13,497	-69.000	. 133	21.000	001
1	-1.697	13.497	-69.888	. 133	21.000	00
1	-1.697	13,497	-69.000	. 133	21.000	~. 962
1	-1.697	13.497	-69.900	.133	21.000	002
1	-1.697	13.497	-69.000	. 133	21.000	001
1	-1.697	13.497	-69.000	. 133	21.000	001
1	-1.697	13.497	-69.000	.133	21.000	001
1	-1.697	13.497	-69.900	.133	21.000	001
1	-1.697	13.497	-69.000	.133	21.090 21.000	001 001
1	-1.697 -1.697	13.497 13.497	-69.00 <b>0</b> -69.000	.133	21.000	001
i	~1.697	13.497	-69.888	.133	21.000	001
i	-1.697	13,497	-69.980	.133	21.000	001
1	-1.697	13.497	~69.00 <b>0</b>	. 133	21.000	001
i	-1.697	13.497	-69.000	.133	21.000	001
i	-1.697	13.497	~69.000	.133	21.000	001
i	-1.697	13.497	-69.888	.133	21.000	006
i	-1.697	13.497	-69.000	. 133	21.000	006
i	-1.697	13.497	-69.000	.133	21.888	000
i	-1.697	13.497	-69.000	. 133	21,000	000
1	-1.697	13.497	-69.000	. 133	21.000	000
2	-3.673	13.087	-68.589	9.990	21.411	-3.673
2	-3.673	13.198	-68.611	.013	21.389	-3.498
2	-3.673	13, 129	-68.632	. 027	21.368	-3.321
2	-3.673	13.150	-68.653	. 040	21.347	-3.144
2	-3.673	13.171	-68.674	. 653	21.326	-2.966
2	-3.673	13.192	-68.493	. 067	21.305	-2.787
2	-3.673	13.213	-68.716	. 880	21.284	-2.696
2	-3.673	13.234	-68.737	. 093	21.263	-2.427
2	-3.673 -3.673	13.255 13.276	-68.758 -68.779	. 107	21.242	-2.245
				. 128	21.221	-2.063
2	-3.673	13.296	-68.799	.133	21.201	-1.

TABLE A-III (CONT)

AY	BETA	THETA(RAY)	HORMAL	\$ 	ALPHA2	RHQ 2
2	-3,673	13.317	-68.828	. 147	21.180	-1.696
2	-3.673	13.337	-68,840	. 168	21.160	-1.511
2	-3,673	13.358	-68.861	.174	21.139	-1.325
2	-3.673	13.378	-68.881	.187	21.119	-1.139
2	-3.673	13.398	-68.991	. 200	21.099	951
2	-3.673	13.418	-68.921	.214	21.079	763
2	-3.673	13.438	-68.941	. 227	21.059	573
2	-3.673	13.458	-68.961	. 240	21.039	383 192
2	-3.673 -3.673	13.477 13.458	~68.988 ~68.961	. 254 . 248	21. <b>929</b> 21. <b>039</b>	383
2	-3.673	13.460	-68.963	.242	21.037	364
ž	-3.673	13.462	-68.965	.243	21.035	345
2	-3. <b>6</b> 73	13.464	-68.967	.244	21.033	326
2	-3.673	13.466	-68.969	.246	21.031	307
Ž	-3.673	13.468	-68,971	.247	21.029	288
2.	-3.673	13.470	-68.973	.248	21.027	268
2	-3.673	13.472	-68.975	. 258	21.625	249
2	-3.673	13.474	-68.976	. 251	21.024	-,238
2	-3.673	13,475	-68.978	. 252	21.022	-,211
2	-3.673	13.477	-68.989	. 254	21.020	192
2	-3.673	13.479	-68.982	. 255	21.018	173
2	-3.673	13.481	-68.984	. 256	21.016	154
2	-3.673	13.483	-68.986	. 258	21.014	134
2	-3.673	13.485	-68.988	. 259	21.012	115
2	-3.673	13.487	-68.998	. 268	21.010	096
2	-3.673	13.489	-68.992	. 262	21.008	077
2	-3.673	13.491	-68.994	. 263	21.006	058
2	-3.673	13.493	-68.996	. 264	21.004	038
2	-3.673	13.495	-68.998	. 266	21.002	019
3	-3.673	13.493	-68.996	. 264	21.884	~.036
5	-3.673	13.493	-68.996	. 264	21.004	037
Š	-3.673	13.494	-68.996	.265	21.004	035
S	-3.673	13.494	-68.997	. 265	21.003	~.033
5	-3.673	13.494	-68.997	. 265	21.803	~. 031
5	-3.673 -3.673	13.494	-68.997 -60.007	. 265	21.003	~. 929
2	-3.673	13.494 13.494	-68.997 -68.997	. 265 . 265	21. <b>46</b> 3 21. <b>66</b> 3	~. 927 ~. 925
2	-3.673	13.495	-68.998	. 265	21.003	~.023
2	-3.673	13.495	-68.998	.265	21.002	021
ž	-3.673	13.495	-68.998	. 266	21.002	021
ž	-3.673	13.495	-68.998	.266	21.002	017
ž	-3.673	13.495	-68.998	.266	21.002	015
ž	-3.673	13.496	-68.779	. 266	21.001	013
2	-3.673	13.496	-68,999	. 266	21.901	912
Ž	-3.673	13.496	-68.999	. 266	21.961	010
2	-3.673	13.496	-68.999	. 266	21.901	008

TABLE A-III (CONT)

C

RAY	BETA	THETA(RAY)	HORMAL	\$ ·	ALPHA2	RHO 2
2	-3,673	13.496	-68,999	. 267	21.991	006
2	-3.673	13.497	-69.000	.267	21.000	004
2	-3.673	13.497	-69.988	.267	21.000	002
2	-3.673	13.497	-69.988	. 267	21.000	804
2	-3.673	13.497	-69.888	.267	21.000	884
2	-3.673	13,497	-69.000	. 267	21.000	803
2	-3,673	13.497	-69.800	. 267	21.000	003
2	-3,673	13.497	-69.000	. 267	21.000	~.003
2	-3,673	13.497	-69.908	.267	21.000	~.003
Ž	-3,673	13.497	-69.800	. 267	21.000	003
2	-3,673	13.497	-69.808	, 267	21.000	003
2	-3.673	13.497	-69.808	. 267	21.000	002
2	-3.673	13.497	-69.888	. 267	21.600	002
2	-3.673	13.497	-69.000	. 267	21.000	-, 982
2	-3.673	13.497	-69.000	. 267	21.000	002
2	-3.673	13.497	-69.800	. 267	21.000	002
2	-3.673	13.497	-69. <b>889</b>	. 267	21.000	001
2	-3.673	13.497	-69. <b>909</b>	. 267	21.000	001
2	-3.673	13.497	-69. <b>999</b>	. 267	21.000	001
2	-3.673	13.497	-69. <b>988</b>	. 267	21.000	001
2	-3.673	13.497	-69.8 <b>66</b>	.267	21.000	001
2	-3.673	13.497	-69.000	. 267	21.899	000
2	-3.673	13.497	-69.000	. 267	21.600	000
2	-3.673	13.497	-69.800	. 267	21.000	000
2	-3.673	13.497	-69.900	. 267	21.888	000
2	-3.673	13.497	-69.888	. 267	21.000	000
2	-3.673	13.497	-69.888	. 267	21.000	000
2	-3.673	13.497	-69.000	. 267	21.000	000
2	-3.673	13.497	-69.808	. 267	21.000	000
2	-3.673 -3.673	13.497 13.497	-69.0 <b>00</b> -69.000	. 267 . 267	21.000 21.000	-,000
2	-3.673	13.497	-69.000	. 267	21.000	000 000
2	-3.673	13.497	~69.000	.267	21.000	806
2	-3.673	13.497	-69.000	. 267	21.868	~.000
2	-3.673	13.497	-69.000	. 267	21.000	000
2	-3.673	13.497	-69.000	.267	21.000	000
2	-3.673	13.497	-69.000	.267	21.000	000
2	-3.673	13.497	-69.000	.267	21.898	000
Ž	-3.673	13.497	-69.000	.267	21.606	000
2	-3.673	13.497	-69.000	.267	21.000	000
2	-3.673	13.497	-69.000	.267	21.800	000
2	-3.673	13.497	-69.900	.267	21.000	000
2	-3.673	13.497	-69.000	.267	21.000	900
3	-5.999	12.787	-68.290	0.000	21.710	-5.999
3	~5.999	12.825	-68.327	. 428	21.673	-5.722

TABLE A-III (CONT)

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RAY	BETA	THETA(RAY)	HORMAL	s	ALPHA2	RHQ 2
3	-5.999	12.862	-68.365	. 049	21.635	-5.442
3	-5.999	12.899	-68.482	. 060	21.598	-5.168
3	-5.999	12.936	-68.439	. 280	21.561	-4.876
3	-5.999	12.972	-68.475	. 100	21.525	-4.589
3	-5.999	13.009	-68.512	. 120	21.488	-4.300
3	-5.999	13.045	-68.548	. 140	21.452	-4.909
3	-5.999	13.061	-68.584	. 160	21.416	-3.715
3	-5.999	13.117	-68.629 -68.656	. 180 . 200	21.3 <b>88</b> 21.344	-3.419
3	-5.999	13.153	•			-3.120
3	-5.999 -5.999	13.1 <b>89</b> 13.224	-68.692 -68.727	. 220 . 240	21.3 <b>08</b> 21.273	-2.819 -2.516
3	-5.999	13.259	-68.762	. 260	21.273	-2.210
3	-5.999	13.294	-68.797	. 288	21.203	-1.902
3	-5.999	13.329	-68.831	.300	21.169	-1.591
3	-5.999	13.363	-68.866	.320	21.134	-1.278
3	-5,999	13.397	-68,900	. 340	21.100	962
3	-5,999	13.431	-68, 933	. 360	21.067	644
3	-5.999	13.464	-68.967	. 380	21.833	323
3	-5.999	13.497	-69.000	. 488	21.989	898
3	-5.999	13.464	-68.967	. 386	21.633	323
3	-5.999	13.467	-68.978	. 382	21.939	291
3	-5.999	13.471	-68.974	. 384	21.026	-, 259
3	-5,999	13.474	-68.977	. 386	21.023	227
3	-5.999	13.477	-68.988	. 386	21. <b>020</b>	194
3	-5.999	13.481	-68, 983	. 390	21.017	162
3	-5.999	13.484	-68.987	. 392	21.013	130
3	-5.999	13.487	-68.990	. 394	21.010	897
3	-5.999	13.490	-68.993	. 396	21.007	065
3	-5.999	13.494	-68.997	. 390	21.003	032
3 3	-5.999	13.497	-69.000	. 400	21.000	000
3	-5.999	13.494	-68.997	. 390	21.003	032
3	-5.999 -5.999	13.494 13.494	-68.997 -68.997	. 399 . 399	21.003 21.003	029 026
3	-5, 999	13.495	-68.998	.399	21.003	023
3	-5.999	13.495	-68.998	.399	21.002	023
3	-5.999	13.495	-61.998	.399	21.002	016
3	-5, 999	13.496	-68,999	. 400	21.001	013
3	-5.999	13.496	-68.999	. 400	21.601	010
3	-5.999	13.496	-68.999	. 400	21.001	006
3	-5.999	13.497	-67.000	. 400	21.000	003
3	-5.999	13.497	-69.000	. 400	21.000	000
3	-5.999	13.497	-69.000	. 400	21.000	003
3	-5.999	13.497	-69.000	. 400	21.000	863
3	-5.999	13.497	-69.000	. 400	21.000	003
3	-5.999	13.497	-69.000	. 400	21.000	002
3	-5.999	13.497	-67.000	. 400	21.000	002

TABLE A-III (CONT)

AY	BETA	THETR(RAY)	HORNAL	<u> </u>	ALPHA2	RHO 2
3	-5.999	13.497	-69.000	. 400	21.000	802
3	-5,999	13.497	-69.000	. 488	21.000	001
3	-5.999	13.497	-69.000	. 480	21.000	001
3	-5.999	13.497	-69.900	. 498	21.000	001
3	-5,999 -5,999	13.497 13.497	-69.0 <del>00</del> -69.000	. 40 <del>0</del> . 40 <b>0</b>	21.000 21.000	000 000
3	-5, 999	13.497	-69.000	. 400	21.000	888 888
3	-5,999	13.497	-69.000	. 400	21.000	000
3	-5,999	13.497	-69.000	. 400	21.000	000
š	-5,999	13.497	-69.000	. 480	21.000	~. 900
3	-5, 999	13.497	-69.800	. 400	21.000	~.800
3	-5.999	13.497	-69.000	. 400	21.000	~.000
3	-5.999	13.497	-69.000	. 468	21.000	000
3	-5.999	13.497	-69.000	. 488	21.999	~.000
3	-5.999 -5.999	13.497	-69.000	. 488	21.000	000
3	-5.999	13.497 13.497	-69.000 -69.000	. 488 . 488	21.900 21.000	000 000
3	-3.777	131471	-47.000	. 700	21.004	000
4	-8.765	12.391	-67.894	8.200	22.106	-8.765
4	-9.765	12.449	-67.952	. 027	22.048	-8.377
4	-8.765	12.507	-68.010	.053	21.998	-7.984
4	-8.765	12.565	-68.068	.888	21.932	-7.586
4	-6.765	12.623	-68.126	. 197	21.874	-7.182
4	-8.765	12.681	-68.184	. 133	21.816	-6.774
4	-8.765	12.738	-68.241	. 160	21.759	-6.361
•	-9.765 -8.765	12.795 12.852	-68.298 -68.355	.187 .214	21.7 <b>92</b> 21.645	-5.942 -5.518
4	-8.765	12.908	-68.411	. 249	21.589	-5.869
4	-9.765	12.964	-68.467	. 267	21.533	-4.654
4	-8.765	13.020	-68.523	. 294	21.477	-4.214
4	-8.765	13.075	-68.578	.320	21.422	-3.760
4	-8.765	13.138	-68.633	.347	21.367	-3.317
4	-9.765	13.184	-68.687	.374	21.313	-2.860
4	-8.765	13.238	-68.741	. 400	21.259	-2.398
4	-0.765	13.291	-68,794	. 427	21.206	-1.930
-	-9.765 -9.765	13.343	-68,846	. 454	21.154	-1.456
•	-8.765	13.395 13.447	-68, 898 -68, 949	. 488 . 507	21.102 21.051	976 491
4	-8.765	13.447	-68, 949	- 507	21.051	491
-	-8.765	13.452	-68, 935	.510	21.045	442
4	-0.765	13.457	-68,968	.513	21.040	393
4	-8.765	13.462	-68,965	.515	21.035	-, 344
4	-0.765	13.467	-68,970	.518	21.930	295
4	-8.765	13.472	-68.975	. 521	21.025	246
4	-8.765	13.477	-60.980	. 523	21.020	197
4	-0.765	13.482	-68.985	. 526	21.015	148

TABLE A-III (CONT)

AY	BETA	THETA(RAY)	HORMAL	<u> </u>	ALPHA2	RHO 2
4	-8.765	13.487	-68.999	. 529	21.010	899
4	-8.765	13.492	-68.995	. 531	21.005	049
4	-8.765	13.492	-68.995	. 531	21.005	049
4	-8.765	13.493	-68.995	. 531	21.005	844
4	-8.765	13.493	-68.996 -68.996	.532 .532	21. <b>004</b> 21. <b>004</b>	040 035
4	-8.765 -8.765	13.494 13.494	-68.997	.532 .532	21.003	039
-	-8.765	13.495	-68.997	.533	21.003	025
4	-8.765	13.495	-68.998	.533	21.982	020
4	-8.765	13.496	-68.998	. 533	21.002	015
4	-8.765	13.496	-68.999	.533	21.001	010
4	-8.765	13.497	-68.999	. 534	21.001	005
4	-8.765	13.497	-68.999	.534	21.981	005
4	-8.765	13.497	-69.000	.534	21.000	004
4	-8.765	13.497	-69.000	. 534	21.000	004
4	-8.765	13.497	-69.000	. 534	21.000	003
4	-8.765	13.497	-69.0 <b>00</b>	. 534	21.000	003
4	-8.765 -8.765	13.497	-69.000 -69.000	. 534 . 534	21.000 21.000	~.002 ~.082
4	-8.765	13.497 13.497	-69.000	. 534	21.000	001
4	-8.765	13.497	-69.000	.534	21.000	001
4	~8.765	13.497	-69.000	.534	21.000	099
4	-8.765	13.497	-69.000	. 534	21.000	000
4	-8.765	13.497	-69,000	.534	21.000	000
4	-8.765	13.497	-69.000	. 534	21.000	000
4	-8.765	13.497	-6%. <b>809</b>	. 534	21.000	-, 999
4	-8.765	13.497	-69.600	.534	21.000	000
4	-8.765	13.497	-69.800	. 534	21.000	998
4	-8.765	13.497	-69. <b>000</b> -69. <b>00</b> 0	. 534 . 534	21. <b>000</b> 21. <b>000</b>	886 8 <b>8</b> 6
4	-9.765 -8.765	13.497 13.497	-69.000	.534	21.000	000
4	-0.765	13.497	-69.800	.534	21.000	000
5	-12.092	11.956	-67.359	0.000	22.641	-12.092
5	-12.092	11.941	-67.444	. 033	22.556	-11.587
5	-12.092	12.027	-67.530	. 867	22.478	-11.073
5 5	-12. <b>09</b> 2 -12. <b>09</b> 2	12.112 12.197	-67.615 -67.7 <b>90</b>	. 1 <b>00</b> . 133	22.365 22.36 <b>0</b>	-10.549 -10.615
5	-12.092	12.283	-67.786	. 167	22.214	-9.471
5	-12.092	12.368	-67.871	. 200	22.129	-8.917
5	-12.092	12.453	-67.956	. 234	22.044	-8.353
5	-12.692	12.537	-68.840	.267	21.960	-7.778
5	-12.092	12.622	-68.125	. 300	21.875	-7.192
5	-12.092	12.705	-69.200	. 334	21.792	-6.596
5	-12.692	12.789	-68.292	. 367	21.700	-5.989
5	-12.092	12.871	-68.374	. 400	21.626	-5.370

TABLE A-III (CONT)

RAY	BETA .	THETR(RAY)	HORMAL	\$	ALPHA2	RHO 2
5	-12.092	12.953	-68.456	. 434	21.544	-4.748
5	-12.092	13.034	-69.537	. 467	21.463	-4.099
5	-12.092	13.114	-68.617	. 501	21.383	-3,446
5	-12.092	13.193	-68.696	. 534	21.384	-2.781
5	-12.892	13.271	-68.774	. 567	21.226	-2.104
5	-12.092	13.348	-68.851	. 661	21.149	-1,415
5	-12.092	13.423	-68.926	. 634	21.074	714
5	-12.092	13.348	-69.951	. 601	21.149	-1.415
5	-12.092	13.355	-68.858	. 684	21.142	-1.345
5	~12. <b>892</b> ~12. <b>89</b> 2	13.3 <b>63</b> 13.371	-68.866 -68.874	.607 .611	21.134 21.126	-1.275 -1.206
5	-12.092	13.378	-68.881	.614	21.126	-1.136
5	-12.092	13.366	-68.889	.617	21.111	-1.066
5	-12.092	13.393	-68.896	.621	21.104	-,995
5	-12.892	13.461	-68.904	.624	21.096	925
5	-12.092	13.408	-68.911	.627	21.089	855
5	-12.092	13.416	-68.919	.631	21.881	784
5	-12.092	13.423	-68.926	. 634	21.874	714
5	-12.092	13.431	-68.934	.637	21.066	643
5	-12.092	13.438	-68.941	.641	21.059	572
5	-12.892	13.446	-68.948	. 644	21.052	501
5	-12.692	13.453	-68.956	.647	21.044	438
5	-12.092	13.460	-68.963	. 651	21.037	358
5	-12.092	13.468	-68.971	. 654	21.029	287
5	-12.092	13.475	-68.978	. 657	21.022	215
5 5	-12. <b>09</b> 2 -12. <b>09</b> 2	13.482	-68.9 <b>8</b> 5	.661	21.915	-,144
5	-12.092	13.498 13.482	-68.993 -68.985	. 664 . 661	21. <b>00</b> 7 21. <b>0</b> 15	072
5	-12.892	13.483	-68.986	.661	21.015	144 137
Š	-12.092	13.484	-68.987	.661	21.013	129
3	-12.092	13.465	-68.988	.662	21.012	122
5	-12.092	13.485	-68.988	. 662	21.012	115
5	-12.092	13.486	-68.989	. 662	21.011	100
5	-12.092	13.487	-68.790	. 663	21.010	-, 101
5	-12.092	13,488	-68.990	. 663	21.010	093
5	-12.092	13.488	-68.991	. 663	21.009	986
3	-12.892	13.489	-68.992	. 664	21.008	879
5	-12.092	13.490	-68.993	. 664	21.007	072
5	-12.092	13.490	-68.993	. 664	21.007	065
5	-12.092	13,491	-68.994	. 665	21.006	050
5	-12.092	13.492	-60.995	. 665	21.005	050
5	-12.092	13.493	-68.996 -68.996	. 665	21.004	043
5	-12. <b>092</b> -12. <b>09</b> 2	13,493 13,494	-68.996 -68.996	.666	21.004	036
5	-12.092	13.495	-68.997 -68.998	. 666 . 666	21. <b>003</b> 21. <b>00</b> 2	~. 929
5	-12.092	13.496	-68.999	. 6 <b>6</b> 7	21.002	022 014

TABLE A-III (CONT)

AY	BETA	THETR(RAY)	HORMAL	<u> </u>	ALPHA2	RHO 2
5	-12.892	13, 496	-68.999	. 667	21.961	887
Š	-12.092	13.497	-69.000	. 667	21.000	000
5	-12.892	13.496	-68.999	. 667	21.001	007
5	-12.092	13.496	-68.999	. 667	21.001	006
5	-12.892	13,496	-68.999	. 667	21.001	886
5	-12.092	13,497	-68.999	. 667	21.001	005
5	-12.892	13.497	-69.000	. 667	21.000	004
5	-12.092	13.497	-69.000	. 667	21.000	004 003
5	-12.092	13.497 13.497	-69.000 -69.000	. 667 . 667	21.990 21.898	002
5 5	-12. <b>89</b> 2 -12. <b>89</b> 2	13.497	-69.000	. 667	21.000	881
5	-12.092	13.497	-69.000	. 667	21.800	001
5	-12.892	13.497	-69.000	.667	21.000	808
5	-12.892	13.497	-69.000	. 667	21.898	001
5	-12.892	13.497	-69.000	.667	21.068	001
5	-12.092	13.497	-69.000	. 667	21.000	891
5	-12.892	13.497	-69.000	. 667	21.000	061
5	-12.092	13.497	-69.000	. 667	21.000	000
5	-12.092	13.497	-69. <b>000</b>	.667	21.900	006
5	-12.092	13.497	-69.888	.667	21.000	80
5	-12.692	13.497	-69.000	. 667	21.000	006
5	-12.092	13.497	-69.000	. 667	21.000	006
5 5	-12.892 -12.892	13.497 13.497	-69.000 -69.000	.667 .667	21. <b>999</b> 21. <b>889</b>	-, 006 -, 006
3	-16.076	19.471	-67,000		21.000	004
6	-16.148	11.126	-66.623	0. <b>000</b>	23.377	-16.146
6	-16.140	11.239	-66.742	. 048	23.258	-15.519
6	-16.140	11.359	-66.862	. 986	23.138	-14.88
6	-16.140	11.479	-66.982	. 120	23.018	-14.227
6 6	-16.140 -16.140	11.6 <b>0</b> 1 11.723	-67.1 <b>04</b> -67.226	.160 .200	22.896 22.774	-13.550 -12.860
6	-16.140	11.845	-67.348	. 248	22.652	-12.157
6	-16.140	11.968	-67.471	. 280	22.529	-11.436
Ğ	-16.140	12.090	-67.593	. 320	22.407	-18.68
6	-16.140	12.213	-67.716	. 360	22.284	-9.91
6	-16.140	12.336	-67.839	. 480	22.161	-9.128
6	-16.140	12.458	-67.961	. 448	22.039	-8.319
6	-16.148	12.579	-68.082	. 488	21.918	· -7.481
6	-16.146	12.700	-68.203	. 521	21.797	-6.63
6	-16.148	12.819	-68.322	. 561	21.678	-5.75
6	-16.140	12.938	-68.441	. 601	21.559	-4.86
6	-16.140	13.054	-68.557	. 641	21.443	-3.93
6	-16.140	13.169	-68.672	. 681	21.326	-2.996
•	-16.140 -16.140	13.281 13.396	-68.784 -68.893	.721 .761	21.216 21.1 <b>0</b> 7	-2.019 -1.02
•	-16,140	13.281	-68.784	.721	21.216	-2.019

TABLE A-III (CONT)

AY	BETA	THETA(RAY)	HORMAL	\$ 	ALPHA2	RHO 2
6	-16,140	13.2 <del>9</del> 2	-68.795	.725	21.205	-1.926
6	-16.140	13.303	-68.986	.729	21.194	-1.821
i	-16.140	13.314	-68.817	.733	21.183	-1.722
6	-16.140	13.325	-68.828	.737	21.172	-1.623
6	-16.140	13.336	-68.839	.741	21.161	-1.52
6	-16.140	13.347	-68.959	.745	21.150	-1.42
6	-16.140	13.358	-68.861	.749	21.139	-1.32
6	-16.140	13.369	-68.872	.753	21.128	-1.22
6	-16.140	13.380	-68.883	. 757	21.117	-1.123
6	-16.140	13.398	-68.893	.761	21.197	-1.02
6	-16.148	13.461	-68.984	.765	21.096	92
6	-16.140	13.412	-68.915	.769	21.085	820
6	-16,140	13.423	-68.926	. 773	21.074	71
6	-16.140	13.433	-68.936	.777	21.064	61
6	-16.140	13.444	-68.947	.781	21.053	51
6	-16.140	13.455	-68.958	.785	21.042	41
6	-16.148	13.465	-68.968	.789	21.032	-,30
6	-16.140	13.476	-68.979	. 793	21.021	20
6	-16.140	13.487	-68.989	. 797	21.011	10
6	-16.140	13.476	-68.979	. 793	21.021	20
6	-16.140	13.477	-68.980	. 793	21.020	19
6	-16.140	13.478	-68.981	.794	21.019	186 176
6	-16.140 -16.140	13.479 13.480	-68.982 -68.983	.794 .794	21.018 21.017	16
6	-16.140	13.481	-68.984	.795	21.016	15
6	-16.140	13.482	-68.985	.795	21.815	149
6	-16.140	13.483	-68.986	.796	21.014	13
6	-16.140	13.484	-68.987	.796	21.013	124
6	-16.140	13.485	-68.988	.796	21.012	11
6	-16.149	13.487	-68.989	.797	21.011	103
6	-16.140	13.488	-68.991	.797	21.009	89
6	-16.140	13.489	-68.992	.798	21.006	003
6	-16.140	13.490	-68.993	. 798	21.007	97
6	-16.140	13.491	-68.994	. 798	21.006	96
6	-16.148	13.492	-68.995	.799	21.005	05
6	-16.148	13.493	-68.996	.799	21.084	84
6	-16.148	13.494	-68.997	. 800	21.003	03
6	-16.140	13.495	-68.998	. 800	21.002	92
6	-16.140	13.496	-68.999	. 800	21.001	016
6	-16.140	13.495	-68.998	. 900	21.002	02
6	-16.140	13.495	-60.998	. 899	21.002	026
6	-16.140	13.495	-68.998	. 800	21.002	019
6	-16.140	13.495	-68.998	. 800	21.002	019
6	-16.140	13.495	-68.998	. 800	21.092	01
6	-16.140	13.495	-68.998	. 800	21.002	010
6	-16.140	13.496	-68.999	. 800	21.001	014

TABLE A-III (CONT)

AY	BETA	THETA(RAY)	HORMAL	s 	ALPHA2	RHO 2
6	-16,148	13.496	-68.999	. 998	21.001	013
6	-16.140	13,496	-68.999	. 888	21.001	012
6	-16.140	13,496	-68.999	. 806	21.801	911
6	-16.148	13,496	-68.999	. 888	21.901	010
6	-16.148	13.496	-68.999	. 888	21.001	009
6	-16.140	13,496	-60.999	. 800	21.001	098
6	-16.148	13.496	-68.999	.801	21.001	007
6	-16.148	13.496	-68.999	. 881	21.001	006
6	-16.148	13.497	-68.999	.861	21.001	005
6	-16.140	13.497	-69.000	. 901	21.800	004
6	-16.140	13.497	-69.000	. 881	21.000	003
6	-16.149	13.497	-69.080	.861	21.886	062
6	-16.140	13.497	-69.000	. 891	21.000	00 1
6	-16.140	13.497	-69.000	.801	21.800	996
7	-21.114	10.008	-65.591	e. eee	24.489	-21.114
7	-21.114	19.246	-65.749	.047	24.251	-20.394
7	-21.114	19.406	-65,969	.093	24.091	-19.647
7	-21.114	10.578	-66.873	.140	23.927	-18.872
7	-21.114	10.736	-66.239	.187	23.761	-18.968
7	-21.114	18.985	-66.488	. 234	23.592	-17.233
7	-21.114	11.076	-66.579	. 288	23.421	-16.366
7	~21.114	11.249	-66.732	.327	23.248	-15.466
7	~21.114	11.424	-66.926	.374	23.074	-14.531
7	~21.114	11.600	-67.103	. 428	22.897	-13.568
7	-21.114	11.778	-67.286	. 467	22.728	-12.550
7	-21.114	11.956	-67.439	.514	22.541	-11.500
7	-21.114	12.135	-67.637	. 561	22.363	-10.418
7	-21.114	12.313	-67.816	. 607	22.184	-9.27€
7	-21.114	12.491	-67.994	. 654	22.006	~8.097
7	-21.114	12.667	-68.178	.701	21.830	-6.872
7	-21.114	12.841	-60.344	.747	21.656	-5.599
7 7	-21.114	13.012	-68.515	. 794	21.485	-4.277
7	-21.114 -21.114	13.179 13.341	-68.692 -68.844	. 841 . 88 <b>2</b>	21.318	-2.984
7	-21.114	13.179	-68.682	.841	21.1 <b>56</b> 21.318	-1.479 -2.984
7	-21.114	13.195	-68.698	.846	21.302	-2.764
7	-21.114	13.212	-68.715	. 850	21.285	-2.623
7	-21.114	13.228	-68.731	. 853	21.269	-2.482
7	-21.114	13.244	-68.747	. 860	21.253	-2.340
7	-21.114	13.260	-68.763	. 864	21.237	-2.198
7	-21.114	13.277	-68.788	. 869	21.220	-2.055
7	-21.114	13.293	-68.796	.874	21.294	-1.912
7	-21.114	13.309	-68.812	.878	21.188	-1.768
7	-21.114	13.325	-68.828	. 883	21.172	-1.624
7	-21.114	13.341	-68.844	. 864	21.156	-1.479

TABLE A-III (CONT)

AY	<b>DETA</b>	THETA(RAY)	HORMAL	<b>S</b>	ALPHA2	RHO
7	-21.114	13.357	-68.860	.892	21.148	-1.33
7	-21.114	13.373	-68.876	. 897	21.124	-1.18
7	-21.114	13.388	-68.891	. 982	21.189	-1.04
7 7	-21.114	13.404	-68.987	. 986	21. <b>09</b> 3 21. <b>0</b> 77	89· 74
7	-21.114	13.420	-60.923 -68.938	.911 .916	21.077	59
<b>,</b>	-21.114 -21.114	13.435 13.451	-68.954	. 920	21.046	44
7	-21.114	13.466	-68.969	. 925	21.031	30
7	-21.114	13.482	-68.985	. 930	21.015	15
7	-21.114	13.497	-69.000	.934	21.000	00
8	-27.265	8.626	-64.129	0.000	25.871	-27.26
8	-27.265	8.828	-64.323	. 053	25.677	-26.49
8	-27.265 -27.265	9.021 9.229	-64.524 -64.732	.107 .160	25.476 25.268	-25.68 -24.82
8	-27.265	9.444	-64.947	.214	25.053	-23.92
8	-27,265	9.665	-65.168	. 267	24.832	-22.98
8	-27.265	9.894	-65.397	. 320	24.603	-21.98
8	-27.265	10.129	-65.632	.374	24.368	-20.92
8	-27.265	10.371	-65.874	. 427	24.126	-19.81
8	-27.265	10.620	-66.122	. 480	23.878	-18.63
9	-27.265	10.874	-66.377	. 534	23.623	-17.38
8	-27.265 -27.265	11.134	-66.637 -66.901	. 587 . 641	23.363 23. <b>099</b>	-16.06 -14.66
8	-27.265 -27.265	11.398 11.666	-67.169	. 694	22.831	-13.18
8	-27.265	11.936	-67.439	.747	22.561	-11.61
ě	-27.265	12.208	-67.711	. 891	22.289	-9.95
8	-27.265	12.478	-67.981	. 854	22.019	-8.18
8	-27.265	12.745	-68.248	. 988	21.752	-6.31
8	-27.265	13.006	-68.509	. 961	21.491	-4.32
8	-27.265	13.258	-68.761	1.014	21.239	-2.22
9	-27.265	13.006	-60.509	.961	21.491	~4.32
•	-27.2 <b>65</b> -27.2 <b>65</b>	13.031 13.057	-68.534 -68.568	. 966 . 972	21.466 21.440	-4.12 -3.91
:	-27.265	13.082	-68.585	. 977	21.415	-3.78
•	-27.265	13.100	-68.611	.982	21.389	-3.50
ě	-27.265	13.133	-68.636	. 986	21.364	-3.29
8	-27.265	13.150	-68.661	. 993	21.339	-3.87
8	-27.265	13.183	-68.686	. 998	21.314	-2.86
•	-27.265	13.208	-68.711	1.004	21.289	-2.65
•	-27.265	13.233	-68.736	1.009	21.264	-2.44
8	-27.265 -37.365	13.258	-68.761 -68.761	1.014	21.239	-2.22
•	-27.265 -27.265	13.282	-68.785	1.020 1.025	21.215 21.1 <b>90</b>	-2.00 -1.78
•	-27.265 -27.265	13.3 <b>0</b> 7 13.331	-68.810 -68.834	1.025	21.166	~1.57
i	-27.265	13.355	-68.858	1.036	21.142	-1.34

TABLE A-III (CONT)

AY	BETA	THETA(RAY)	HORMAL	\$ 	ALPHA2	RHO 2
8	-27.265	13.379	-68.882	1.041	21.118	-1,127
9	-27.265	13.483	-68.986	1.046	21.094	904
8	-27.265	13.427	-68.938	1.052	21.070	686
8	-27.265	13.450	-68.953	1.057	21.047	45
8	-27.265	13.474	-68.977	1.962	21.023	-,228
8	-27.265	13.450	-68.953	1.057	21.847	~, 455
8	-27.265	13.453	-68.956	1.058	21.044	~, 432
8	-27.265	13.455	-68.958	1.058	21.042	409
8	-27.265	13.457	-68.960	1.059	21.840	387
8	-27.265	13.468	-68.963	1.059	21.037	~.364
8 8	-27.265	13.462	-68.965	1.060	21.035	~.341
9 8	-27.265 -27.265	13.464 13.467	-68.967 -68.979	1.060 1.061	21.033 21.030	319 296
8	-27.265 -27.265	13.469	-68.972	1.061	21.028	273
8	-27.265	13.471	-68.974	1.862	21.026	25
9	-27.265	13.474	-68.977	1.062	21.023	22
8	-27.265	13.476	-68.979	1.063	21.021	20
9	-27.265	13.478	-68.981	1.063	21.019	18
8	-27.265	13.481	-68,984	1.864	21.016	160
8	-27.265	13.483	-68,986	1.065	21.014	13
8	-27.265	13.485	-68.988	1.065	21.012	11
8	-27.265	13.488	-68.991	1.866	21.869	89
8	~27.265	13.490	-68.993	1.066	21.007	869
8	-27.265	13.492	-68.995	1.867	21.005	040
8	-27.265	13.495	-68.998	1.067	21.002	023
9	-27.265	13.492	-68.995	1.867	21.005	846
3	-27.265	13.493	-68.996	1.067	21.004	04
9	-27.265	13.493	-69.996	1.067	21.004	04
3	-27.265	13.493	-68.996	1.867	21.004	03
3	-27.265	13.493	-68.996	1.967	21.804	03
8 B	-27.265	13.494	-68.997	1.067	21.003	034
•	-27.265 -27.265	13.494	-68.997	1.067	21.003	03
•	-27.265 -27.265	13.494 13.494	-68.997 -68.997	1.867 1.867	21. <b>003</b> 21. <b>00</b> 3	931 921
•	-27.265	13.494	-68.997	1.067	21.003	92
3	-27.265	13.495	-68.998	1.067	21.002	823
	-27.265	13.495	-68.998	1.867	21.002	02
•	-27,265	13.495	-68.998	1.067	21.002	918
ĺ	-27.265	13.495	-68.998	1.067	21.002	016
ě	-27,265	13.496	-64.999	1.067	21.861	01
•	-27.265	13.496	-68.999	1.067	21.001	011
•	-27.265	13,496	-68.999	1.068	21.001	909
•	-27.265	13.496	-68.999	1.068	21.001	007
•	-27.265	13.497	-69.000	1.868	21.000	005
3	-27.265	13.497	-69.888	1.068	21.000	002
9	-27.265	13.497	-69.900	1.868	21.000	005

TABLE A-III (CONT)

The second second

RAY	BETA	THETACRAY	NORMAL	\$	ALPHR2	RHQ 2
8	-27.265	13.497	-69.000	1.068	21.000	994
8	-27.265	13.497	-69.000	1.068	21.000	004
8	-27.265	13,497	-69.000	1.068	21.000	004
8	-27.265	13.497	-69.000	1.068	21.000	004
8	-27.265	13.497	-69.000	1.068	21.000	003
8	-27.265	13.497	-69.800	1.068	21.000	003
8	-27.265	13.497	-69.000	1.068	21.000	003
8	-27.265	13.497	-69.000	1.068	21.000	003
8	-27.265	13.497	-69.000	1.068	21.000	003
8	-27.265	13.497	-69.000	1.068	21.000	002
8	-27.265	13.497	-69.000	1.068 1.068	21.00 <del>0</del> 21.000	002 002
8 8	-27.265 -27.265	13.497 13.497	-69.000 -69.000	1.068	21.000	002
9	-27.265	13.497	-69.000	1.068	21.000	001
8	-27.265	13.497	-69.000	1.068	21.000	001
8	-27.265	13.497	-69,000	1.068	21.999	001
8	-27.265	13.497	-69,000	1.068	21.000	001
ě	-27,265	13.497	-69.980	1.068	21.000	000
8	-27.265	13.497	-69.000	1.068	21.990	000
9	-34.865	6.562	-62.065	a. 200	27.935	-34.865
9	-34.865	6.769	-62,272	. 060	27.728	-34.142
9	-34.865	6.989	-62,492	. 120	27.508	-33.368
9	-34.865	7.221	-62.724	. 180	27.276	-32.539
9	-34.865	7.467	-62.978	. 248	27.030	-31.649
9	-34.865	7.728	-63.231	. 306	26.769	-30.693
9	-34.865	8.084	-63.507	. 360	26.493	-29.661
9	-34.865	8.296	-63.799	.428	26.2 <del>0</del> 1	-28.547
9	-34.865	8.6 <b>86</b>	-64.109	. 480	25.891	-27.341
9	-34.865	8.935	-64.437	.541	25.563	-26.032
9	-34.865	9.282	-64.785	. 601	25.215	-24.609
9	-34.865	9.648	-65.151	.661	24.849	-23.054
9	-34.865	10.034	-65.537	.721	24,463	-21.356 -19.495
•	-34.865	19.439 10.861	-65.942 -66.364	.781 .841	24. <b>058</b> 23.63 <b>6</b>	-17.452
,	-34.865 -34.865	11.298	-66.801	. 961	23.199	-15.204
÷	-34.865	11.747	-67,250	. 961	22.750	-12.727
9	-34.865	12.201	-67.794	1.021	22.296	-9.994
ź	-34.865	12.652	-68.155	1.001	21.845	-6.986
÷	-34.865	13.689	-68.592	1.141	21.408	-3.656
ý	-34.865	12.652	-68.155	1.001	21.845	-6.986
ý	-34.865	12.696	-68.199	1.087	21.801	-6.662
9	-34.865	12.741	-68.244	1.093	21.756	-6.341
•	-34.865	12.785	-68.288	1.099	21.712	-6.016
•	-34.865	12.829	-68.332	1.105	21.668	-5.689
9	-34.865	12.873	-68.376	1.111	21.624	-5.358

TABLE A-III (CONT)

AY	BETA	THETA(RAY)	NORMAL	<u> </u>	ALPHA2	RHO 2
9	-34.865	12.916	-68.419	1.117	21.581	-5.924
ģ	-34.865	12.960	-68.463	1.123	21.537	-4.68
ý	-34.865	13.003	-68.596	1.129	21.494	-4.34
ý	-34.865	13.046	-68.549	1.135	21.451	-4.00
9	-34.865	13.089	-68.592	1.141	21.408	-3.656
9	-34.865	13.131	-68.634	1.147	21.366	-3.30
9	-34.865	13.173	-68.676	1.153	21.324	-2.95
9	-34.865	13.215	-68.718	1.159	21.282	-2.595
9	-34.865	13.256	-68.759	1.165	21.241	-2.23
9	-34.865	13.297	-68.800	1.171	21.200	-1.87
9	-34.865	13.338	-68.841	1.177	21.159	-1.504
9	-34.865	13.378	-68.881	1.183	21.119	-1.133
9	-34.865	13.418	-68.921	1.189	21.079	75
9	-34.865	13.458	-68.961	1.195	21.039	38
9	-34.865	13.418	-68.921	1.189	21.079	75
9	-34.865	13.422	-68.925	1.190	21.075	72
9	-34.865	13.426	-68.929	1.190	21.071	68
9	-34.865	13.430	-68.933	1.191	21.067	64
9	-34.865	13.434	-68.937	1.192	21.063	60
9	-34.865	13.438	-68.941	1.192	21.059	57
9	-34.865	13.442	-68.945	1.193	21.055	53
9 9	-34.865	13.446	-68.949	1.193	21.051	49
9	-34.865 -34.865	13.450 13.454	-68.953 -68.957	1.194 1.195	21.047 21.043	457 419
9	-34.865	13.458	-68.961	1.195	21.039	38
9	-34.865	13.462	-68.965	1.196	21.035	34
ģ	-34.865	13.466	-68.969	1.196	21.031	30
ý	-34.865	13.470	-68.973	1.197	21.827	267
ģ	-34,865	13.474	-68.977	1.198	21.023	229
9	-34.865	13.478	-68.981	1.198	21.019	19
9	-34.865	13.481	-68.984	1.199	21.016	15
9	-34.865	13.485	-68.988	1.199	21.012	11
9	-34.865	13.489	-68.992	1.200	21.998	07
9	-34.865	13.493	-68.996	1.201	21.004	038
9	-34.865	13.489	-68.992	1.200	21.008	07
9	-34.865	13.496	-68. <del>99</del> 3	1.200	21.007	97
9	-34.865	13.496	-68.993	1.200	21.007	069
9	-34.865	13.490	-68.993	1.200	21.007	86
9	-34.865	13,491	-68.994	1.200	21.006	06
9	-34.865	12.491	-68.994	1.200	21.006	057
9	-34.865	13.492	-68.995	1.200	21.005	054
•	-34.865	13.492	-68.995	1.200	21.005	05
9	-34.865	13.492	-68.995	1.201	21.005	04
9	-34.865	13.493	-68.996	1.201	21.004	04
•	-34. <b>86</b> 5 -34. <b>86</b> 5	13.493 13.494	-68.9 <b>96</b> -68.997	1.201 1.201	21.004 21.003	036 034

TABLE A-III (CONT)

AY	BETA	THETR(RRY)	NORMAL	<b>s</b>	ALPHA2	RHO 2
9	-34.865	13.494	-68.997	1.201	21.003	031
ý	-34.865	13,494	-68.997	1.201	21.003	027
ģ	-34.865	13.495	-68,998	1.201	21.002	023
ģ	-34.865	13.495	-68.998	1.201	21.002	019
ý	-34.865	13.495	-68,998	1.201	21.002	015
ý	-34.865	13.496	-68,999	1.201	21.001	011
ģ	-34.865	13.496	-68.999	1.201	21.001	008
9	-34.865	13.497	-69.000	1.201	21.000	004
9	-34.865	13.496	-68.999	1.201	21.001	008
9	-34.865	13.496	-68.999	1.201	21.001	097
9	-34.865	13.496	-68.999	1.201	21.001	007
9	-34.865	13.496	-68.999	1.291	21.001	007
9	-34.865	13.496	-68.999	1.201	21.001	006
9	-34.865	13.496	-68.999	1.201	21.001	006
9	-34.865	13.496	-68.999	1.201	21.001	00
9	-34.865	13.497	-68.999	1.201	21.001	005
9	-34.865	13.497	-69.000	1.201	21.000	00
9	-34.865	13.497	-69.000	1.201	21.000	99
9	-34.865	13.497	-69.000	1.201	21.000	00
9	-34.865	13.497	-69.000	1.201	21.000	00
9	-34.865 .	13.497	-69.000	1.261	21.000	~.003
9	-34.865	13.497	-69.00 <b>0</b>	1.201	21.000	~.803
9	-34.865	13.497	-69.000	1.291	21.000	00
9	-34.865	12.497	-69.000 -69.000	1.201 1.201	21. <b>000</b> 21.0 <b>00</b>	003 003
9	-34.865 -34.865	13.497 13.497	-69.000	1.201	21.000	00
9	-34.865	13.497	-69.000	1.201	21.000	98
9	-34,865	13.497	-69.000	1.201	21.000	00
-						
0	-44.118	3.748	-55 , 243	9.888	30.757	-44.11
0	-44.118	3.899	-59.402	.067	30.598	-43.62
	-44,118	4.071	-59.574	. 133	30.426	-43.076
	-44.118	4.259	-59.762	. 200	30.238	-42.48
0	-44.116	4.463	-59.966	. 267	38.034	-41.829
0	-44.118	4.688	-60.191	. 334	29.889	-41.109
9	-44.118	4.935	-60.438	. 400	29.562	-40.310
-	-44.118	5.208	-60.711	. 467	29.289	~39.420
8	-44.118 -44.118	5.511 5.848	-61.014 -61.351	.534	28.986	-38.420 -37.290
9	-44.118	6.226	-61.729	. 601 . 667	28.649 28.271	-36.02
8	-44.118	6.650	-62.153	.734	27.847	-34.559
	-44.118	7.129	-62.631	. 801	27.369	-32.87
9	-44.118	7.669	-63.172	. 868	26.328	-30.90
e	-44.118	9.283	-63.786	. 934	26.214	-28.60
ø	-44,118	8.978	-64.481	1.001	25.519	-25.85
9	-44.118	9.763	-65.266	1.068	24.734	-22.556

TABLE A-III (CONT)

AY	BETA	THETA(RAY)	NORMAL	\$	ALPHA2	RHO 2
18	-44.118	10.638	-66.141 -67.092	1.134 1.201	23.859 22.9 <b>08</b>	-18.544 -13.618
10 10	-44.118 -44.118	11.590 12.574	-68.077	1.268	21.923	-7.527
10	-44.118	11.590	-67.092	1.201	22.908	-13.618
	-44.118	11.688	-67.191	1.208	22.809	-13.066
. 0	-44.118	11.786	-67.289	1.215	22.711	-12.50
ë	-44.118	11.884	-67.387	1.221	22.613	-11.92
9	-44.118	11.983	-67.486	1.228	22.514	-11.33
9	-44.118	12.082	-67.585	1.235	22.415	-10.73
ě	-44.118	12.181	-67.684	1.241	22.316	-10.126
ē	-44.118	12.279	-67.782	1.248	22.218	-9.492
9	-44.118	12.378	-67.881	1.255	22.119	-8.85
0	-44.118	12.476	-67.979	1.261	22.021	-8.196
0	-44.118	12.574	-68.077	1.268	21.923	-7.527
9	-44.118	12.671	-68.174	1.275	21.826	-6.843
8	-44.118	12.767	-68.270	1.281	21.730	-6.14
0	-44.118	12.863	-68.366	1.288	21.634	-5.431
0	-44.118	12.958	-68.461	1.295	21.539	-4.70
0	-44.118	13.051	-68.554	1.301	21.446	-3.959
9	-44.118	13.144	-68.647	1.308	21.353	-3.199
8	-44.118	13.235	-68,738	1.315	21.262	-2.42
.0	-44.118	13.324	-68.327	1.321	21.173	-1.63
.0	-44.118	13.411	-68.914	1.328	21.086	824
0	-44.118	13.324	-68.827	1.321	21.:73 21.164	-1.632 -1.552
9	-44.118	13.333	-68.836	1.322	21.155	-1.47
0	-44.118 -44.118	13.342 13.350	-68.845 -68.853	1.323	21.147	-1.39
ě	-44.118	13.359	-68.862	1.324	21.138	-1.31
9	-44.118	13.368	-68.871	1.325	21.129	-1.23
9	-44.118	13.377	-68.880	1.325	21.126	-1.149
ē	-44.118	13.385	-68.988	1.326	21.112	-1.868
ě	-44.118	13.394	-68.897	1.327	21.193	98
ě	-44.118	13.483	-68.906	1.327	21.894	90
ě	-44.118	13.411	-68.914	1.328	21.086	82
•	-44.118	13.420	-68.923	1.329	21.077	743
0	-44.118	13.429	-68.932	1.329	21.068	66
8	-44.118	13.437	-68.948	1.330	21.068	579
8	-44.118	13.446	-68.949	1.331	21.051	49
•	-44.118	13.455	-68.957	1.331	21.043	414
0	-44.118	13.463	-68.966	1.332	21.034	33
0	-44.118	13.472	-68.975	1.333	21.025	249
	-44.118	13.488	-60.983	1.333	21.017	166
	-44.118	13.489	-68.992	1.334	21.808	083
8	-44.118	13.488	-68.983	1.333	21.017	166
9	-44.118	13.401	-68.984	1.333	21.016	156
9	-44.118	13.482	-68.985	1.333	21.815	150

TABLE A-III (CONT)

RY	BETA	THETR(RAY)	NORMAL	\$ 	ALPHA2	RHQ 2
10 10	-44.118 -44.118	13.483 13.483	-68.98 <b>6</b> -68.986	1.334	21.014 21.014	141 133
10	-44.118	13.484	-68.987	1.334	21.014	133
10	-44.118	13.485	-68.988	1.334	21.013	116
10	-44.118	13.486	-68.989	1.334	21.012	108
19	-44.118	13.487	~68.990	1.334	21.011	100
10	-44.118	13.488	-68.991	1.334	21.009	091
18	-44.118	13.489	-68.992	1.334	21.009	083
18	-44.118	13.489	-68.992	1.334	21.008	075
10	-44.118	13.490	-68,993	1.334	21.007	067
10	-44.118	13.491	-68.994	1.334	21.006	958
10	-44.118	13.492	-68.995	1.334	21.005	050
19	-44.118	13.493	-68.996	1.334	21.004	842
10	-44.118	13,494	-68, 997	1.334	21.003	633
18	-44.118	13,495	-68.997	1.334	21.003	025
10	-44.118	13.495	-68.998	1.335	21.002	017
10	-44.118	13,496	-68.999	1.335	21.881	008
10	-44.118	13,496	-68.999	1.335	21.081	008
18	-44.118	13,496	-68.999	1,335	21.001	087
10	-44.118	13,496	-68.999	1.335	21.001	007
10	-44.118	13,496	-68,999	1.335	21.001	806
10	-44.118	13,497	-68,999	1.335	21.001	205
10	-44.118	13,497	-69.000	1.335	21.000	004
	-44.118	13,497	-69.000	1.335	21.000	003
10	-44.118	13,497	-69.000	1.335	21.000	002
10	-44.118	13,497	-69.000	1.335	21.000	002
10	-44.118	13,497	-69.000	1.335	21.000	001

TABLE A-IV

SECOND SURFACE COORDINATE (X,Y) VALUES, S, ALPHA2 AND RHO2 FOR THE FAMILY OF SURFACES IN FIGURES 17 AND 18. THE COLUMN LABELED BEGIN RAY CORRESPONDS TO THE FAMILY MEMBER.

Ray n	Next RAY	Xsurf (next)	Ysurf (next)	S (next)	Alpha2 (next)	RHQ 2 . (next)	
ı	1	. 362	. 008	. 133	21.000	000	
1	2	. 649	.118	. 133	21.201	-1.886	
1	3	.935	.221	. 132	21.466	-4.122	
1	4	1.220	.333	.130	21.824	-6.831	
1	5	1.504	.447	. 125	22.321	-10.147	
1	6	1.786	. 563	.118	23.024	-14.262	
1	7	2.867	. 682	.107	24.043	-19,425	
1	8	2.344	.805	. 090	25.538	-25.934	
1	9	2.616	. 936	. 066	27.707	-34.070	
1	10	2.882	1.076	. 836	30.688	-43.901	
2	2	.724	. 000	. 267	21.201	~.000	
2	3	1.010	.111	. 266	21.228	-2.125	
2	4	1.296	. 222	. 265	21.538	-4.693	
2	5	1.581	.334	. 262	21.973	-7.878	
2 2	6	1.865	.449	. 256	22.603	-11.968	
2	7	2.146	. 366	.248	23.542	-16.978	
2	ė	2.425	.687	. 234	24.971	-23.577	
2	ÿ	2.699	.815	.212	27.147	-32.074	
2	10	2.967	. 953	.179	30.300	-42.677	
_	_		222	400	21.228	000	
3	3	1.086	. 000	. 4 <b>00</b> . 399	21.262	-2,420	
3	4	1.372	.111	.398	21.633	-5.420	
3 3	5	1.658	.335	.394	22.186	-9.251	
	7	1.943 2.226	. 450	.388	23.021	-14.243	
3 3	8	2.506	.570	.377	24.354	-20.865	
3	9	2.782	.695	.358	26.502	-29.695	
3	19	3.052	.829	.329	29.826	-41.164	
,	10	3.034	. 627	. 367	27.040	******	
4	4	1.449	. 986	. 534	21.262	000	
4	5	1.734	.111	. 532	21.397	-2.810	
4	6	2.029	. 223	. 531	21.766	-6.414	
4	7	2.384	. 336	. 527	22.493	-11.208	
4	8	2.586	. 453	.519	23.690	-17.757	
4	9	2.864	. 575	. 584	25.766	-26.849	
4	10	3.136	.786	.478	29.242	-39.260	
5	5	1.811	. 000	. 667	21.307	000	
5	6	2.896	.111	. 666	21.371	-3.349	
5	ž	2.302	. 223	. 664	21.970	-7.849	
5	8	2.665	.337	. 658	23.011	-14.189	
5	9	2.946	.457	.647	24.932	-23.412	
5	10	3.220	. 584	. 626	28.510	-36.832	
6	6	2.173	. 200	. 801	21.371	900	

O

TABLE A-IV (CONT)

Begin Burf	Hext Surf	Xsurf (next)	Ysurf (next)	\$ (next)	Alpha2 (next)	RHQ 2 (next)
6 6 6	7 8 9	2.458	.112	.799	21.469	-4.143
6	8	2.743	. 224	. 796	22.313	-10.099
6	9	3.026	. 340	.789	24.002	-19.227
6	10	3.303	. 463	. 773	27.578	-33.615
7 7 7 7	7 8	2.535	. 000	. 934	21.469	000
7	9	2.8 <b>20</b>	.112	. 932	21.634	-5,429
7	9	3.105	. 225	. 928	22.996	-14.107
7	10	3.385	. 344	.917	26.378	-29.225
9	8	2.897	. 888	1.068	21.634	888
8 8	9	3.182	.113	1.864	21.971	-7.855
8	10	3.465	. 227	1.059	24.843	-23.029
9	9	3.259	. 000	1.291	21.971	000
9	10	3.543	.114	1.196	22.986	-14.051
. 0	10	3.622	. 888	1.335	22.986	961

TABLE A-V

COMPARISON OF THE MAXIMUM ALLOWED LENGTH OF THE RAY IN THE LENS QA AND THE ACTUAL VALUE USED  $\mathbf{S}_{\text{MAX}}$ , FOR EACH SURFACE IN FIGURES 17 AND 18. ALPHA2 AND RHO2 ARE THE VALUES AT  $\mathbf{S}_{\text{MAX}}$ .

R	AY	QA	Smax	Alpha2	RHO 2
				البسن المسائد المسائد	
	_		400	21,000	-, 980
	1	. 133	. 133	21.201	000
	2 3	. 267	. 267	21.228	000
	3	. 400	. 400		800
	4	. 534	. 534	21.262	800
	5 6	. 667	. 667	21.387	
	6	. 88 1	.801	21.371	000
	7	. 934	. 934	21.469	~. 969
	•	1.968	1.068	21.634	~.000
	•	1.201	1.201	21.971	~.000
	Ó	1.335	1.335	22.986	991

TABLE A-VI

CALCULATED VALUES OF S AND ALPHA2 USED TO CONSTRUCT THE DESIGN CHART IN FIGURE 19 FOR THE FINAL DESIGN OF SURFACE NUMBER 1 in FIGURE 20.

RAY	BETA	THETA(RAY)	NORMAL	s 	ALPHA2	RH0 2
		12 217	-69 929	9.9 <b>99</b>	21.180	-1.697
1	-1.697 -1.697	13.317 13.326	-68.829 -68.829	. 007	21.171	-1.614
i	-1.697	13.325	-68.838	.013	21.162	-1.530
i	-1.697	13.344	-68.847	. 828	21.153	-1.447
i	-1.697	13.354	-68.856	. 027	21.144	-1.363
i	-1.697	13.363	-68.866	, 033	21.134	-1.279
i	-1.697	13.372	-68.875	. 040	21.125	-1.195
i	-1.697	13.381	-68.884	.047	21.116	-1.111
ī	-1.697	13.390	-68.893	. 853	21.107	-1.027
i	-1.697	13.399	-68.902	. 960	21.098	942
ī	-1.697	13.408	-68.911	. 967	21.089	857
ī	-1.697	13.417	-68.928	. 873	21.080	772
ĩ	-1.697	13.426	-68.929	. 699	21.071	687
i	-1.697	13.435	-68.938	. 887	21.862	602
1	-1.697	13.444	-68.947	. 893	21.053	517
1	-1.697	13.453	-68.956	. 100	21.044	431
1	~1.697	13.462	-68.965	. 107	21.035	345
1	-1.697	13.471	-68.974	.113	21.026	259
1	-1.697	13.479	-68.982	. 120	21.018	173
ı	-1.697	13.488	-68.991	.127	21.009	087
1	-1.697	13.479	-68.982	. 120	21.818	173
1	-1.697	13.489	-68.983	.121	21.017	164
1	-1.697	13.481	-68.984	. 121	21.016	156
1	-1.697	13.482	-68.985	. 122	21.015	147
1	-1.697	13.483	-68.986	.123	21.014	139
1	-1.697	13.484	-68.987	. 123	21.013	130
1	-1.697	13.485	-68.988	. 124	21.012	121
1	-1.697	13.486	-68.989	. 125	21.011	112
1	-1.697	13.486	-68.989	. 125	21.011	104
1	-1.697	13.487	-68,998	. 126	21.010	095
1	-1.697	13.488	-68.991	. 127	21.009	087
1	-1.697	13.489	-68.992	. 127	21.008	078
1	-1.697	13.496	-68,993 -68,994	. 126	21.667	<b>869</b> <b>86</b> 1
1	-1.697	13.491	-68, 995	. 129	21.006	052
1	-1.697	13.492	-68.996	. 129 . 13 <b>9</b>	21.0 <b>6</b> 5 21.004	043
1	-1.697	13.493 13.494	-68.9 <b>96</b>	. 131	21.864	835
1	-1.697 -1.697	13.494	-68.997	. 131	21.003	026
1	-1.697	13.495	-68.9 <del>98</del>	. 132	21.882	817
1	-1.697	13.496	-68,999	. 133	21.001	009
1	-1.697	13.495	-68.998	. 132	21.001	817
1	-1.697	13.495	-68.998	. 132	21.002	016
i	697	13.495	-68.998	. 132	21.002	016
i	-1.697	13.496	-68.999	. 132	21.001	015
i	-1.697	13.496	-68.999	.132	21.001	014
i	-1.697	13.496	-68.999	. 132	21.001	013

TABLE A-VI (CONT)

The second second

AY	BETA	THETR(RAY)	HORMAL	\$ 	ALPHA2	RHO 2
		10.406	-60 000		21.001	012
1	-1. <b>697</b> -1. <b>697</b>	13.496 13.496	-68.999 -68.999	.133	21.001	011
1	-1.697	13.496	-68.999	. 133	21.001	010
1	-1.697	13.496	-68.999	. 133	21.001	010
i	-1.697	13.496	-68.999	.133	21.961	009
i	-1.697	13.496	-68,999	.133	21.001	008
i	-1.697	13.496	-68.999	. 133	21.001	007
i	-1.697	13.496	-68,999	. 133	21.001	886
ī	-1.697	13.497	-68.999	.133	21.001	865
1	-1.697	13.497	-69.000	. 133	21.000	804
1	-1.697	13.497	-69.000	. 133	21.000	003
1	-1.697	13.497	-69.000	. 133	21.000	883
1	-1.697	13.497	-69.000	. 133	21.999	002
1	-1.697	13.497	-69.000	.133	21.000	801
1	-1.697	13.497	-69.000	. 133	21.000	002
1	-1.697	13.497	-69.080	. 133	21.899	902
1	-1.697	13.497	-69.000	.133	21.800	002
1	-1.697	13.497	-69.000	. 133	21.000	001
1	-1.697	13.497	-69.000	. 133	21.000	001
1	-1.697	13.497	-69.000	. 133	21.000	001
1	-1.697	13.497	-69.000	. 133	21.888	001
1	-1.697	13.497	-69.000	. 133	21.000	001
1	-1.697	13.497	-69.000 -69.000	. 133 . 133	21.899 21.888	001 801
i	-1.697 -1.697	13.497 13.497	-69.000	.133	21.000	001
i	-1.697	13.497	-69.000	.133	21.000	001
i	-1.697	13.497	-69.000	. 133	21,000	891
i	-1.697	13.497	-69.000	.133	21.888	991
i	-1.697	13.497	-69.000	. 133	21.000	991
ī	-1.697	13.497	-69.000	. 133	21.000	886
i	-1.697	13.497	-69.800	.133	21.000	800
1	-1.697	13.497	-69.888	. 133	21.000	900
1	-1.697	13.497	-69.000	. 133	21.000	906
1	-1.697	13.497	-69.000	. 133	21.000	996
2	-2.373	13.241	-68.743	6.666	21.257	-2.373
2	-2.373	13.254	-68.757	. 809	21,243	-2.258
2	-2.373	13.267	-68.770	.018	21.230	-2.142
2	-2.373	13.200	-68.783	.027	21.217	-2.026
2	-2.373 -2.373	13.293	-68.7 <del>9</del> 6	. 036	21.204	-1.916
2 2	-2.373 -2.373	13.306 13.319	-68.809 -68.822	. 845 . 854	21.191 21.17 <b>0</b>	-1,793 -1,676
2	-2.373 -2.373	13.317	-68.835	. 954 . 964	21.175	-1.558
2	-2.373	13.345	-68.848	. 673	21.152	-1,550
2	-2.373	13.358	-68.861	. 082	21.139	-1.323
2	-2.373	13.371	-68.874	.091	21.126	-1,294

TABLE A-VI (CONT)

RAY	DETA	THETR(RAY)	HORMAL	s 	ALPHA2	RHO 2
2	-2.373	13.384	-69.987	. 100	21.113	-1.085
2	-2.373	13.396	-68.899	. 109	21.101	966
2	-2.373	13.409	-68.912	.118	21.088	847
	-2.373	13.422	-68.925	. 127	21.975	727
2 2 2	-2.373	13.434	-68.937	. 136	21.063	606
2	-2.373	13.447	-68.950	.145	21.050	486
2 2 2	-2.373	13.460	-68.963	.154	21.037	365
2	-2.373	13.472	-68.975	. 163	21.025	244
2	-2.373	13.485	-68.988	. 172	21.012	122
2	-2.373	13.497	-69.0 <b>00</b>	. 182	21.999	000
2	-2.373	13.485	-68.988	.172	21.012	122
2	-2.373	13.486	-68.989	. 173	21.011	110
2	-2.373	13.487	-68.998	.174	21.010	098
2	-2.373	13.488	-68.991	. 175	21.009	885
2	-2.373	13.490	-68.993	. 176	21.007	073
2	-2.373	13.491	-68.994	.177	21.006	961
2	-2.373	13.492	-68.995	.178	21.005	049
Z	-2.373	13.493	-68.996	.179	21.004	037
2 2 2 2 2	-2.373	13.495	-68.998	. 188	21.002	024
2	-2.373	13.496	-68.999	. 181	21.001	012
2	-2.373	13.497	-69.000	. 182	21.600	000
2	-2.373	13.496	-68.999	. 181	21.901	012
2	-2.373 -2.373	13.496 13.496	-68.999 -68.999	. 1 <b>91</b> . 1 <b>9</b> 1	21.091 21.991	011 010
4	-2.373	13.496	-68.999	. 181	21.881	889
2	-2.373	13.496	-68.999	. 181	- 21.001	~. 807
5	-2.373	13.496	-68.999	. 181	21.801	896
5	-2.373	13.497	-69.808	. 191	21.000	805
Ž	-2.373	13.497	-69.980	. 181	21.000	~. 904
ž	-2.373	13.497	-69.888	. 181	21.000	~.002
2	-2,373	13.497	-69.888	. 181	21.000	001
2	-2.373	13.497	-69.800	. 182	21.800	868
2	-2.373	13.497	-69.800	. 181	21.000	991
2	-2.373	13.497	-69.000	. 181	21.900	001
2	-2.373	13.497	-69.000	. 181	21.999	981
2	-2.373	13.497	-69.000	. 181	21.000	001
2 2 2	-2.373	13.497	-69.800	. 181	21.000	001
2	-2.373	13.497	-69.000	. 181	21.000	661
2	-2.373	13.497	-69.000	. 181	21.000	999
2	-2.373	13.497	-69.900	. 191	21.900	000
2	-2.373	13.497	-69.900	. 192	21.000	000
2	-2.373	13.497	~69.000	. 182	21.000	906
3	-3.008	13.157	-68.660	0.000	21.340	-3.069
3	-3.088	13.175	-68.678	. 611	21.322	-2.939
3	-3.088	13.192	-68.695	. 823	21.395	-2.790

TABLE A-VI (CONT)

The second secon

O

AY	BETA	THETA(RAY)	HORMAL	\$	ALPHA2	RHO
		8				
3	-3.088	13.210	-68.713	. 034	21.287	-2.64
3	-3.888	13.227	-68.730	. 846	21.270	-2.49
3	-3.088	13.244	-68.747	. 957	21.253	-2.33
3	-3.008	13.262	-68.765	. 069	21.235	-2.18
3	-3.000 -3.000	13.279	-68.782 -68.799	.080 .092	21.218 21.2 <b>9</b> 1	-2.03 -1.88
3	-3.688	13.296 13.313	-68.816	. 103	21.184	-1.72
3	-3.088	13.330	-68.833	.115	21.167	-1.57
3	-3.088	13.347	-68.850	. 126	21.150	-1.42
3	-3.888	13.364	-68.867	.138	21.133	-1.26
3	-3.088	13.381	-68.884	.149	21.116	-1.10
3	-3.888	13.398	-68.901	. 161	21.099	95
3	-3.088	13.415	-68.918	.172	21.082	79
3	-3.088	13.431	-68.934	. 184	21.066	63
3	-3.088	13.448	-68.951	. 195	21.049	47
3	-3.088	13.464	-68.967	. 207	21.033	32
3	-3.088	13.481	-68.984	.218	21.016	16
3 3	-3.088 -3.008	13.497 13.481	-69.000 -68.984	.23 <b>0</b> .218	21.009 21.016	00 16
3 3	-3.688	13.482	-68.985	.219	21.015	14
3	-3.088	13.484	-68.987	. 220	21.813	12
3	-3.088	13.486	-68.989	.222	21.011	11
3	-3.088	13.487	-68.990	.223	21.010	09
3	-3.688	13.489	-68.992	. 224	21.008	08
3	-3.088	13.491	-68.993	. 225	21.807	96
3	-3.088	13.492	-68.995	. 226	21.005	84
3	-3.088	13.494	-68.997	.227	21.003	03
3	-3.068	13.495	-68.998	. 228	21.002	01
3 3	-3.088	13.495	-68.998	. 228	21.002	01 01
3 3	-3.060 -3.088	13.496 13.496	-68.999 -68.9 <del>9</del> 9	. 229 . 229	21.001 21.001	61
3 3	-3.088	13.496	-68.999	.229	21.001	01
3	-3.688	13.496	-68, 999	. 229	21.001	01
3	-3.000	13.496	-68,999	. 229	21.001	00
3	-3.000	13.496	-68.999	. 229	21.001	90
3	-3.088	13.497	-69.000	.229	21.998	00
3	-3.008	13.497	-69.000	. 229	21.000	00
3	-3.088	13.497	-69.0 <del>00</del>	. 229	21.000	86
3	-3.088	13.497	-69.000	. 230	21.000	00
3	-3.000	13.497	-69.888	. 229	21.000	80
3	-3.088	13.497	-69.000	. 229	21.900	00
3	-3. <b>008</b>	13.497 13.497	-69.888 -69.888	. 229 . 229	21.000 21.000	00 00
3	-3. <b>008</b> -3. <b>008</b>	13.497	-69.000 -69.000	.229	21.000	00
3	-3.088	13.497	-69.000	. 239	21.000	00
3	-3.000	13.497	-69.000	. 230	21.000	00

TABLE A-VI (CONT)

The second second

RAY	BETA	THETA(RAY)	HORMAL	\$	ALPHA2	RHQ 2
	2 222	40.407	co 000	222	24 202	200
3 3	-3.088 -3.088	13.497 13.497	-69.000 -69.000	. 230 . 230	21.090 21.000	000 000
3	-3.008	13.497	-69.000	. 230	21.000	000
3	-3.088	13.497	-69.000	. 230	21.000	000
3	-3.008	13.497	-69.808	. 238	21.000	000
ž	-3.008	13.497	-69.000	. 239	21.000	~.000
3	-3.088	13,497	-69.000	.230	21.000	000
3	-3.088	13.497	-69.000	. 230	21.000	~.000
3	-3.088	13.497	-69.000	. 230	21.000	~.000
3	-3.688	13.497	-69.000	. 230	21.000	~.000
3	-3.088	13.497	-69.000	. 230	21.000	~.000
3	-3.088	13,497	-69.000	. 238	21.000	~.000
3	-3.088	13.497	-69.000	. 230	21.000	000
3	-3.088	13.497	-69.000	. 238	21.000	~.000
4	-3.845	13.065	-68.568	0.000	21.432	-3.845
4	-3.845	13.088	-68.591	.014	21.409	-3.662
4	-3.845	13.110	-68.613	. 028	21.387	-3.478
4	-3.845	13.133	-68.636	. 842	21.364	-3.293
4	-3.845	13.155	-68.658	. 056	21.342	-3.107
4	-3.845	13.177	-68.680	. 069	21.328	-2.920
4	-3.845	13.199	-68.702	. 083	21.298	-2.732
4	-3.845	13.221	-68.724	. 897	21.276	-2.543
4	-3.845	13.243	-68.746	.111	21.254	-2.353
4	-3.845	13.265	-68.768	. 125	21.232	-2.162
4	-3.845	13.286	-68.789	. 139	21.211	-1.970
4	-3.845	13.308	-68.811	. 153	21.189	-1.778
4	-3.845	13.329	-68.832	. 167	21.168	-1.584
4	-3.845	13.351	-68.854	. 189	21.146	-1.389
4	-3.845	13.372	-69.875	. 194	21.125	-1.194
4	-3.845 -3.645	13.393 13.414	-68.89 <b>6</b> -68.917	. 208 . 222	21.194 21.083	997
7	-3.845 -3.845	13.435	-68,938	. 236	21.062	800 601
4	-3.845	13.456	-68.959	. 25 <b>0</b>	21.041	402
4	-3.845	13.476	-68.979	. 264	21.021	201
4	-3.845	13.476	-68,979	.264	21.021	-, 201
4	-3.845	13.479	-68, 982	. 265	21.018	181
4	-3.845	13,481	-68.984	. 267	21.016	161
4	-3.845	13.483	-68,986	.268	21.014	141
4	-3.845	13.485	-68,988	. 269	21.012	121
4	-3.845	13.487	-68.990	. 271	21.010	101
4	-3.845	13,489	-68.992	.272	21.000	081
4	-3.845	13.491	-68.994	. 273	21.006	061
4	-3.845	13.493	-68.996	. 275	21.004	949
4	-3.845	13.495	-68,998	. 276	21.002	029
4	-3.845	13.495	-68.998	. 276	21.002	020

TABLE A-VI (CONT)

The state of the s

C

O

AY	DETA	THETA(RAY)	HORMAL	\$	ALPHA2	RHO
			co 000	276	04 000	
4	-3.845	13.495	-68.998 -68.998	.276 .277	21.002 21.002	01 01
•	-3.845 -3.845	13.495 13.496	-68.999	377	21.881	01
4	-3.845	13.496	-68.999	, 277	21.881	01
4	-3.845	13.496	-68.999	.277	21.001	01
4	-3.845	13.496	-68.999	.277	21.001	80
4	-3.845	13.496	-68.999	.277	21.001	00
4	-3.845	13.497	-69.000	.277	21.000	00
4	-3.845	13.497	-69.000	. 277	21.000	00
4	-3.845	13.497	-69.000	.277	21.000	00
4	-3.845	13.497	-69.000	.277	21.000	00
4	-3.845	13.497	-69.000	. 278	21.000	00
4	-3.845	13.497	-69.000	. 278	21.000	00
4	-3.845	13.497	-69.000	. 279	21.000	00
4	-3.845	13.497	-69.000	. 279	21.000	00
4	-3.845	13.497	-69.000	.278	21.000	00
4	-3.845	13.497	-69.000	. 278	21.000	00
4	-3.845	13.497	-69.000	.278	21.000	00
4	-3.845	13.497	-69.000	. 278	21.000	00
4	-3.845	13.497	-69.000	.278	21.000	00
4	-3.845	13.497	-69.000	. 278 . 278	21.000	00
4	-3.845 -3.845	13.497 13.497	-69.000 -69.000	.278	21.000 21.000	00 00
4	-3.845	13.497	-69.800	.278	21.000	00
4	-3.845	13.497	-69.800	.278	21.000	00
4	-3.845	13.497	-69.000	.278	21.000	00
4	-3.845	13.497	-69.000	.278	21.888	00
4	-3.845	13.497	-69.000	.278	21.900	80
4	-3.845	13.497	-69.000	. 278	21.888	00
5	-4.649	12.965	-68.468	0.000	21.532	-4.64
5	-4.649	12.993	-68.496	.016	21.504	-4.43
5 5	-4.649 -4.649	13.020 13.040	-68.523 -68.551	. 033	21.477 21.449	-4.20 -3.98
3 5	-4.649	13.075	-68.578	. 849 . 865	21.422	-3.76
5 5	-4.649	13.103	-68.606	. 081	21.394	-3.53
5	-4.649	13.130	-68.633	. 898	21.367	-3.33
5	-4.649	13.157	-68.668	.114	21.340	-3.08
5	-4.649	13.184	-68.687	.138	21.313	-2.85
5	-4.649	13.211	-68.714	.147	21.286	-2.62
Š	-4.649	13.238	-68.741	. 163	21.259	-2.39
5	-4.649	13.265	-68.768	.179	21.232	-2.16
5	-4.649	13.291	-68.794	. 195	21.206	-1.92
5	-4.649	13.317	-68.820	.212	21.186	-1.69
5	-4.649	13.344	-68.847	. 228	21.153	-1.45
5	-4.649	13.370	-68.873	. 244	21.127	-1.21

TABLE A-VI (CONT)

RY	BETA	THETR(RAY)	HORMAL	\$	ALPHA2	RHQ 2
5	~4,649	13.395	-68.898	. 261	21.192	975
5	-4.649	13.421	-68.924	.277	21.076	734
Š	-4.649	13.447	-68.950	. 293	21.050	~.491
5	~4.649	13.472	-68.975	.309	21.625	246
5	-4.649	13.472	-68.975	. 309	21.025	246
5	-4.649	13.474	-68.977	.311	21.023	221
5	-4.649	13.477	-68.989	.313	21.020	197
5	-4.649	13.479	-68.982	.314	21.018	172
5	-4.649	13.482	-68.995	.316	21.015	-,148
5	-4.649	13.484	-68.987	.318	21.013	123
5	-4.649	13.487	-68.990	.319	21.010	099
5	-4.649	13.490	-68.992	.321	21.008	074
5	-4.649	13.492	-68.995	. 322	21.005	049
5	-4.549	13.495	-68.997	. 324	21.003	025
5	-4.649	13.492	-68.995	. 322	21.005	049
5	-4.649	13.492	-68.995	. 323	21.005	047
5	-4.649	13.493	-68.995	. 323	21.005	044
5	-4.649 -4.649	13.493 13.493	-68.996 -68.996	. 323	21.004 21.004	-, 842 -, 839
5	-4.649	13.493	~68.996	. 3 <b>23</b> . 323	21.004	037
5	-4.649	13.494	-68.996	, 323	21.884	037
5	-4.649	13.494	~68.997	, 324	21.003	032
5	-4.649	13.494	~68.997	.324	21.003	038
5	-4.649	13.494	~68.997	.324	21.883	-,027
5	-4.649	13.495	-68,997	.324	21.003	025
5	-4.649	13.495	-68.998	.324	21.002	022
5	-4.649	13.495	-68.998	.324	21.002	020
5	-4.649	13,495	-68.998	.325	21.002	617
5	-4,649	13.496	-68.998	. 325	21.062	015
5	-4.649	13.496	-68.999	. 325	21.001	012
5	-4.649	13.496	-68.999	. 325	21.001	018
5	-4,649	13.496	-68.999	. 325	21.001	067
5	-4.649	13.497	-68.999	. 325	21.001	~.005
5	-4,649	13.497	-69.688	. 326	21.000	~.902
5	-4.649	13.497	-69.000	. 326	21.000	~.002
5	-4,649	13.497	-69.000	. 326	21.000	~. 892
5	-4.649	13.497	-69.800	. 326	21.000	. ~. 992
5	-4.649	13.497	-69.000	. 326	21.000	~. 962
5	-4,649	13,497	-69.800	.326	21.000	~. 901
5 5	-4,649	13.497	-69. <b>490</b>	. 326	21.000	~.001
5	-4,649	13.497	-69.860	.326	21.060	~. 001
5	-4.649	13.497	-69.000 -69.000	.326	21.000	001 001
5	-4.649 -4.649	13.497 13.497	-67. <b>888</b> -67. <b>888</b>	. 326	21.000 21.000	900 900
5	-4.649	13.497	-67. <b>886</b>	. 32 <b>6</b> . 32 <b>6</b>	21.000	000
5	-4.649	13.497	-69.000	.326	21.900	0 <b>00</b>

TABLE A-VI (CONT)

RAY	BETA	THETR(RAY)	HORMAL	s	ALPHA2	RHO 2
5	-4.649	13.497	-69.000	. 326	21.000	000
5	-4.649	13.497	-69.000	. 326	21.000	000
5	-4.649	13.497	-69. <b>008</b>	. 326	21.000	000
5	-4.649	13.497	-69.000	. 326	21.000	000
5	-4.649	13.497	-69.868	.326	21.000	000
5	-4.649	13.497	-69.000	. 326	21.000	000
5	-4.649	13.497	-69.000	. 326	21.000	000
5	-4.649	13.497	-69.008	. 326	21.000	000
5	-4.649	13.497	-69.000	. 326	21.000	000
5	-4,649	13.497	-69.000	. 326	21.000 21.000	000 000
5 5	-4.649 -4.649	13.497 13.497	-69.000 -69.000	. 326 . 326	21.000	000
5	-4.649	13.497	-69.000	. 326	21.000	000
5	-4.649	13,497	-69.000	. 326	21.000	000
5	-4,649	13.497	-69.000	. 326	21.060	000
5	-4.649	13.497	-69.000	.326	21.800	000
5	-4,649	13.497	-69.000	. 326	21.000	000
5	-4.649	13.497	-69.000	. 326	21.000	000
6	-5.502	12.854	-68.357	9.000	21.643	-5.502
6	-5.502	12.988	-68.390	.019	21.610	-5.246
6	-5.502	12.921	-68.424	. 037	21.576	-4.987
6	-5.502	12.955	-68.458	. 056	21.542	-4.727
6	-5.502	12.988	-68.491	. 075	21.509	-4.465
6	-5.502	13.021	-68.524	. 893	21.476 21.443	-4.201 -3.935
6	-5.502 -5.502	13.054 13.087	-68.557 -68.59 <b>0</b>	.112	21.419	-3.667
6	-5.502 -5.502	13.120	-68. <b>62</b> 3	.149	21.377	-3.397
6	-5.502	13.153	-68.656	. 168	21.344	-3.125
6	-5.502	13.185	-68.688	. 187	21.312	-2.851
6	-5.502	13.217	-68.728	. 296	21,280	-2.576
6	-5.502	13.249	-68.752	.224	21.248	-2.298
6	-5.502	13.281	-68.784	.243	21.216	-2.018
6	-5.502	13.313	-68.815	. 262	21.185	-1.736
6	-5.582	13.344	-68.847	. 286	21.153	-1.451
6	-5.502	13.375	-68.878	. 299	21,122	-1.165
6	-5.502	13.496	-68.989	.318	21.091	877
6	-5.502	13.437	-68.939	. 336	21.061	587
6	-5.582	13.467	-68.978	. 355	21.030	294
6	-5.502	13.437	-68.939	. 336	21.061	587
6	-5.502	13.440	-68.943	. 338	21.057	558
6	-5.502	13.443	-68.946	. 340	21,054	529
6	·-5.502	13.446	-68.949	. 342	21.051	499
6	-5.502	13,449	-68.952	. 344	21.048	470
6	-5.502	13.452	-68.955	. 346	21.045	441
6	-5.502	13.455	-68.958	. 348	21.842	412

TABLE A-VI (CONT)

RAY	BETA	THETA(RAY)	HORMAL	\$ 	ALPHA2	RHO 2
6	-5.502	13.458	~68.961	. 349	21.039	382
6	-5.502	13.461	-68.964	.351	21.036	353
6	-5.502	13.464	-68.967	. 353	21.033	324
6	-5.502	13.467	-68.970	. 355	21.030	294
6	-5.592	13.478	-68.973	. 357	21.627	265
6	-5.502	13.473	-68.976	. 359	21.824	236
6	-5.502	13.476	-68.979	. 361	21.021	206
6	-5.502	13.479	-68.982	. 363	21.018	177
6	-5.502	13.482	-68.905	. 364	21.015	147
6	-5.502	13.485	-68.988	. 366	21.012	118 089
6	-5.502 -5.502	13.48 <b>8</b> 13.491	-68.991 -68.994	.368 .37 <b>9</b>	21.609 21.606	059
6	-5.502 -5.502	13.494	-68.997	.372	21.003	036
6	-5.502	13.491	-68.994	.370	21.006	059
6	-5.502	13.491	-68.994	.376	21.006	056
6	-5.502	13.492	-68.995	.370	21.005	053
6	-5.502	13.492	-68.995	.371	21.005	056
6	-5.502	13.492	-68.995	.371	21.005	947
6	-5.502	13.493	-68.995	.371	21.005	844
6	-5.502	13.493	-68.996	.371	21.994	04 1
6	-5.502	13.493	-68.996	.371	21.004	039
6	-5.502	13.493	-68.996	.371	21.004	935
6	-5.502	13.494	-68.997	. 372	21.003	032 038
6	-5.502 -5.502	13.494 13.494	-68.997 -68.997	.372 .372	21.003 21.003	027
6	-5.502	13.495	-68.998	.372	21.002	024
6	-5.502	13,495	-68.998	.372	21.002	021
6	-5.502	13.495	-68,998	.373	21.002	018
6	-5,502	13.496	-68.999	.373	21.001	015
6	-5.502	13.496	-68.999	. 373	21.001	012
6	-5.502	13.496	-68.999	.373	21.001	009
6	-5.502	13.496	-68.999	.373	21.001	006
6	-5.502	13.497	-69.000	. 374	21.000	003
6	-5.502	13.496	-68.999	. 373	21.001	006
6	-5.502	13.496	-68.999	. 373	21.001	006 005
ċ	-5. 502 -5. 502	13.4 <b>96</b> 13.497	-68.999 -68.999	. 373 . 373	21.001 21.001	005
•	-5.502	13.497	-69.888	.373	21.000	885
•	-5.502	13,497	-69.888	.373	21.999	994
•	-5.502	13.497	-69.800	.373	21.000	06
•	-5.502	13.497	-69.000	.373	21.000	004
6	-5.502	13.497	-69.000	. 373	21.000	004
6	-5.502	13,497	-69.000	.374	21.000	003
6	-5.502	13.497	-69.000	.374	21.000	003
6	-5.502	13.497	-69.888	. 374	21.000	003
6	-5.502	13.497	-69.000	. 374	21.000	002

TABLE A-VI (CONT)

AY	BETA	THETA(RAY)	NORMAL	\$	АLРНА2	RHO :
6	-5.502	13.497	-69.000	.374	21.000	00
6	-5.502	13.497	-69.000	.374	21.000	00
6	-5.502	13.497	-69.008	.374	21.889	88
6	-5.502	13,497	-69.900	.374	21.800	00
6	-5.502	13.497	-69.000	.374	21.999	00
6	-5.502	13,497	-69.000	.374	21.000	00
6	-5.502	13.497	-69.900	.374	21.000	00
6	-5.502	13.497	-69.800	.374	21.000	00
6	-5.502	13.497	-69.000	.374	21.000	00
6	-5,502	13.497	-69.000	. 374	21.000	00
6	-5.502	13.497	-69.000	. 374	21.000	00
6	-5.502	13.497	-69.000	. 374	21.000	99
6	-5.502	13.497	-69.000	.374 .374	21. <b>096</b> 21. <b>000</b>	000 000
6	-5.502	13.497	-69. <b>000</b>	.374	21.000	00
6	-5.5 <b>0</b> 2 -5.5 <b>0</b> 2	13.497 13.497	-69. <b>000</b> -69. <b>000</b>	.374	21.000	89
•	-5.5 <b>62</b>	13.497	-69.000	. 374	21.000	88
6	-5.502	13.497	-69.000	.374	21.000	00
6	-5.502	13.497	-67.000	.374	21.800	66
6	-5,502	13.497	-67.000	.374	21.000	00
6	-5.502	13.497	-69.000	.374	21.000	00
6	-5.502	13.497	-69.000	.374	21.000	000
6	-5.502	13.497	-69.000	.374	21.000	000
6	-5.502	13.497	-67.000	. 374	21.000	900
6	-5.502	13.497	-69.000	. 374	21.000	000
6	-5.502	13.497	-69.000	. 374	21.000	000
6	-5.502	13.497	-69.988	.374	21.000	000
6	-5.502	13.497	-69.000	.374	21.000	000
7	-6.409	12.731	-68.234	9.000	21.766 21.726	-6.40 -6.11
7	-6. 489 -6. 489	12.772 12.812	- <b>68.</b> 274 - <b>68.</b> 315	.021 .042	21.685	-5.81
7 7	-6.489	12.852	-68.355	, 963	21.645	-5.51
7	-6.409	12.892	-68.394	. 084	21.606	-5.21
7	-6.409	12.931	-68.434	. 185	21.566	-4.91
7	-6.409	12.971	-68.474	.127	21.526	-4.60
7	-6.409	13.010	-68.513	. 148	21.407	-4.29
7	-6.489	13.049	-68.352	.169	21.448	-3.97
7	-6.409	13.088	-68.591	. 190	21.409	-3.66
7	-6, 489	13.126	-68.629	.211	21.371	-3.34
7	-6.489	13.165	-68.668	. 232	21.332	-3.02
7	-6.489	13.203	-68.786	. 253	21.294	-2.69
7	-6.409	13.241	-68.744	.274	21.256	-2.37
7	-6.489	13.278	-68.781	. 295	21.219	-2.04
7	-6.409	13.316	-68.819	.316	21.101	-1.70
7	-6.489	13.353	-68.856	. 337	21.144	-1.37

TABLE A-VI (CONT)

AY	DETA	THETACRAY	HORMAL	\$ 	ALPHA2	RHO 2
7	-6. 409	13.309	-68.892	. 359	21.100	-1.033
7	-6.409	13.426	-68.928	. 386	21.072	692
7	-6.489	13.461	-68.964	. 401	21.036	347
7	-6.409	13.426	-68.928	. 380	21.072	692
7	-6.489	13.429	-68.932	. 382	21.068	657
7	-6.409	13.433	-68.936	. 384	21.064	623
7	-6.409	13.436	-68.939	. 386	21.861	589
7	-6.409	13.448	-68.943	. 388	21.057	554
7	-6.409	13.444	-68.946	. 396	21.054	520
?	-6.409	13.447	-68.950	. 392	21.050	485
7	-6.409	13.451	-68.954	. 394	21.846	451
7 7	-6.409	13.454	-68.957	. 396	21.043	-,416
7	-6.489 -6.489	13.45 <b>9</b> 13.461	-68.961 -68.964	. 3 <b>99</b> . 401	21.039 21.036	382 347
7	-6.409	13.465	-68.968	. 403	21.032	313
7	-6.409	13.469	-68.972	. 405	21.028	278
7	-6.409	13.472	-68.975	. 487	21.025	243
7	-6.409	13.476	-68.979	. 489	21.621	209
7	-6.409	13.479	-68.982	.411	21.018	174
ż	-6.489	13.483	-68.986	.413	21.014	139
7	-6.489	13.486	-68.989	.415	21.911	194
7	-6.489	13.498	~68.993	.418	21.007	879
7	-6.409	13,493	-68.996	. 420	21.004	035
7	-6.409	13.490	~68.993	.418	21.007	879
7	-6.489	13.490	~68.993	.418	21.007	066
7	-6.489	13.491	-68.994	.418	21.006	063
7	-6.409	13.491	-68.994	.418	21.906	059
7	-6.409	13.491	-68.994	.418	21.806	056
7	-6.489	13.492	-68.995	.419	21.005	052
7	-6.409	13.492	-68.995	.419	21.005	049
7	-6.409	13.492	-68.995	.419	21.865	845
7	-6.489	13.493	~68.996	.419	21.004	042
7 7	-6.409	13.493	-68.996	.419	21.004	030
7	-6.489 -6.489	13.493 13.494	-68.99 <b>6</b> -68.997	.428	21. <b>004</b> 21. <b>003</b>	<b>935</b> <b>93</b> 1
7	-6.489	13.494	-68.997	. 420 . 420	21.003	628
7	-6.489	13.495	-68.998	. 428	21.003	824
7	-6.409	13.495	-68.998	.420	21.002	021
7	-6.409	13.495	-68.998	. 421	21.002	817
7	-6.409	13.496	-68.999	.421	21.001	014
7	-6.409	13.496	-68.999	.421	21.001	010
7	-6.409	13.496	-68,999	. 421	21.001	007
7	-6.489	13,497	-69.000	. 422	21.900	903
7	-6.409	13.496	-68.999	. 421	21.001	-,007
7	-6.409	13.496	-68.999	. 421	21.001	007
7	-6.409	13.496	-68.999	.421	21.001	996

TABLE A-VI (CONT)

AY	BETA	THETA(RAY)	NORMAL	\$	ALPHA2	RHG 2
						•
7	-6.409	13.496	-68.999	.421	21.001	896
7	-6.409	13.496	-68.999	. 421	21.001	006
7	-6.489	13.497	-68.999	. 421	21.001	805
7	-6.409	13.497	-69.000	. 421	21.000	085
7	-6.409	13.497	-69.000	. 421	21.000	005
7	-6.489	13.497	-69.000	. 422	21.800	994
7 7	-6.409	13.497	-69.800	. 422 . 422	21.000	004
7	-6.409 -6.409	13.497 13.497	-69.000 -69.000	.422	21.000 21.000	003 003
7	-6.409	13.497	-69 <b>.000</b>	.422	21.000	003
7	-6.489	13.497	-69.000	. 422	21.000	003
7	-6.489	13.497	-69.800	. 422	21.000	002
7	-6.409	13.497	-69,000	.422	21.000	002
7	-6.489	13.497	-69.000	. 422	21.000	001
7	-6.489	13.497	-69.000	. 422	21.800	00
7	-6.489	13.497	-69.000	. 422	21.000	001
7	-6.489	13.497	-69.000	.422	21.000	000
7	-6.489	13.497	-69 <b>.000</b>	. 422	21.000	006
?	-6.489	13.497	-69.000	. 422	21.000	086
7	-6.409	13.497	-69,000	. 422	21.000	000
7	-6.409	13.497	-69.000	. 422	21.000	000
7 7	-6.409	13.497	-69.000	. 422	21.000	000
7	-6.409 -6.409	13.497 13.497	-69. <b>000</b> -69. <b>00</b> 0	. 422 . 422	21.8 <b>99</b> 21. <b>099</b>	000 000
7	-6.489	13.497	-69.000	. 422	21.080	001
7	-6.409	13.497	-69.000	. 422	21.000	890
7	-6.409	13.497	-69.000	.422	21.000	886
8	-7.375	12.595	-68.098	0.000	21.982	-7.375
•	-7.375	12.643	-68.146	. 623	21.854	-7.041
•	-7.375	12.690	-68.193	. 847	21.897	-6.784
	-7.375	12.730	-68.241	. 070	21.759	-6.363
8	-7.375 -7.375	12.7 <b>85</b> 12. <b>83</b> 1	-68.288 -68.334	. <b>094</b> . 117	21.712 21.6 <b>66</b>	-6.018 -5.676
	-7.375 -7.375	12.878	-68.391	.141	21.619	-5.319
	-7.375	12.924	-68.427	.164	21.573	-4.963
Ĭ	-7.375	12.970	-68,473	. 100	21.527	-4.684
j	-7.375	13.016	-68.519	.211	21.481	-4.241
	-7.375	13.062	-68.565	. 235	21.435	-3.875
•	-7.375	13.107	-68.610	. 258	21.390	-3.505
•	-7.375	13.152	-68,655	. 282	21.345	-3.131
•	-7.375	13.196	-68.699	. 305	21.361	-2.753
•	-7.375	13.241	-68.744	. 329	21.256	-2.371
•	-7.375	13.205	-68.787	. 352	21.213	-1.986
•	-7.375	13.328	-68.831	.376	21.169	-1.597
8	-7.375	13.371	-68.874	. 399	21,126	-1.203

TABLE A-VI (CONT)

AY	DETA	THETA(RAY)	NORMAL	<b>S</b>	ALPHA2	RHO :
8	-7.375	13.413	-68.916	. 423	21.884	80
8	-7.375	13.455	-68.958	. 446	21.042	40
8	-7.375	13.413	-68.916	. 423	21.084	80
8	-7.375	13.418	-68.921	. 425	21.079	76
9	-7.375	13.422	-68.925	. 428	21.075	72
8	-7.375	13.426	-68.929	. 430	21.071	68
9	-7.375	13.430	-68.933	. 432	21.067	-, 64
8	-7.375	13.435	-68.937	. 435	21.063	60
<b>8</b>	-7.375 -7.375	13.439	-68.942	.437	21.656 21.654	56
8 8	-7.375 -7.375	13.443 13.447	-68.946	. 439 . 442	21.054	52 48
8	-7.375 -7.375	13.447	-68.950 -68.954	. 444	21.856	44
8	-7.375	13.455	-68.958	. 446	21.842	48
8	-7.375	13.460	-68.963	. 449	21.037	36
8	-7.375	13.464	-68.967	. 451	21.033	-, 32
8	-7.375	13.468	-68.971	. 453	21.029	-, 28
ě	-7.375	13.472	-68.975	. 456	21.025	24
8	-7.375	13.476	-68.979	. 458	21.021	-, 20:
8	-7.375	13.480	-68.983	.468	21.017	16
3	-7.375	13.485	-68.988	. 463	21.012	-, 12
9	-7.375	13.489	-68.992	. 465	21.000	08
8	-7.375	13.493	-68.996	. 467	21.004	84
8	-7.375	13.489	-68.992	. 465	21.008	08
8	-7.375	13.489	-68.9 <del>9</del> 2	. 465	21.008	87
8	-7.375	13.498	-68.993	. 466	21.007	07
8	-7.375	13.490	-68.993	. 466	21.007	069
0	-7.375	13.498	-68.993	. 466	21.007	06
8 <b>8</b>	-7.375	13.491	-68.994	. 466	21.006	06
8 8	-7.37 <b>5</b> -7.375	13.491	-63.994 -68.995	. 467 . 467	21. <b>986</b> 21. <b>99</b> 5	95°
â	-7.375	13.492 13.492	-68.995	. 467	21.005	84
	-7.375	13.492	-68.995	. 467	21.005	04
Ĭ	-7.375	13.493	-68.996	. 467	21.004	84
ě	-7.375	13.493	-68,996	. 468	21.004	03
8	-7.375	13.494	-68,997	. 468	21.803	03
•	-7.375	13,494	-68.997	. 460	21.003	92
	-7.375	13.495	-68.998	. 468	21.002	82
• ,	-7.375	13.495	-68.998	. 469	21.002	020
•	-7.375	13.495	-68.998	.469	21.002	010
•	-7.375	13.496	-68.999	. 469	21.001	01
•	-7.375	13.496	-68.999	. 469	21.001	001
•	-7.375	13.497	-69.000	. 470	21.000	00
•	-7.375	13.496	-68.999	. 469	21.001	000
•	-7.375	13.496	-68.999	. 469	21.001	881
•	-7.375 -7.375	13.496 13.496	-68.999 -68.999	. 469 . 469	21. <b>00</b> 1 21. <b>00</b> 1	907 807

TABLE A-VI (CONT)

RAY	BETA	THETR <rry></rry>	Norhal ————————————————————————————————————	<b>s</b>	ALPHA2	RHQ 2
•	-7.375	13.496	-68.999	. 469	21.001	007
8	-7.375	13.496	-68.999	. 469	21.001	006
8	-7.375	13.496	-60.999	. 469	21.001	006
8	-7.375	13.497	-68.999	. 470	21.001	605
8	-7.375	13.497	-69.000	. 470	21.000	995
	-7.375	13.497	-69.000	. 470	21.000	984
8 8	-7.375 -7.375	13.497	-69.000 -69.000	.470 .470	21. <b>999</b> 21. <b>999</b>	894
å	-7.375 -7.375	13.497 13.497	-67.000	. 470	21.000 21.000	004 003
8	-7.375 -7.375	13.497	-69.000	.476	21.000	003
8	-7.375 -7.375	13.497	-67.000	.470	21.000	002
ě	-7.375	13.497	-67.000	.478	21.000	862
i	-7.375	13.497	-67.000	.470	21.000	002
ě	-7.375	13.497	-67.000	. 470	21.000	001
i	-7.375	13.497	-69.000	. 478	21.000	001
8	-7.375	13.497	-69.000	.479	21.000	000
9	-7.375	13.497	-69.000	.478	21.000	001
9	-7.375	13.497	-67.000	. 478	21.000	001
8	-7.375	13.497	-69.000	. 478	21.000	001
3	-7.375	13.497	-69.800	. 478	21.000	001
9	-7.375	13.497	-69.000	. 478	21.000	001
8	-7.375	13.497	-69.000	.478	21.900	001
8	-7.375	13.497	-69.000	. 478	21.000	801
8	-7.375	13.497	-69.000	. 478	21.000	001
8	-7.375	13.497	-67.000	. 478	21.000	000
8	-7.375	13.497	-69.000	.476	21.000	000
9	-7.375 -7.375	13.497	-69.000	. 478	21.000	000
	-7.375 -7.375	13.497 13.497	-69.000 -69.000	.479 .476	21. <b>966</b> 21. <b>966</b>	000 000
8	-7.375 -7.375	13.497	-67.000	. 470	21.000	000
ă	-7.375	13.497	-67.000	. 478	21.000	999
ě	-7.375	13.497	-69.000	.478	21.000	000
ě	-7.375	13.497	-69.000	. 470	21.000	000
8	-7.375	13,497	-69.000	. 478	21.000	000
i	-7.375	13,497	-69.000	.470	21.000	-, 900
•	-7.375	13.497	-69.000	.470	21.000	990
•	-8.486	12.445	-67.948	0.000	22.052	-8.486
?	-8.406	12.500	-60.003	. 026	21.997	-8.032
,	-8.406	12.556	-68.059	. 052	21.941	-7.653 -7.653
,	-8, 486 -8, 486	12.611	-68.114	. 979 . 104	21. <b>886</b> 21. <b>83</b> 1	-7.269
,	-8.486	12.6 <b>66</b> 12.72 <b>0</b>	-68.169 -68.223	. 129	21.031	-6.881 -6.488
ģ	-8.486	12.775	-68.278	. 155	21.722	-6.89 <b>0</b>
ý	-8.406	12.829	-68.332	. 181	21.668	-5.688
ý	-8.406	12.883	-68.386	. 207	21.614	-5.289

TABLE A-VI (CONT)

AY	BETA	THETA(RAY)	NORMAL	\$ 	ALPHA2	RHO 2
9	-8.486	12.937	-68.448	. 233	21.560	~4.868
9	-8.406	12.990	-68.493	. 259	21.507	~4.451
9	-8.406	13.043	-68.546	. 295	21.454	-4.029
9	-8.486	13.095	-68.598	. 311	21.402	-3.682
9	-8.406	13.147	-68.650	. 337	21.350	-3.170
9	-8.406	13.199	-68.792	. 363	21.298	-2.732
9	-8.486	13.250	-68.753	. 388	21.247	-2.290
9	-8.406 -8.406	13.3 <b>0</b> 1 13.351	-68.8 <b>64</b> -68.854	.414 .440	21.196 21.146	-1.842 -1.396
9	-8.486	13.400	-68.9 <b>9</b> 3	. 466	21.170	-1.376
9	-8.406	13.449	-68.952	. 492	21.048	469
ģ	-8.486	13.449	-68.952	. 492	21.848	469
ý	-8.406	13,454	-68.957	. 495	21.043	422
ś	-8.486	13.459	-68.962	. 497	21.038	375
9	-8, 406	13.463	-68,966	. 580	21.034	329
ģ	-8.486	13.468	-68.971	.502	21.029	282
9	-8.406	13.473	-68,976	. 505	21.024	235
9	-8.486	13.478	-68.981	. 588	21.019	188
9	-8.486	13.483	-68.986	.516	21.614	141
9	-8.486	13.487	-68.990	.513	21.010	994
9	-8.486	13.492	-68. <del>99</del> 5	.515	21.005	847
9	-8.486	13.492	-68.995	.515	21.005	847
9	-8.486	13.493	-68.9 <b>96</b>	.516	21.004	942
9	-8.486	13.493	-68.996	.516	21.004	036
9	-8.406	13.494	-68.997	.516	21.003	033
9	-8.406	13.494	-68.997	.516	21.003	928
9	-8.406	13.495	-68.998	.517	21.002	024
9	-8.406	13.495	-68.998	.517	21.982	019
,	-8.406	13.496	-68.999	.517	21.061	014
•	-9.496 -8.496	13.496	-68.999 -69.8 <b>0</b> 0	.517	21.001 21.000	009
,	-0.406	13.497 13.497	-69.888	.518 .518	21.000	005 005
,	-8.486	13.497	-69,000	.518	21.888	004
•	-8.406	13.497	-69.800	.518	21.000	884
'n	-8.406	13.497	-69.000	.516	21.000	003
ý	-0.406	13.497	-69.000	.518	21.000	003
•	-8.406	13.497	-69.889	.518	21.000	002
•	-0.406	13.497	-69,000	.518	21.000	002
•	-8.486	13.497	-69.000	.518	21.800	981
•	-0.406	13.497	-69.000	.518	21.000	001
•	-8.486	13.497	-69.000	.518	21.000	000
9	-8.486	13.497	-69.000	.518	21.000	000
9	-8.406	13.497	-69.000	.518	21.000	000
•	-8.486	13.497	-69.000	.518	21.000	096
•	-8.406	13.497	-69.000	.518	21.000	000
•	-8.486	13.497	-69.888	.518	21.000	999

TABLE A-VI (CONT)

AY	BETA	THETR(RAY)	HORMAL	<b>s</b>	ALPHA2	RHO 2
9	-8.486	13.497	-69.888	. 518	21.000	006
9	-8.486	13.497	-69.000	.518	21.000	000
9	-8.486	13.497	-69.000	.518	21.000	006
9	-8.486	13.497	-69 <b>.999</b>	.518	21.000	806
9	-8.486	13.497	-69.000	.518	21.000	000
10	-9.507	12.277	-67.788	0.008	22.220	-9.587
19	-9.507	12.341	-67.844	. 028	22.156	-9.091
18	-9.507	12.405	-67.988	. 657	22.692	-8.676
10	-9.507	12.469	-67.972	. 885	22.628	-8.242
	-9.507	12.533	-68.036 -68.099	.113	21.964 21.981	-7.800 -7.369
16 18	-9.507 -9.507	12.596 12.660	-68.163	. 170	21.837	-6.92
10	-9.507	12.723	-68.226	. 198	21.774	~6.47
	-9.507	12.785	-68.288	. 226	21.712	-6.01
10	-9.567	12.848	-68.351	. 255	21.649	~5.548
ě	-9.507	12.910	-68.412	. 283	21.588	-5.07
	-9.587	12.971	-68.474	.311	21.526	-4.60
LO	-9.507	13.032	-68.535	. 340	21.465	~4.11
l O	-9.507	13.092	-68.595	. 368	21.405	-3.62
1.0	<del>-9.507</del>	13.152	-68.655	. 396	21.345	-3.12
10	-9.507	13.212	-68.715	, 424	21.265	-2.62
10	-9.587	13.270	-68.773	. 453	21.227 21.1 <b>69</b>	-2.113 -1.59
10	~9.507 ~9.507	13.32 <b>6</b> 13.3 <b>9</b> 5	- <b>68.</b> 831 -68.888	. 461 . 509	21.112	-1.87
10 18	~9.5 <b>0</b> 7	13,442	-68.945	.538	21.955	53
18	-9.507	13.385	-68.988	. 589	21.112	-1.07
	-9.507	13.391	-68.894	.512	21.186	-1.01
i	-9.567	13.397	-68.900	,515	21.198	96
i	~9.507	13.402	-68.905	.518	21.095	91
	~9.507	13.408	-68.911	. 521	21.089	95
10	~9.507	13.414	-68.916	. 523	21.984	88
10	-9.587	13.419	-68.922	. 526	21.078	?5
LO	-9.507	13.425	-68.928	. 529	21.072	69
	~9.507	13.430	-68.933	. 532	21.067	640 59
	-9.507 -9.507	13.436 13.442	-68.939 -68.945	. 535 . 538	21.061 21.055	~. 53°
	-9.507	13.447	-68.950	. 548	21.050	48
io	-9.507	13.453	-68.956	.543	21.044	43
	-9.507	13.458	-68.961	. 546	21.039	~.37
io	-9.567	13.464	-68.967	.549	21.633	32
10	-9.567	13.469	-60.972	. 552	21.020	27
10	-9.507	13.475	-68,978	. 355	21.922	21
10	-9.507	13.480	-68.983	.557	21.917	16
10	-9.507	13.486	-68.989	. 560	21.011	18
10	-9.587	13.492	-68.994	. 563	21.006	854

TABLE A-VI (CONT)

AY	BETA	THETA(RAY)	NORMAL	<b>S</b>	ALPHA2	RHO 2
10	-9.507	13.492	-68.994	. 563	21.006	~. 054
18	-9.507	13.492	-68.995	.563	21.905	~. 049
10	-9.507	13.493	-68.996	. 564	21.004	043
10	-9.587	13.493	-68.996	. 564	21.884	~. 038
10	-9.507	13.494	-68.997	. 564	21.003	033
10	-9.507	13.494	-68.997	. 564	21.003	027
10	-9.507	13.495	-68.998	. 565	21.002	022
10	-9.507	13.495	-68.998	. 565	21.002	016
10	-9.507	13.496	-68.999	. 565	21.001	011
	-9.507	13.496	-68,999	. 566	21.001	005
10	-9.507	13.496	-68.999	. 566	21.001	~.005
10	<b>-9.507</b>	13.497	-69.000	. 566	21.000	005
10	-9.507	13.497	-69.888	. 566	21.000	804
10 10	-9.507 -9.507	13.497 13.497	-69.000 -69.000	. 566 . 566	21.000 21.000	~.004 ~.003
10	~9.5 <del>0</del> 7	13.497	-69.000	. 566	21.000	883
10	-9.507	13.497	-69.000	. 566	21.000	002
	-9.507	13.497	-69.800	.566	21.000	002
ě	-9.507	13,497	-69.000	. 566	21.000	801
	-9.507	13.497	-69.000	. 566	21.000	001
. 0	-9.587	13.497	-69.800	. 566	21.989	00
10	-9.507	13.497	-69.000	. 566	21.000	000
10	-9.507	13.497	-69.000	. 566	21.000	008
l 🛛	-9.507	13.497	-69.000	. 566	21.000	006
10	-9.507	13.497	-69.000	. 566	21.000	000
	-9.507	13.497	-69.000	. 566	21.000	~. 886
l O	-9.507	13.497	-69.000	. 566	21.000	000
10	-9.587	13.497	-69.000	. 566	21.000	000
L <b>e</b>	-9.507 -9.507	13.497 13.497	-69.000 -69.800	. 566 . 566	21 <b>.000</b> 21 <b>.000</b>	000 000
11	-10.685	12.096	-67,593	8.600	22.407	-18.685
11 11	-10.685	12.164	-67.667	.031	22.333	-10.227
	-10.685 -10.685	12.237	-67.740	.061	22.269	-9.762
11	-10.685	12.311 12.384	-67.814 -67.887	. <b>092</b> . 123	22.186 22.113	-9.2 <b>9</b> 9 -8.8 <b>0</b> 9
11	-10.605	12.458	-67.961	.153	22.839	8.329
i	-10,685	12.531	-68.034	. 184	21.966	-7.825
11	-10.685	12.603	-68.196	.215	21.894	-7.321
1	-10.685	12.676	-68,179	. 246	21.821	-6.809
i	-10.685	12.748	-68.251	.276	21.749	-6.289
i	-10.685	12.819	-68.322	.307	21.678	-5.769
11	-10.685	12.890	-68.393	. 330	21.607	-5.224
1 1	-10.685	12.961	-69.464	. 368	21.536	-4.679
1 2	-10.685	13.031	-68.534	. 399	21.466	-4.125
11	-10.685	13.100	-60.603	. 430	21.397	-3.562

TABLE A-VI (CONT)

C

RRY	BETA	THETA(RAY)	NORMAL	ş	ALPHA2	RHO 2
11	-10.685	13.169 -	<b>~68.6</b> 71	. 469	21.329	-2.991
11	-10,685	13.236	-68.739	. 491	21.261	-2.411
11	-18.685	13.303	-69.806	. 522	21.194	-1.822
11	-18.685	13.369	-68.872	. 553	21.128	-1.224
11	-10.685	13.433	-68.936	. 583	21.064	616
11	-10.685	13.369	-68.872	. 553	21.128	-1.224
11	-18.685	13.375	-69.978	. 556	21.122	-1.163
11	-10.685	13.382	-68.895	. 559	21.115	-1.103
11	-10.685	13.388	-68.891	. 562	21.189	-1.042
11	-10.685	13.395	-68.898	. 565	21.102	982
11	-10.605	13.401	-68.904	. 568	21.096	921
11	~10.685	13.408	-68.911	.571	21.089	860
11	-18.685	13.414	-68.917	. 574	21.083	800
11	-19.685	13.421	-68.924	. 577	21.076	739
11	-19.685	13.427	-69.939	. 588	21.070	678
11	-10.685	13.433	-68.936	. 583	21.064	616
11	-10.685 -10.685	13.440 13.446	-68.943 -68.949	. 586 . 589	21.057 21.051	555 494
11	-10.685	13.453	-68.956	.592	21.051	432
11	-10.685	13.459	-68.962	. 596	21.038	371
ii	-10.685	13.465	-68.968	. 599	21.032	309
ii	-10.685	13.472	-68.975	.692	21.025	248
ii	-10.685	13,478	-68.981	. 685	21.619	186
ii	-10,685	13.484	-68.987	.608	21.013	124
11	-10.685	13.491	-68.994	.611	21.006	062
11	-10.685	13.484	-68.987	. 688	21,013	124
11	-19,685	13.485	-68.989	. 608	21.012	118
11	-18.685	13.486	-68.989	. 688	21.011	112
11	-19.685	13,486	-68.989	. 689	21.011	195
11	-10.685	13.487	-68.990	. 689	21.616	899
11	-10.685	13.488	-68.991	. 609	21.009	693
11	-10.685	13.488	-68.991	.610	21.909	087
11	-10.685	13.489	-68.992	.619	21.886	081
11	-10.685	13.489	-68.992	.618	21.006	074
11	-10.685	13,490	-68.993	.611	21.807	068
11	-10.685	13,491	-68.994	.611	21.906	962
11	-10.685	13,491	-68.994	.611	21.996	056
11 11	-10.685 -10.685	13,492 13,493	-68.995 -68.996	.612	21.985	050
11	-10.685	13.493	-68.996	.612 .612	21. <b>00</b> 4 21. <b>00</b> 4	043 037
11	-10.685	13,494	-68.997	.612	21.003	<b>93</b> 7
11	-10.685	13.495	-68.997	.613	21.003	931 925
11	-10.685	13,495	-60.998	.613	21.003	019
ii	-10.685	13.496	-68.999	.613	21.001	012
ii	-10.685	13, 496	-68.999	.614	21.961	996
11	-10.685	13.496	-68.999	.613	21.001	-,612

TABLE A-VI (CONT)

C

AY	BETA	THETR(RAY)	HORMAL	\$	ALPHA2	RHO 2
11	-10.685	13.496	-68.999	. 613	21.001	012
11	-10.685	13.496	-68.999	.613	21.001	011
11	-10.685	13.496	-68.999	.613	21.001	011
1	-10.685	13.496	-68.999	.613	21.001	016
1	-18.685	13.496	-68.999	.614	21.001	009
1	-10.685	13.496	-68.999	.614	21.001	009
1	-10.685	13.496	-68.999	.614	21.001	008
.1	-10.685	13.496	-68.999	.614	21.861	007
1	-10.685	13.496	-68.999	.614	21.001	007
1	-10.685	13.496	-68.999	.614	21.001	006 006
1	-10.685	13.496 13.497	-68.999 -68.999	.614 .614	21.001 21.001	005
1	-10.695 -10.685	13.497	-69.000	.614	21.000	89
1	-10.685	13.497	-69.00 <b>0</b>	.614	21.000	004
i	-10.685	13.497	-69.000	.614	21.000	003
i	-10.685	13.497	-69.000	.614	21.000	00
ī	-10.685	13.497	-69.000	.614	21.000	002
i	-10.685	13.497	-69.000	.614	21.000	00
ī	-10.685	13.497	-69.800	.614	21.000	00
1	-10.685	13.497	-69.000	.614	21.000	00
1	-10.685	13.497	-69.000	.614	21.000	98
1	-18.685	13.497	-69.000	.614	21.000	09
1	-18.685	13.497	-69.000	.614	21.000	80
1	-10.685	13.497	-69.000	.614	21.000	00
1	-10.685	13.497	-69.000	.614	21.888	00
1	-10.685	13.497	-69.000	.614	21.000	00
1	-10.685	13.497	-69.000	.614	21.000	00
1	-10.685	13.497	-69.000	.614	21. <b>000</b> 21.000	00: 00:
1	-10.685	13.497 13.497	-69.000 -69.000	.614 .614	21.000	00
1	-10.685 -10.685	13.497	-69.0 <b>00</b>	.614	21.000	00
i	-10.685	13.497	-69. <b>000</b>	.614	21.000	00
i	-10.685	13.497	-69.000	.614	21.000	000
i	-10.685	13.497	-69.000	.614	21.860	000
1	-18.685	13.497	-69.888	.614	21.800	996
1	-10.685	13.497	-69.000	.614	21.000	000
1	-10.685	13.497	-69.000	.614	21.000	006
1	-10.685	13.497	-69.000	.614	21.000	990
1	-19.685	13.497	-69.000	.614	21.000	900
2	-11.947	11.961	-67.384	9.900	22.616	-11.947
2	-11.947	11.965	-67.468	. 033	22.532	-11.446
2	-11.947	12.049	-67.552	. 866	22.448	-10.937
2	-11.947	12.133	-67.636	. 099	22.364	-10.418
2	-11.947	12.217	-67.720	. 132	22.280	-9.889
2	-11.947	12.301	-67.884	. 166	22.196	-9.351

TABLE A-VI (CONT)

AY	BETA	THETA(RAY)	HORMAL.	\$ 	ALPHA2	RHO 2
		40.005	47 AAA	100	20.442	-8.803
12 12	-11.947 -11.947	12.385 12.469	-67.988 -67.972	. 199 . 232	22.112 22.028	-8.24
12	-11.947	12.552	-68.055	. 265	21.945	-7.677
12	-11.947	12.635	-68.138	. 298	21.862	-7.098
2	-11.947	12.717	-68.228	. 331	21.789	-6.50
2	-11.947	12.799	-68.302	. 364	21.698	-5.908
2	-11.947	12.881	-68.384	.397	21.616	-5.29
2	-11.947	12.961	-68.464	.430	21.536	-4.67
2	-11.947	13.041	-68.544	. 463	21.456	-4.04
2	-11.947	13.120	-68.623	. 497	21.377	-3.39
2	-11.947	13.120	-68.781	.538	21.299	-2.74
2	-11.947	13.275	-68.778	.563	21.222	-2.07
2	-11.947	13.350	-68.853	.596	21.147	-1.39
2	-11.947	13.424	-68.927	.629	21.073	70
2	-11.947	13.497	-69.000	.662	21.088	88
2	-11.947	13.424	-68.927	. 629	21.073	70
2	-11.947	13.432	-68.935	.632	21.065	63
2	-11.947	13.439	-68.942	.636	21.058	56
2	-11.947	13.446	-68.949	. 639	21.051	-, 49
2	-11.947	13.454	-68.957	.642	21.043	42
2	-11.947	13.461	-68.964	. 645	21.036	35
2	-11.947	13.468	-68.971	. 649	21.029	28
2	-11.947	13.475	-68.978	.652	21.022	21
2	-11.947	13.483	-68.986	.655	21.014	14
2	-11.947	13.490	-68.993	. 659	21.007	07
2	-11.947	13.497	-69.000	. 662	21.000	98
Ž	-11.947	13,498	-68.993	. 659	21.007	07
2	-11.947	13.491	-68.994	. 659	21.006	86
2	-11.947	13.491	-68.994	. 659	21.006	85
2	-11.947	13.492	-68.995	. 660	21.005	85
2	-11.947	13.493	-68.996	. 668	21.004	84
2	-11.947	13.493	-68.996	. 660	21.004	03
2	-11.947	13.494	-68.997	.661	21.003	028
2	-11.947	13.495	-68.998	. 661	21.002	92
2	-11.947	13.496	-68.999	. 661	21.001	01
2	-11.947	13.496	~68.999	. 662	21.001	00
2	-11.947	13.497	~69. <b>000</b>	. 662	21.000	000
2	-11.947	13.496	~68.999	. 662	21.001	007
2	-11.947	13.496	-68.999	. 662	21.001	99
2	-11.947	13.496	-68.999	. 662	21.001	99
2	-11.947	13.497	-68.999	. 662	21.001	00
2	-11.947	13.497	-69.000	. 662	21.000	994
2	-11.947	13.497	-69.000	. 662	21.000	00
2	-11.947	13.497	-69.000	. 662	21.000	883
2	-11.947	13.497	-69.000	. 662	21.000	002
2	-11.947	13.497	-69.000	. 662	21. <b>000</b>	001

TABLE A-VI (CONT)

RAY	DETA	THETA(RAY)	NORMAL	\$	ALPHA2	RHO 2
12	-11.947	13.497	-69.000	.662	21.000	00
12	-11.947	13.497	-69.000	. 662	21.000	000
12	-11.947	13.497	-69.000	. 662	21.000	001
12	-11.947	13.497	-69.000	. 662	21.000	001
12	-11.947	13.497	-69.000	. 662	21.900	001
12	-11.947	13.497	-69.000	. 662	21.000	900
12	-11.947	13.497	-69.000	. 662	21.000	000
12	-11.947	13.497	-69. <b>000</b>	. 662	21.000	000
12	-11.947	13.497	-69.000	. 662	21.000	000
12	-11.947	13.497	-69.000	. 662	21.000	000
12	-11.947	13.497	-69.800	. 662	21.000	000
12	-11.947	13.497	-69.000	. 662	21.000	000
12	-11.947	13.497	-69.000	. 662	21.888	000
13	-13.300	11.646	-67.149	0.000	22.851	-13.30
13	-13.300	11.741	-67.244	. 036	22.756	-12.75
13	-13.300	11.937	-67.340	.071	22.668	-12.203
13	-13.300	11.933	-67.436	. 187	22.564	-11.638
13	-13.300	12.029	-67.532	. 142	22.468	-11.96
13	-13.300	12.125	-67.628	. 178	22.372	-18.476
13	-13.300	12.221	-67.724	.213	22.276	-9.86
13	-13.300	12.316	-67.819	. 249	22.181	-9.25
13	-13.300	12.412	-67.915	. 284	22.005	-8.62
13	-13.300	12.507	-68.010	. 320	21.990	-7.98
13	-13.300	12.602	-68.105	. 355	21.895	-7.33
13	-13.300	12.696	-68.199	.391	21.861	-6.663
13	-13.300	12.798	-68.293	. 426	21.707	-5.98
13 13	-13.300	12.882	-68.385	. 462 . 497	21.615 21.523	-5.285 -4.575
13	-13.300 -13.300	12.974 13 <b>.065</b>	-68.477 -68.5 <b>6</b> 8	. 533	21.432	-3.856
13.	-13.3 <b>00</b>	13.154	-68.657	. 568	21.343	-3.116
13	-13.300	13.242	-68.745	. 604	21.255	-2.35
13	-13.300	13.329	-68.832	. 639	21.168	-1.586
13	-13.300	13.414	-68.917	.675	21.003	80
13	-13.300	13.329	-68.832	. 639	21.168	-1.58
13	-13.300	13.338	-68.841	. 643	21.159	-1.506
13	-13.300	13.346	-68.849	. 646	21.151	1.436
13	-13.300	13.355	-68.858	. 650	21.142	-1.35
13	-13.300	13.363	-68.866	. 653	21.134	-1.274
13	-13.308	13.372	-68.875	. 657	21.125	-1.195
13	-13.300	13.388	-68.883	. 660	21.117	-1.117
13	-13.30 <b>0</b>	13.389	-68.892	. 664	21.108	-1.038
13	-13.300	13.397	-68.900	. 667	21.190	959
13	-13.308	13.406	-68.909	. 671	21.091	389
13	-13.300	13.414	-68.917	. 675	21.083	80
13	-13.300	13.422	-68.925	. 678	21.875	721

TABLE A-VI (CONT)

A CANADA CANADA

RAY	<b>DETA</b>	THETA(RAY)	HORMAL	s 	ALPHA2	RHO 2
13	-13.300	13.431	-68.934	. 682	21.966	642
13	-13.300	13.439	-68.942	. 685	21.058	562
13	-13.300	13.447	-68.958	. 689	21.050	-, 482
13	-13.300	13.456	-68.959	. 692	21.041	492
13	-13.306	13.464	-68.967	. 696	21.033	322
13	-13.300	13.472	-68.975	. 699	21.025	242
13	-13.300	13.481	-68.984	.703	21.016	161
13	-13.300	13.489	-68.992	.797	21.908	081
13	-13.300	13.481	-68.984	.703	21.016	161
13	-13.300	13.481	-68.984	. 703	21.016	153
13	-13.300	13.482	-68.985	.784	21.015	145
13 13	-13.300	13.483	-68.986	.784	21.814	137
13	-13.300 -13.300	13.484	-68.987	.784	21.013	129
13	-13.300	13.485	-68.988	. 795	21.012	121
13	-13.306	13.486 13.486	-68.988	.795	21.012	113
3	-13.300	13.487	-68.989	.785	21.011	105
3	-13.300	13.488	-68.990 -68.991	.706 .706	21.010	897
3	-13.300	13.489	-68.992	.787	21.869	889
3	-13.300	13.498	-68.993	.707	21.000	081
3	-13.300	13.498	-68.993	.707	21.007 21.007	873
13	-13.300	13.491	-68.994	.798	21.006	065 057
13	-13.300	13.492	-68.995	.788	21.005	048
13	-13.300	13.493	-68.996	.798	21.004	040
13	-13.300	13.494	-68.997	.709	21.863	032
13	-13.300	13.495	-68.998	.709	21.062	024
13	-13.300	13.495	-60.998	.709	21.002	016
3	-13.300	13.496	-68.999	.710	21.001	888
.3	-13.300	13.495	-68.998	. 789	21.802	016
3	-13.300	13.495	-68.9 <del>9</del> 8	. 709	21.002	015
3	-13.300	13.496	-68.999	.789	21.001	015
3	-13.300	13.496	-68. 999	.709	21.001	014
3	-13.300	13.496	-68.999	.709	21.001	013
3	-13.300	13.496	-68.999	.710	21.061	012
3	-13.300	13.496	-68.999	.710	21.001	011
3	-13.3 <b>00</b> -13.3 <b>00</b>	13.496	-68.999	.719	21.001	011
3	-13.300	13.496 13.496	-68.999	.718	21.001	010
3	-13.300	13.496	-68.999	.710	21.001	009
3	-13.386	13.496	-68.999 -68.999	.710	21.001	008
3	-13.300	13.496	-68.999	.71 <b>0</b> .710	21.601	007
3	-13.366	13.496	-68,999	.710	21. <b>00</b> 1 21. <b>00</b> 1	006
3	-13.300	13.497	-69.999	.710	21.000	006
3	-13.300	13.497	-69.000	.710	21.000	<b>00</b> 5
3	-13.300	13.497	-69.000	.710	21.000	004 003
3	-13.300	13.497	-69.000	.710	21.000	003

TABLE A-VI (CONT)

RAY	<b>JETA</b>	THETR(RAY)	NORMAL	\$ 	ALPHA2	RHO :
13	-13.300	13.497	-69.000	.710	21.000	<b>00</b> :
13	-13.300	13.497	-69.000	.710	21.000	00
13	-13.300	13.497	-69.000	.710	21.990	00
13	-13.300	13.497	-69.000	.710	21.000	00
13	-13.300	13.497	-69.000	.710	21.000	00
13	-13.300	13.497	-69.900	.710	21.000	90
13	-13.300	13.497	-69.000	.718	21.000	88
13	-13.300	13.497	-69.800	.710	21.000	99
13	-13.300	13.497	-69.000	.719	21.000	00
13	-13.300	13.497	-69.000	.710	21.000	00
13	-13.300	13.497	-69.000	.719	21.000	00
13	-13.389	13.497	-69. <b>000</b>	.710 .710	21.000	00 00
13 13	-13.300 -13.300	13.497 13.497	-69.000 -69.800	.710	21. <b>000</b> 21. <b>000</b>	00
13	-13.300	13.497	-69.000	.710	21.000	00
13	-13.300	13.497	-69.880	.710	21.000	00
13	-13.300	13.497	-69.000	.718	21.800	00
13	-13.300	13.497	-69.000	.710	21.000	00
13	-13.300	13.497	-69.008	.710	21.000	00
13	-13.300	13.497	-69.000	.710	21.000	88
13	-13.300	13.497	-69.000	.710	21.000	98
13	-13.300	13.497	-69.000	.719	21.000	00
14	-14.755	11.382	-66.885	8.888	23.115	-14.75
14	-14.755	11.490	-66.993	. 038	23.007	-14.17
14 14	-14.755	11.598	-67.101	.076 .114	22.899 22.791	-13.57
14	-14.755 -14.755	11.7 <b>06</b> 11.815	-67.209 -67.318	.152	22.682	-12.959 -12.33
14	-14.755	11.924	-67.427	. 198	22.573	-11.68
14	-14.755	12.834	-67.537	.227	22.463	-11.03
14	-14.755	12.143	-67.646	.265	22.354	-10.35
14	-14,755	12.252	-67.755	. 303	22,245	-9.66
14	-14.755	12.361	-67.864	. 341	22.136	-8.96
14	-14.755	12.479	-67.973	. 379	22.827	-9.23
14	-14.755	12.578	-68.081	.417	21.919	-7.49
14	-14.755	12.685	-68.18 <del>8</del>	. 455	21.812	-6.74
14	-14.755	12.792	468.295	. 493	21.705	. <b>~5.96</b>
14	-14.755	12.897	-68.400	. 531	21.600	-5.17
14	-14.755	13.002	-68.505	. 569	21.495	-4.35
14	-14.755	13.105	-68.600	. 606	21.392	-3.52
14	-14.755	13.206	-68.709	. 644	21.291	-2.67
14	-14.755	13.305	-68.808	. 602 . 720	21.1 <b>92</b> 21. <b>09</b> 5	-1.80
14 14	-14.755 -14.755	13.402 13.402	-68.905 -68.905	.720	21.075	91: 91:
14	-14.755	13.412	-68.915	.724	21.005	82
14	-14.755	13.421	-68.924	.720	21.876	73

. TABLE A-VI (CONT)

O

AY	BETA	THETA(RAY)	HORMAL	<b>s</b>	ALPHA2	RH0 2
14	-14.755	13.431	-68.934	.732	21.066	-,648
14	-14.755	13.440	-68.943	. 735	21.057	549
14	-14.755	13.450	-68.953	.739	21.847 21.838	-, 458 -, 367
14	-14.755	13.459	-68.962 -68.972	.743 .747	21.030	275
14 14	-14.755 -14.755	13.469 13.478	-68.981	.751	21.619	184
4	-14.755	13.488	-68.991	.754	21.009	092
14	-14.755	13.488	-68.991	.754	21.009	092
14	-14.755	13.489	-68.992	.755	21.008	083
14	-14.755	13.498	-68.993	. 755	21.007	074
14	-14.755	13.490	-68.993	. 755	21.007	064
14	-14.755	13.491	-68.994	. 756	21.906	055
14	-14.755	13.492	-68.995	.756	21. <b>885</b> 21. <b>984</b>	<b>046</b> <b>0</b> 37
14	-14.755 -14.755	13.493 13.494	-68.996 -68.9 <del>9</del> 7	.757 .757	21.003	028
14 14	-14.755 -14.755	13.495	-68.998	.757	21.002	018
14	-14.755	13.496	-68.999	.758	21.001	009
14	-14.755	13.496	-68.999	.758	21.001	909
14	-14.755	13.496	-68.999	.758	21.001	-, 901
14	-14.755	13.496	-68.999	. 758	21.001	007
14	-14.755	13.496	-68.999	. 758	21.001	006
14	-14.755	13.496	-68.999	.758	21. <b>001</b> 21. <b>000</b>	006 005
14	-14.755	13.497	-69.000	.758 .758	21.000	804
14 14	-14.755 -14.755	13.497 13.497	-69.888 -69.888	.758	21.000	003
14	-14.755	13.497	-69.000	.758	21.000	802
14	-14.755	13.497	-69.000	.758	21.000	001
14	-14.755	13.497	-69.000	. 758	21.000	001
14	-14.755	13.497	-69.000	. 758	21.000	-, 001
14	-14.755	13.497	-69.008	. 758	21.800	661
14	-14.755	13.497	-69.888	. 758	21.000	001
14	-14.755	13.497	-69.000	.758	21. <b>000</b> 21. <b>000</b>	901 901
14	-14.755	13.497	-69. <b>000</b> -69. <b>000</b>	.758 .758	21.000	991
14 14	-14.755 -14.755	13.497 13.497	-69.000	.758	21.000	000
14	-14.755	13.497	-69.800	.758	21.000	896
14	-14.755	13.497	-69.000	. 758	21.000	000
15	-16.328	11.005	-66.588 -66.7 <b>8</b> 8	0.000	23.412 23.292	-16.326 -15.694
15	-16.320 -16.320	11.2 <b>05</b> 11.327	-66.830	. 040 . 081	23.170	-15.052
15 15	-16.320	11.449	-66.952	. 121	23.846	-14.393
15	-16.320	11.572	-67.075	. 161	22.925	-13.715
15	-16.320	11.696	-67.199	. 202	22.801	-13.019
15	-16.320	11.820	-67.323	. 242	22.677	-12.305
15	-16.320	11.944	-67.447	. 292	22.553	-11.576

TABLE A-VI (CONT)

The second secon

AY	DETA	THETR <ray></ray>	NORMAL	\$	ALPHA2	RHO 2
15	-16.320	12.069	-67.572	. 322	22.428	-10.816
15	-16.320	12.193	-67.696	. 363	22.304	-18.041
15	-16.320	12.318	-67.821	. 403	22.179	-9.245
15	-16.320	12.442	-67.945	. 443	22.055	-8.427
15	-16.320	12.565	-68.068	. 484	21.932	-7.587
15	-16.320	12.688	-60.191	. 524	21.809	-6.724
5	-16.320	12.809	-68.312	. 564	21.688	-5.838
15	-16.320	12.929	-68.432	. 605	21.568	-4.927
15	-16.320	13.047	-68.550	. 645	21.450	-3.992
5	-16.320	13.164 13.278	-68.667 -68.788	.685 .726	21.333 21.22 <b>0</b>	-3.033 -2.048
15 15	-16.320 -16.320	13.389	-68.892	.766	21.198	-1.037
15	-16.320	13.307	-68.788	.726	21.220	-2.848
15	-16.320	13.289	-68.792	.738	21.208	-1.948
15	-16.320	13.300	-68.883	.734	21.197	-1.848
15	-16.320	13.311	-68.814	.738	21.186	-1.747
5	-16.320	13.322	-68.825	.742	21.175	-1.646
5	-16.320	13.334	-68.836	.746	21.164	-1.546
5	-16.328	13.345	-68.848	.750	21.152	-1.444
5	-16.320	13.356	-68.859	. 754	21.141	-1.343
5	-16.320	13.367	-68.878	. 758	21.130	-1.241
3	-16.328	13.378	-68.881	.762	21.119	-1.139
15	-16.320	13.389	-68.892	.766	21.108	-1.037
5	-16.320	13.4 <b>80</b>	-68.993	.770	21.097	934
5	-16.320	13.411	-68.914	.774	21.886	832
5	-16.320	13.422	-68.925	.778	21.075	729
5	-16.320	13.432	-68.935	. 792	21.065	625
5	-16.320	13.443	-68.946	.786	21.054	522
5	-16.320	13.454	-68.957	. 790	21. <b>04</b> 3 21. <b>0</b> 32	418
5	-16.320 -16.320	13.465 13.47 <b>6</b>	-68.968 -68.97 <del>9</del>	.794 .7 <b>98</b>	21.032	314 2 <b>0</b> 9
5	-16.320	13.486	-68.989	. 802	21.011	105
5	-16.328	13.486	-68.989	. 802	21.011	105
5	-16.320	13.407	-68.990	. 803	21.010	094
3	-16.320	13.489	-68.991	. 883	21.009	084
5	-16.329	13.498	-68.993	. 803	21.007	073
5	-16.320	13.491	-68.994	. 884	21.006	063
5	-16.320	13.492	-68.995	. 884	21.005	052
5	-16.320	13.493	-68.996	. 805	21.004	942
5	-16.320	13.494	-68.997	. 805	21.003	031
5	-16.320	13.495	-68.998	. 805	21.002	921
5	-16.328	13.496	-68.999	. 206	21.001	010
5	-16.328	13.496	-68.999	. 886	21.001	010
5	-16.320	13.496	-68.999	. 806	21.001	009
.5	-16.320	13.496	-68.999	, 906	21.001	998
5	-16.320	13.4 <b>96</b>	-68.999	. 806	21.001	967

TABLE A-VI (CONT)

The state of the s

RAY	BETA	THETA(RAY)	HORMAL	<b>s</b>	ALPHA2	RHG 2
15	-16.320	13.496	-68.999	. 996	21.001	886
15	-16.320	13,497	-68,999	. 806	21.001	605
15	-16.320	13.497	-69.888	. 996	21.000	864
15	-16.328	13.497	-69.000	. 896	21.960	003
15	-16.320	13.497	-69.000	. 806	21.000	902
15	-16.320	13.497	-69.000	. 906	21.890	001
15	-16.320	13.497	-69.000	. 806	21.000	001
15	-16.320	13.497	-69.000	. 806	21.000	001
15	-16.320	13.497	-69.000	. 806	21.000	001
15	-16.320	13.497	-69.000	. 806	21.900	001
15	-16.320	13.497	-69.000	. 806	21.000	001
15	-16.320	13.497	-69.000	. 996	21.000	001
15	-16.320	13.497	-69.008	. 806	21.000	000
15	-16.320	13.497	-67.8 <b>00</b> -69. <b>000</b>	. 806 . 806	21.000 21.000	000 000
15 15	-16.32 <b>9</b> -16.32 <b>9</b>	13.497 13.497	-69.000	. 806	21.000	886
13	-10.320	13.47	-07.000		21.000	000
16	-18.895	10.749	-66, 252	0.898	23.748	-18.005
16	-18.005	10.883	-66.386	. 843	23.614	-17.341
16	-18.005	11.019	-66.522	. 985	23.478	-16.657
16	-18.005	11.156	-66.659	. 128	23.341	-15.952
16	-18.005	11.294	-66.797	. 171	23.203	-15.226
16	-18.005	11.434	-66.937	.214	23.063	-14.477
16	-18.095	11.574	-67.077	. 256	22.923	-13.704
16	-18.005	11.715	-67.218	. 299	22.782	-12.988
16	-18.005	11.857	-67.368	. 342	22.640	-12.087
16	-18.005	11.999	-67.502	. 384	22.498	-11.248
16	-18.005	12.141	-67.644	. 427	22.356	-10.367
16	-18.805	12.283	-67.786	. 470	22.214	-9.467
16	-18.605	12.425	-67.928	.513	22.072	-8.538
16	-18.005	12.566	-68.069	. 555	21.931	-7.586
16	-18.005	12.786	-68.209	. 598	21.791	-6.593
16	-18.005	12.844	-60.347	.641	21.653	-5.575
16	-18.005	12.900	-68.483	. 683	21.517	~4.525
16	-18.005	13.114	-68.617 -68.748	.726 .769	21.3 <b>0</b> 3 21.252	-3.444 -2.329
16 16	-18.995 -18.995	13.245 13.373	-68.876	.811	21.124	-1.182
16	-18.865	13.373	-68.748	.769	21.252	-2.329
16	-18.005	13.258	-60.761	.773	21.239	-2.216
16	-16.005	13.271	-68.774	.777	21.226	-2.103
16	-18.005	13.284	-68.787	.782	21.213	-1.989
16	-18.005	13.297	-68.800	.786	21.200	-1.874
16	-18.005	13.310	-68.813	.790	21.187	-1.760
16	-18.005	13.323	-68.826	.794	21.174	-1.645
16	-18.005	13.335	-60.838	. 799	21.162	-1.530
16	-18.005	13.346	-68.851	. 003	21.149	-1.414

TABLE A-VI (CONT)

The second secon

RAY	BETA	THETA(RAY)	HORMAL	<b>s</b>	ALPHA2	RHO 2
16	-18.005	13.361	-68.864	. 807	21.136	-1.296
16	-18.065	13.373	-68.876	. 811	21.124	-1.182
16	-18.965	13.386	-68.889	. 816	21.111	-1.069
16	-18.005	13.398	-68.901	. 820	21.099	946
16 16	-10.005 -18.005	13.411 13.423	-68.914 -68.926	. 824 . 829	21. <b>096</b> 21. <b>074</b>	831 713
16	-18.005	13.436	-68.939	.833	21.061	595
16	-18.805	13.448	-68.951	.837	21.049	477
16	-18.005	13.460	-68.963	.841	21.037	356
16	-18.005	13.473	-68.976	. 846	21.024	239
16	-18.005	13.485	-68.98 <b>8</b>	. 850	21.012	126
16	-18.805	13.473	-68.976	. 846	21.024	239
16	-18.005	13.474	-68.977	. 846	21.023	227
16	-19.005	13.475	-68.978	. 847	21.022	215
16 16	-18.005 -18.005	13.476 13.478	-68.979 -68.9 <b>80</b>	.847 .847	21.921 21.929	283 193
16	-18.805	13.479	-68.982	.848	21.018	17
16	-18.605	13.480	-68.983	.848	21.017	16
16	-18.005	13.481	-68.984	.849	21.816	15
16	-18.005	13.482	-68.985	. 849	21.015	14
16	-18.005	13.484	-68.987	. 850	21.013	13
16	-18.805	13.485	-68.988	. 850	21.012	120
16	-18.005	13.486	-68.989	. 850	21.011	10
16	-18.005	13.487	-68.990	. 851	21.010	09
16	-18.905	13.489	-68.991 -68.993	. 851 . 852	21.009 21.007	884 872
16 16	-18.005 -18.005	13.49 <b>0</b> 13.491	-68.994	. 852	21.006	06
16	-18.005	13.492	-68.995	. 952	21.885	041
16	-18.865	13.493	-68,996	. 853	21.004	03
16	-18.695	13.495	-68.998	. 853	21.002	82
16	-18.005	13.496	-68.999	. 854	21.001	01
16	-18.005	13.496	-68.999	. 954	21.001	01
16	-18.005	13.496	-68.999	. 854	21.001	01
16	-18.805	13.496	-68.999	. 854	21.901	010
16 16	-18.005	13.496	-68.9 <b>79</b> -68.999	. 854 . 854	21.001 21.001	000 00
16	-18.005 -18.005	13.49 <b>6</b> 13.49 <b>6</b>	-68.999	. 854	21.001	00
16	-18.005	13.497	-69.000	.854	21.000	00
16	-18.005	13.497	-69.000	.854	21.000	004
16	-18.005	13.497	-69.000	. 854	21.000	00
16	-18.005	13.497	-69.000	. 854	21.000	00
16	-18.005	13.497	-69.888	.854	21.000	002
16	-18.005	13.497	-69.000	. 854	21.000	862
16	-18.005	13.497	-69.000	. 854	21.000	80
16	-18.005	13.497	-69.000	. 854	21.000	002

TABLE A-VI (CONT)

The second second second

AY	BETA	THETR(RAY)	HORMAL	3	ALPHA2	RHQ 2
16	-18.805	13.497	-69.000	. 854	21.000	992
16	-18.005	13.497	-69.888	. 854	21.000	882
16	-18.005	13.497	-69.000	. 854	21.000	802
16	18.005	13.497	-69.000	. 854	21.000	001
16	-18.095	13.497	-69.688	. 854	21.000	001
16	-18.005	13.497	-69. <b>888</b>	. 854	21.000	001
16	-18.005	13.497	-69.000	. 854	21.000	001
16	-18.805	13.497	-69.888	. 854	21.900	001
16	-18.095	13.497	-69.888	. 854	21.000	001
16	-18.895	13.497	-69.000	. 854	21.000	001
16	-18.895	13.497	-69.000	. 954	21.000	061
16	-18.005	13.497	-69.666	. 854	21.000	~. 986
16	-18.005	13.497	-69.000	. 854	21.800	~.000
16	-18,665	13.497	-69.000	. 854	21.888	~.000
16	-18.995	13.497	-69.000	. 854	21.000	~. 000
17	-19.823	10.369	-65.872	0.966	24.128	-19.823
17	-19,823	18.517	-66.828	. 845	23.980	-19.124
7	-19.823	19.668	-66,171	. 990	23.829	-18.400
7	-19.823	10.821	-66,323	. 135	23.677	-17.652
7	-19.823	10.975	-66,478	. 186	23.522	-16.878
17	-19.823	11.132	-66,635	. 226	23,365	-16.077
17	-19.823	11.299	-66,793	. 271	23.287	-15.248
17	-19.823	11.450	-66,933	.316	23.847	-14.389
7	-19.823	11.611	-67.114	. 361	22.886	-13.500
17	-19.823	11.773	-67.275	. 496	22.725	-12.578
.7	-19.823	11.935	-67.438	. 451	22.562	-11.624
7	-19.823	12.098	-67.691	. 496	22.399	-10.636
.7	-19.823	12.261	-67.764	.541	22.236	-9.612
7	-19.823	12.423	-67.926	. 586	22.074	-8.552
7	-19.823	12.584	-68.087	. 632	21.913	-7.454
17	-19.823	12.744	-68.247	.677	21.753	-6.316
	-19.823	12.902	-68.405	.722	21.595	-5.138
17 17	~19.823 ~19.823	13. <b>956</b> 13.2 <b>99</b>	-68.559 -68.711	.767	21,441 21,289	-3.918
7	-19. <b>823</b>	13.255	-68.858	.812		-2.656
7	-19.823	13.355	-68.711	.857 .812	21.142 21.2 <b>89</b>	~!.350 ~2.656
7	-19.823	13.223	-68.726	.817	21.274	-2.527
7	-19.823	13.238	-68.741	.921	21.259	-2.398
7	-19.823	13.252	-68.755	. 826	21.245	-2.269
7	-19.823	13.267	-68.779	. 838	21,230	~2,139
7	-19.823	13.282	-68.785	. 835	21.215	-2.009
7	-19.823	13.297	-68.800	. 839	21.200	-1.878
7	-19.823	13.311	-68.814	.844	21.186	-1.747
7	-19.823	13.326	-68.829	. 848	21.171	-1.615
7	-19.023	13.346	-68.843	. 853	21.157	-1.483

TABLE A-VI (CONT)

AY	BETA	THETA(RAY)	HORMAL	<b>S</b>	ALPHA2	RHO 2
17	-19.823	13.355	-68.858	. 857	21.142	-1.356
17	-19.823	13.369	-68.872	. 862	21.128	-1.217
17	-19.823	13.384	-68.887	. 866	21.113	-1.084
17	-19.823	13.398	-68.901	.871	21.099	950
17	-19.823	13.412	-68.915	. 875	21.005	816
17	-19.823	13.427	-68.930	. 889	21.078	681
17 17	-19.823	13.441	-68.944 -68.958	. 8 <b>64</b> . 8 <b>8</b> 9	21. <b>056</b> 21. <b>042</b>	545 416
17	-19.823 -19.823	13.455 13.4 <b>69</b>	-68.972	. 893	21.028	274
7	-19.823	13.483	-68.986	. 898	21.014	13
7	-19.823	13.497	-69.000	. 902	21.600	000
18	-21.784	9.938	-65.441	0.000	24.559	-21.78
18	-21.784	10.101	-65.684	. 848	24.396	-21.05
8	-21.784	10.267	-65.778	. 895	24.23 <b>0</b> 24.061	-20.297 -19.509
18	-21.784 -21.784	10.436 10.608	-65.939 -66.111	.143 .198	23.889	-19.50
8	-21.784	10.782	-66.2 <b>8</b> 5	. 238	23.715	-17.84
8	-21.784	10.960	-66.463	. 285	23.537	-16.95
8	-21.784	11.140	-66,643	. 333	23.357	-16.83
8	-21.784	11.322	-66.825	. 388	23.175	-15.07
18	-21.784	11.506	-67.889	. 428	22.991	-14.08
18	-21.784	11.692	-67.195	. 475	22.865	-13.04
8	-21.784	11.878	-67.381	. 523	22.619	-11.96
18	-21.784	12.066	-67.569	. 570	22.431	-10.83
	-21.784	12.253	-67.756	.618	22.244	-9.66
	-21.794	12.439	-67.942	. 665	22.058	-8,44
8	-21.794 -21.794	12.625 12.8 <b>0</b> 7	-68.127 -68.318	.713 .7 <b>68</b>	21.873 21.690	-7.172 -5.849
8	-21.784	12.987	-68.49 <b>0</b>	. 808	21.518	-4.47
8	-21.784	13.163	-68.666	.855	21.334	-3.03
	-21.784	13.333	-60.836	. 983	21.164	-1.549
18	-21.784	13.333	-68.836	. 903	21.164	-1.549
LS	-21.784	13.350	-68.853	. 900	21.147	-1.39
l S	-21.784	13.367	-68.969	.912	21.131	-1.244
l B	-21.794	13.383	-68.886	.917	21.114	-1.890
	-21.704	13.400	-68.903	. 922	21.097	93
	-21.784	13.416	-68.919	. 927	21.001	782
	-21.784 -21.784	13.432 13.449	-68.935 -68.952	. 931 . 936	21. <b>065</b> 21. <b>048</b>	627 471
18	-21.784 -21.784	13.465	-68.752 -68.768	. 941	21.632	31
18	-21.784	13.481	-68.984	. 946	21.016	150
	-21.784	13.461	-68.984	.946	21.016	150
	-21.784	13.483	-60.986	. 946	21.014	14
i	-21.784	13.484	-68.987	.947	21.013	12
i B	-21.784	13.486	-68.707	.947	21.011	110

TABLE A-VI (CONT)

G

AY	BETA	THETR(RAY)	HORMAL	\$ 	ALPHA2	RHO (
10	-21.784	13.487	-68.998	. 947	21.010	- <i>.</i> 095
18	-21.784	13.489	-68.992	. 948	21.000	079
10	-21.784	13.491	-68.994	. 948	21.006	063
18 18	-21.784 -21.784	13.492 13.494	-68.995 -68.997	. 949 . 949	21. <b>005</b> 21. <b>00</b> 3	047
8	-21.784	13.495	-68.99 <b>8</b>	. 95 <b>9</b>	21.803	<b>0</b> 32
š	-21.784	13.495	-68.998	. 958	21.002	01
ě	-21.784	13.496	-68,999	. 950	21.901	01
	-21.784	13.496	-68.999	. 950	21.001	013
•	-21.784	13.496	-68.999	. 950	21.001	011
•	-21.784	13.496	-68.999	. 950	21.001	~. 809
	-21.784	13.496	-68.999	. 950	21.001	~. 000
•	-21.784	13.496	-68.999	. 950	21.861	000
9 9	-21.784 -21.784	13.497	-69.000	. 950	21.800	905
i	-21.784	13.497 13.497	-69. <b>000</b> -69.000	. 95 <b>0</b> . 950	21. <b>000</b> 21. <b>000</b>	003 002
š	-21.784	13.497	-69.000	. 956	21.000	892
i	-21.784	13.497	-69.800	.958	21.000	001
8	-21.784	13,497	-67.000	, 950	21.000	~. 99
8	-21.784	13.497	-69.888	. 950	21.000	00
8	-21.784	13.497	-69.000	. 950	21.000	~.001
•	-21.784	13.497	-69 <b>.000</b>	. 950	21.000	~.001
	-21.784	13.497	-69.000	. 950	21.000	001
8	-21.784	13.497	-69.000	. 950	21.000	~. 000
•	-21.784 -21.784	13.497 13.497	-69.800 -69.808	. 95 <b>0</b> . 95 <b>0</b>	21. <b>000</b> 21. <b>000</b>	~.000 ~.000
•	-611104	13.77	-07.000	. 750	21.000	000
9	-23,983	9.450	-64.953	0.900	25.047	-23.903
9	-23.903	9.626	-65.129	. 050	24.871	-23.149
9	-23.903	9.807	-65.310	. 100	24.690	-22.362
•	-23.903	9.993	-65.496	. 150	24.584	-21.541
•	-23.903	10.182	-65.685	. 200	24.315	-20.684
<b>,</b>	-23.903	10.376	-65.879	. 250	24.121	-19.788
•	-23.983 -23,983	10.574 10.776	-66.977 -66.279	.300 .349	23.923 23.721	-18.851 -17.872
Ź	-23, 903	10.901	-66.484	. 399	23.516	-16.847
•	-23.903	11.190	-66.693	.449	23.307	-15.773
•	-23.903	11.402	-66.905	. 499	23.095	-14.649
•	-23.903	11.616	-67.118	. 549	22.882	-13.472
•	-23.903	11.831	-67.334	. 599	22.666	-12.239
•	-23,903	12.047	-67.350	. 649	22.450	-10.946
•	-23.903	12.264	-67.767	. 699	22.233	-9.591
•	-23 <b>.90</b> 3	12.480	-67.983	.749	22.017	-8.172
, ,	-23 <b>.903</b> -23 <b>.90</b> 3	12.693 12.9 <b>0</b> 3	-68.196 -68.486	. 799 . 849	21. <b>904</b> 21.5 <b>94</b>	-6.684 -5.126
, ,	-23.903 -23.903	13.100	-68.611	. 899	21.389	-3.126 -3.494

TABLE A-VI (CONT)

RAY	BETA	THETA(RAY)	HORMAL	\$	ALPHA2 	RHG 2
	22 222	40.307	60.010			
19 19	-23.903 -23.903	13.3 <b>0</b> 7 13.497	-68.810 -69.000	. 948 . 998	21.190 21.000	-1.786 000
29	-26.190	8.895	-64.398	0.000	25.602	-26.196
20	-26.190	9.085	-64.588	. 952	25.412	-25.42
20	-26.190	9.288	-64.783	. 105	25.217	-24.615
20	-26.198	9.481	-64.984	. 157	25.016	-23.769
28	-26.190	9.688	-65.191	. 209	24.809	-22.986
20	-26.198	9.902	-65.405	. 262	24.595	-21.946
20	-26.190	10.121	-65.624	.314	24.376	-20.964
20	-26.190	10.346	-65.849	. 366	24.151	-19.931
20	-26.190	10.576	-66.079	.419	23.921	-18.842
20	-26.190	10.912	-66.315	.471	23.685	-17.695
20	-26.198	11.052	-66.555	. 523	23.445	-16.486
20	-26.198	11.297	-66.800	. 576	23.200	-15.210
20	-26.198	11.545	-67.048	. 628	22.952	-13.363
20	-26.198	11.796	-67.299	. 6 <b>80</b>	22.701	-12.441
20	-26.190	12.049	-67.552	.732	22.448	-10.946
20	-26.190	12.301	-67.884	. 785	22.196	-9.354
20	-26.198	12.552	-68.055	.837	21.945	-7.679
20	-26.198	12.799	-68.302	. 889	21.698	-5.910
28	-26.198	13.041	-68.544	. 942	21.456	-4.843
20 20	-26.190 -26.190	13.274 13.497	-68.777 -69.000	.994	21.223	-2.075
20	-29.170	13.477	~57.000	1.046	21.000	~. 806
21	-28.661	8.267	-63.778	0.000	26.238	-28.661
21	-28.661	8.467	-63.970	. 855	26.030	-27.888
21	-28.661	8.674	-64.177	. 169	25.823	-27.073
21	-28.661	8.890	-64.393	. 164	25.607	-26.213
21	-28.661	9.113	-64.616	.219	25.384	-25.305
21	-28.661	9.345	-64.848	. 274	25.152	-24.344
21	-28.661	9.585	-65.088	. 328	24.912	-23.326
21	-28.661	9.833	-65.336	. 383	24.664	-22.248
21	-28.661	18.898	-65.593	. 438	24.407	-21.194
21	-28.661	10.355	-65.858	. 493	24.142	-19.889
21	-28.661 -38.661	16.627	-66.13 <b>9</b>	.547	23.870	-18.598
21 21	-28.661 -28.661	1 <b>0.906</b> 11.1 <b>92</b>	-66.4 <del>89</del> -66.695	. 602	23.591	-17.224
21 21	-28.661	11.192	-66.997	. <b>65</b> 7	23.385	-15.762
21	-28.661	11.779	-67.2 <b>8</b> 2	.711 .766	23.013	-14.204
21	-28.661	12.076	-67.579	. 821	22.718	-12.543
21	-28.661	12.373	-67.876	.876	22.421 22.124	-10.771 -8.882
21	-28.661	12.667	-68.176	. 930	21.830	-6.368
21	-20.661	12.956	-68,459	. 985	21.541	-4.721
21	-28.661	13.234	-68.737	1.040	21.263	-2,433
21	-28.661	12.956	-68.459	.985	21.541	-4.721

TABLE A-VI (CONT)

O

RAY	JETA	THETR <ray></ray>	NORMAL	<b>s</b>	ALPHA2	RHO 2
21	-28,661	12.984	-68.487	. 9 <b>98</b>	21.513	-4.496
21	-28.661	13.012	-68.515	. 996	21.485	-4.274
21	-28.661	13.040	-68.543	1.001	21.457	-4.049
21	-28,661	13.868	-68.571	1.007	21.429	-3.823
21	-28.661	13.096	-68.599	1.012	21.401	-3.595
21	-28.661	13.124	-68,627	1.818	21.373	-3.365
21	-28.661	13.151	-68.654	1.023	21.346	-3, 134
21	-28,661	13.179	-68.682	1.829	21.318	-2.902
21	-28.661	13.206	-68.709	1.034	21.291	-2.668
21	-28.661	13.234	-68,737	1.040	21.263	-2.433
21	-28.661	13.261	-68,764	1.845	21.236	-2.197
21	-28.661	13.288	-68.791	1.051	21.209	-1.955
21	-28.661	13.314	-68,817	1.056	21.183	-1.719
21	-28.661	13.341	-68.844	1.862	21.156	-1.478
21	-28.661	13.367	-68.879	1.067	21.130	-1.235
21	-28.661	13.394	-68.897	1.073	21.103	991
21	-28.661	13.428	-68,923	1.078	21.677	746
21	-28.661	13.446	-68,949	1.004	21.051	499
21	-28.661	13.471	-68.974	1.669	21.026	256
21	-28.661	13.471	-68.974 -68.977	1.009 1.090	21. <b>026</b> 21. <b>023</b>	256 225
21	-28.661	13.474			21.023	225
21 21	-28.661 -28.661	13.477 13.479	-68.989 -68.982	1. <b>090</b> 1. <b>09</b> 1	21.018	175
21	-28.661	13.482	-68.985	1.091	21.015	150
21	-28.661	13.484	-68.987	1.092	21.013	125
21	-28.661	13.487	-68.990	1.892	21.010	199
21	-28.661	13.489	-68.992	1.893	21.008	075
21	-28.661	13.492	-68.995	1.093	21.005	956
21	-29.661	13.494	-68.997	1.094	21.003	025
21	-28,661	13.497	-69.000	1.894	21.000	000
21	-28.661	13.494	-68.997	1.094	21.003	025
21	-28.661	13.495	-68.998	1.094	21.002	023
21	-28.661	13.495	-68.998	1.094	21.002	926
21	-28.661	13.495	-68.999	1.894	21.002	018
21	-28.661	13.496	-68.998	1.094	21.002	015
21	-28.661	13.496	-68.999	1.894	21.001	913
21	-28.661	13.496	-68.999	1.094	21.001	916
21	-20.661	13.496	-60.999	1.094	21.001	~. 001
21	-20.661	13.497	-68.999	1.094	21.001	965
21	-20.661	13.497	-69.000	1.094	21.000	~. 903
21	-28.661	13.497	-60. 999	1.094	21.001	~. 065
21	-28.661	13.497	-69.000	1.094	21.000	~. 003
21	-29.661	13.497	-69.000	1.894	21.000	005
21	-28.661	13.497	-69.000	1.094	21.000	~. 994
21	-28.661	13.497	-69.000	1.094	21.990	004
21	-28.661	13.497	-69.000	1.074	21.000	~. 004

TABLE A-VI (CONT)

RAY	DETA	THETA(RAY)	NORMAL	\$ 	ALPHA2	RHO 2
21	-20 551	13.497	-69.000	1.094	21.000	004
21	-29.661 -28.661	13.497	-69.000	1.094	21.000	003
21	-28.661	13.497	-69.000	1.094	21.000	003
21	-28.661	13.497	-69.000	1.894	21.000	003
21	-28.661	13.497	-69.000	1.094	21.000	003
21	-28.661	13.497	-69.000	1.894	21.000	002
21	-28.661	13.497	-69.000	1.894	21.000	002
21	-28.661	13.497	-69.000	1.094	21.000	002
21	-28.661	13.497	-69.000	1.094	21.000	002
21	-28.661	13.497	-69.000	1.094	21.000	001
21	-28.661	13.497	-69.000	1.094	21.000	001
21	-28.661	13.497	-69.000	1.094	21.000	001
21	<b>-28.66</b> 1	13.497	-69.000	1.094	21.000	001
21	-28.661	13.497	-69.000	1.094	21.000	000
22	-31.326	7.556	-63.058	0.000	26.942	-31.326
22	-31.326	7.762	-63.265	. 057	26.735	-30.564
22	-31.326	7.979	-63.482	.114	26.518	-29.756
22	-31.326	8.265	-63.708	.171	26.292	-28.898
22	-31.326	8.442	-63.945	. 229	26.055	-27.985
22	-31.326	8.690	-64.193	. 286	25.807	-27.012
22	-31.326	8.949	-64.452	. 343	25.548	-25.974
22	-31.326	9.219	-64.722	. 400	25.278	-24.866
22	-31.326	9.502	-65.005	. 457	24.995	-23.686
22	-31.326	9.796	-65.299	.514	24.701	-22.416
22	-31.326	10.103	-65.606	. 571	24.394	-21.046
22	-31.326	10.420	-65.923	. 628	24.877	-19.582
22	-31.326	18.749	-66.252	. 686	23.748	-18.005
22	-31.326	11.087	-66.590	.743	23.410	-16.300
22	-31.326	11.434	-66.937	. 889	23.063	-14.477 -12.501
22	-31.326	11.786	-67.289	.857 .914	22.711 22.356	-10.367
22	-31.326	12.141	-67.644 -67.999	.971	22.001	-9.06
22 22	-31.326	12.496 12.844	-68.347	1.028	21.653	-5.575
22	-31.326 -31.326	13.180	-68.683	1.085	21.317	-2.891
22	-31.326	12.844	-68.347	1.028	21.653	-5.57
22	-31.326	12.876	-68.381	1.034	21.619	-5.31
22	-31.326	12.913	-68.415	1.849	21.585	-5.05
22	-31.326	12.947	-68.458	1.845	21.550	-4.79
22	-31.326	12.900	-68.483	1.051	21.517	-4.52
22	-31.326	13.014	-68.517	1.057	21.483	-4.258
22	-31.326	13.040	-68.551	1.063	21.449	-3.989
22	-31.326	13.061	-68.584	1.968	21.416	-3.71
22	-31.326	13.114	-68.617	1.074	21.383	-3.44
22	-31.326	13.147	-68.658	1.000	21.359	-3.16
22	-31.326	13.100	-68.683	1.005	21.317	-2.89

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TABLE A-VI (CONT)

AY	BETA	THETA(RAY)	HORMAL	\$ 	ALPHA2	RHO 2
22	-31.326	13.213	-68.716	1.091	21.284	-2.61
22	-31.326	13.215	-68.748	1.097	21.252	-2.33
22	-31.326	13.278	-68.781	1.103	21.219	-2.04
22	-31.326	13.310	-68.913	1.108	21.187	-1.76
22	-31.326	13.342	-68,845	1.114	21.155	-1.47
22	-31.326	13,373	-68.876	1.120	21.124	-1.18
22	-31.326	13.405	-68,988	1.125	21.092	896
2	-31.326	13.436	-68.939	1.131	21.061	59
22	-31.326	13.466	-68.969	1.137	21.031	299
22	-31.326	13.436	-68.939	1.131	21.061	59
22	-31.326	13.439	-68.942	1.132	21.058	566
22	-31.326	13.442	-68.945	1.132	21.055	53
2	-31.326	13.445	-68.948	1.133	21.052	50
2	-31.326	13.448	-68.951	1.133	21.049	47
2	-31.326	13.451	-68.954	1.134	21.046	44
2	-31.326	13.454	-68.957	1.135	21.043	41
2	-31.326	13.457	-68.96 <b>8</b>	1.135	21.040	38
2	-31.326	13.460	-68.963	1.136	21.037	35
2	-31.326	13.463	-68.966	1.136	21.034	32
2	-31.326	13.466	-68.969	1.137	21.031	29
2	-31.326	13.470	-68.973	1.137	21.027	26
2	-31.326	13.473	-68.976	1.138	21.024	23
2	-31.326	13.476	-68.979	1.139	21.021	20
2	-31.326	13.479	-68.982	1.139	21.018	17
2	-31.326	13.482	-68.985	1.140	21.015	15
2	-31.326	13.485	-68.988	1.140	21.012	12: 09:
2	-31.326	13.488	-68.991 -69.004	1.141 1.141	21.009 21.006	86
2	-31.326 -31.326	13.491 13.494	-68.994 -68.997	1.142	21.003	83
2	-31.326		-68.994	1.141	21.005	06
2	-31.326	13.491 13.491	-68.994	1.141	21.006	05
2	-31.326	13.492	-68.995	1.141	21.005	05
2	-31.326	13.492	-68.995	1.142	21.005	05
2	-31.326	13.492	-68,995	1.142	21.005	04
2	-31.326	13.492	-68.995	1.142	21.005	84
2	-31.326	13.493	-68.996	1.142	21.004	04
2	-31.326	13.493	-68,996	1.142	21.004	03
2	-31.326	13.493	-68.996	1.142	21.004	03
2	-31.326	13.494	-68.997	1.142	21.003	03
2	-31.326	13.494	-68.997	1.142	21.003	03
2	-31.326	13.494	-68.997	1.142	21.003	02
2	-31.326	13.495	-68.998	1.142	21.002	82
2	-31.326	13.495	-68.998	1.142	21.002	82
2	-31.326	13.495	-68.998	1.142	21.002	01
2	-31.326	13.496	-68.998	1.142	21.002	01
2	-31.326	13.496	-68,999	1.142	21.061	012

TABLE A-VI (CONT)

AY	BETA	THETA(RAY)	NORMAL	\$ 	ALPHA2	RHO 2
22	-31.326	13.496	-68,999	1.142	21.001	~.009
22	-31.326	13.496	-68.999	1.142	21.001	~. 000
22	-31.326	13.497	-69.000	1.142	21.000	~. 863
22	-31.326	13.496	-68,999	1.142	21.001	~.000
22	-31.326	13.496	-68.999	1.142	21.001	006
22	-31.326	13.496	-68.999	1.142	21.001	805
22	-31.326	13.497	-68.999	1.142	21.001	~. 005
22	-31.326	13.497	-69.000	1.142	21.000	~. 905
22	-31.326	13.497	-69.000	1.142	21.000	204
22	-31.326	13.497	-69.000	1.142	21.000	~. 004
22	-31.326	13.497	-69. <b>080</b>	1.142	21.000	004
22	-31.326	13.497	-69.000	1.142	21.000	004
22	~31.326	13.497	-69.000	1.142	21.000	00
22	-31.326	13.497	-69.000	1.142	21.000	~.003
2	-31.326	13.497	-69.000	1.142	21.000	003
2	-31.326	13.497	-69.000	1.142	21.000	00
2	-31.326	13.497	-69.000	1.142	21.000	00
2	-31.326	13.497	-69.800	1.142	21.000	00
2	-31.326	13.497	-69.000	1.142	21.896	~.001
	-31.326 -31.326	13.497	-69.000	1.142	21.000	~. 80
2 2	-31.326	13.497 13.497	-69.000 -69.000	1.142 1.142	21.000 21.000	00: 00:
2	-31.326	13.497	-69.000	1.142	21.000	00
23	-34.198	6.753	-62.256	0.000	27.744	-34.198
23	-34.198	6.961	-62.464	. 060	27.536	-33.46
:3	-34.198	7.181	-62.684	.119	27.316	-32.683
3	-34.198	7.413	-62.916	. 179	27.084	-31.84
3	-34.198	7.658	-63.161	. 238	26.839	-30.949
3	-34.198	7.917	-63.420	. 298	26,588	-29.98
3	-34.198	8.191	-63.694	.357	26.306	-28.95
3	-34.198	8.400	-63.983	.417	26.017	-27.83
3	-34.198	8.786	-64.289	. 476	25.711	-26.621
3	~34.198 ~34.198	9.109 9.449	-64.612 -64.952	. 536 . 595	25.388 25.048	-25.323
3	-34.198	7. <b>7. 7</b> 9. 8 <b>06</b>	-65.3 <b>09</b>	. 655	25.698 24.691	-23.907 -22.367
3	-34.198	10.181	-65.684	.714	24.316	-20.688
3	-34.198	10.573	-66.876	.774	23.924	-18.85
3	-34.198	19.981	-66.484	. 833	23.516	-16.856
23	-34.196	11.401	-66.904	. 893	23.096	-14.653
3	-34,198	11.831	-67.333	. 952	22.667	-12.242
3	-34.198	12.264	-67.767	1.012	22.233	-9.594
3	-34.198	12.693	-68.196	1.071	21.864	-6.686
3	-34.198	13.108	-68.611	1.131	21.369	-3.495
:3	-34.198	13.497	-69.800	1.191	21.000	000

TABLE A-VI (CONT)

24 24 24 24 24 24 24 24 24 24 24 24 24 2	-37.285 -37.285 -37.285 -37.285 -37.285 -37.285 -37.285 -37.285 -37.285 -37.285	5.852 6.955 6.270 6.509 6.745 7.807 7.287	-61.355 -61.558 -61.77 -62.003 -62.248 -62.510	0.000 .062 .124 .186	28.645 28.442 28.227 27.997	-37.285 -36.603 -35.876
24 24 224 224 224 224 224 224 224 224 2	-37.285 -37.285 -37.285 -37.285 -37.285 -37.285 -37.285 -37.285	6.270 6.500 6.745 7.007 7.207 7.507	-61.773 -62.003 -62.240	. 124	28.227	
24 24 24 22 24 22 24 22 24 22 24 22 24 22 24 22 4	-37.285 -37.285 -37.285 -37.285 -37.285 -37.285 -37.285	6.509 6.745 7.007 7.287 7.587	-62.003 -62.248			-35.876
24 24 24 24 224 224 224 224 224 224 224	-37.285 -37.285 -37.285 -37.285 -37.285 -37.285 -37.285	6.745 7.007 7.287 7.507	-62.248	. 186	27 447	
24 24 24 24 224 224 224 224 224 224 224	-37.285 -37.285 -37.285 -37.285 -37.285 -37.285	7.007 7.287 7.587				-35.086
24 24 24 24 24 24 24 24 24 24 24 24	-37.285 -37.285 -37.285 -37.285 -37.285	7.287 7.587	-62.510	. 248	27.752	-34.227
24 24 24 24 24 24 24 24 24 24	-37.285 -37.285 -37.285 -37.285	7.587		.310	27.490	-33.30
24 24 24 24 24 24 24 24 24 24 24	-37.285 -37.285 -37.285		-62.790	.372	27.210	-32.30
24 24 24 24 24 24 24 24 24 24	-37.285 -37.285		-63.090	. 434	26.910	-31.209
24 24 24 24 24 24 24 24 24 24	-37.285	7.909	-63.412	. 495	26.588	-30.017
24 24 24 24 24 24 24 24		8.254	-63.757	. 557	26.243	-28.710
24 24 24 24 24 24 24	-37.285	8.623 9.019	-64.126 -64.522	.619 .681	25.874 25.478	-27.274 -25.696
14 14 14 14 14	-37.285	9.441	-64.944	.743	25.056	-23.93
4 4 4 4 4	-37.285	9.892	-65.395	. 805	24.695	-21.99
14 14 14 14	-37.285	10.369	-65.872	.867	24.128	-19.82
4	-37.285	10.872	-66.375	.929	23.625	-17.39
4	-37.285	11.397	-66.980	.991	23.100	-14.67
4	-37.285	11.935	-67.438	1.053	22.562	-11.62
	-37.285	12.477	-67.980	1.115	22.020	-8.18
	-37.285	13.005	-68.508	1.177	21.492	-4.32
4	-37.285	12.477	-67.980	1.115	22.020	-8.18
4	-37.285	12.531	-68.034	1.121	21.966	-7.82
4	-37.285	12.584	-68.087	1.127	21.913	-7.45
:4	-37.285	12.638	-68.141	1.133	21.859	-7.07
4	-37.285	12.691	-68.194	1.140	21.806	-6.69
4	-37.285	12.744	-68.247	1.146	21.753	-6.31
4	-37.285	12.797	-68.300	1.152	21.700	-5.92
4	-37.285	12.849	-68.352	1.158	21.648	-5.53
4	-37.285	12.902	-68.405	1.164	21.595	-5.13
4	-37.285 -37.285	12.954	-69.457	1.178	21.543	-4.73
4	-37.285 -37.285	13.005 13.057	-68.508 -68.559	1.177 1.1 <b>93</b>	21.492 21.441	-4.329 -3.910
4	-37.285	13.107	-68.610	1.189	21.390	-3.58
4	-37.285	13.158	-68.661	1.195	21.339	-3.00
4	-37.285	13.208	-68.711	1.201	21.289	-2.65
4	-37.285	13.257	-68.768	1.208	21.248	-2.22
4	-37.285	13.306	-68,809	1.214	21.191	1.79
4	-37.285	13.355	-68.858	1.220	21.142	-1.350
4	-37.285	13.403	-68.706	1.226	21.094	98
4	-37.285	13.450	-68.953	1.232	21.047	45
4	-37.285	13.403	-68.906	1.226	21.894	985
4	-37.285	13.408	-68.911	1.227	21.089	860
4	-37.295	13.412	-68.915	1.227	21.005	81
4	-37.285	13.417	-68.920	1.228	21.000	770
4  4	-37.285 -37.285	13.422 13.427	-68.925 -6 <b>8.9</b> 3 <b>8</b>	1.229 1.229	21.075 21.078	726 681

TABLE A-VI (CONT)

A TRUE BE LEVEL AND

AY	BETA	THETA(RAY)	HORMAL	3	ALPHA2	RHO 2
24	-37.285	13.431	-68.934	1.239	21.066	636
24	-37.285	13.436	-68.939	1.231	21.961	596
24	-37.285	13.441	-68.944	1.231	21.056	545
24	-37.285	13.446	-68.949	1.232	21.051	500
24	-37.285	13,450	-68.953	1.232	21.847	455
24	-37.285	13.455	-68.958	1.233	21.842	416
24	-37.285	13.460	-68.963	1.234	21.037	364
24	-37.285	13.464	-68.967	1.234	21.033	319
24	-37.285	13.469	-68.972	1.235	21.028	274
24	-37.285	13.474	-68.977	1.236	21.023	226
24	-37.285 -37.285	13.478 13.483	-68.981 -68.986	1.236 1.237	21.019 21.014	183 137
24 24	-37.285 -37.285	13.488	-68.991	1.237	21.889	091
24	-37.285 -37.285	13.492	-68.995	1.238	21.005	046
24	-37.285	13.492	-68.995	1.238	21.005	046
4	-37.285	13.493	-68.996	1.238	21.664	04
4	-37,285	13, 493	-68.996	1.238	21.004	03
4	-37.285	13,494	-68,997	1.238	21.993	832
4	-37.285	13.494	-68.997	1.238	21.003	927
4	-37.285	13.495	-68.998	1.238	21.002	823
4	-37.285	13.495	-68.998	1.238	21.002	918
24	-37.285	13.496	-68.999	1.238	21.801	014
24	-37.285	13.496	-68.999	1.238	21.001	009
14	-37.285	13.497	-69. <b>000</b>	1.239	21.000	995
4	-37.285	13.497	-69.000	1.239	21.000	~. 005
24	-37.285	13.497	-69.000	1.239	21.000	004
14	-37.285	13.497	-69.000	1.239	21.000	004
4	-37.285	13.497	-69.800	1.239	21.000	903
4	-37.285	13.497	-69.000	1.239	21.000	803
4	-37.285 -37.285	13.497 13.497	-69.0 <b>00</b> -69.000	1.239 1.239	21. <b>000</b> 21. <b>000</b>	00; 00;
}4 }4	-37.285	13.497	-69.000	1.239	21.606	60
4	-37.285	13.497	-67.000	1.239	21.000	00
4	-37,285	13.497	-69.000	1.239	21.800	000
5	-40.591	4.848	-60.351	0.000	29.649	-40.591
5	-40.591	5.835	-60.538	. 964	29.462	-39.900
:5	-48.591	5.235	-60.738	. 129	29.262	-39.33
:5	-48.591	5.451	-60.954	. 193	29.046	-38.621
5	-40.591	5.685	-61.187	. 257	20.613	-37.846
:5	-48.591	5.937	-61.440	. 322	28.560	-37.000
:5	-48.591	6.211	-61.714	. 386	20.206	-36.872
25	-40.591	6.508	-62.011 -62.025	. 450	27 <b>.989</b>	-35.051
25 25	-40.591 -40.591	6.832 7.1 <b>86</b>	-62.335 -62.689	.515 .579	27. <b>663</b> 27.311	-33.921 -32.666
:5 !5	-40.591 -40.591	7.572	-63.075	. 643	26.925	-31.26

TABLE A-VI (CONT)

RAY	DETA	THETA(RAY)	HORMAL	<b>S</b>	ALPHA2	RHQ 2
25	-48.591	7.995	-63.498	.798	26.502	-29.695
25	~40,591	8.458	-63.961	.772	26.039	-27.923
25	-40.591	8.964	-64.467	. 836	25.533	-25.913
25	-40.591	9.516	-65.019	. 981	24.981	-23.628
25	-40.591	10.115	-65.618	. 963	24.382	-20.988
25	-48.591	18.768	-66.263	1.029	23.737	-17.952
25	-40.591	11.442	-66.943	1.894	23.055	-14.438
25	-40.591	12.147	-67 <b>.650</b>	1.158	22.350	-10.331
25	-40.591	12.847	-68.350	1.222	21.658	-5.554
25	-40.591	13.497	-69 <b>.009</b>	1.297	21.000	000
25	-40.591	12.847	-68.359	1.222	21.650	-5.554
25	-40.591	12.915	-68.418	1.229	21.582	-5.935
25	-40.591	12.983	-68.486	1.235	21.514	-4.508
25	-40.591	13.050	-68.553	1.242	21.447	-3.973
25	-40.591	13.116	-68.619	1.248	21.381	-3.430
25	-40.591 -40.591	13.182 13.247	-68.685 -68.75 <b>a</b>	1.254	21.315	-2.879
25 25	-40.591	13.311	-68.814	1.261 1.267	21.2 <b>50</b> 21.186	-2.320 -1.753
25 25	-48.591	13.374	-68.877	1.274	21.123	~1.177
23 2 <b>3</b>	-40.591	13.436	-68.939	1.298	21.061	593
25 25	-40.591	13.497	-69.000	1.287	21.666	888
25	-48.591	13.436	-68.939	1.280	21.061	5 <del>9</del> 3
25	-40.591	13.442	-68.945	1.281	21.055	534
25	-40.591	13.448	-68.951	1.282	21.849	475
25	-48.591	13.454	-68.957	1.282	21.043	416
25	-48.591	13.468	-68.963	1.283	21.037	357
25	-40.591	13.467	-68.979	1.293	21.039	297
25	-40.591	13.473	-68,976	1.284	21.024	238
25	-40.591	13.479	-68,992	1.285	21.018	179
25	-40.591	13.485	-68.988	1.285	21.012	119
25	-40.591	13.491	-68.994	1.286	21.006	964
25	-40.591	13.491	-68,994	1.286	21.006	969
25	-40.591	13.492	~68.995	1.286	21.005	054
25	-40.591	13.492	-68.995	1.286	21.065	048
25	-40.591	13.493	-68.996	1.286	21.004	042
25	-40.591	13.493	-68.996	1.286	21.004	036
25	-40.591 -40.591	13.494	-68.997	1.286	21.003	030
25		13.495	-68.998	1.286	21.002	824
25 25	-40.591 -40.591	13.495 13.496	-68,998 -68,999	1.286 1.287	21. <b>00</b> 2 21. <b>00</b> 1	018 012
29 2 <b>5</b>	-40.591	13.496	-68.999	1.267	21.001	896
23 25	-40.591	13.497	-69.000	1.287	21.001	000
23 25	-40.591	13.496	-68.999	1.287	21.001	006
25	-40.591	13.496	-68.999	1.287	21.001	003
2 <b>5</b>	-40.591	13.497	-69.000	1.287	21.000	005
25	-46.591	13.497	-69.000	1.287	21.000	884

O

TABLE A-VI (CONT)

AY	BETA	THETR(RAY)	HORMAL	s 	ALPHA2	RHO 2
25	<b>-40.5</b> 91	13.497	-69.000	1.287	21.000	0 <del>0</del> 4
25	-48.591	13.497	-69.000	1.287	21.900	003
25	-48.591	13.497	-69.000	1.287	21.000	002
25	-40.591	13.497	-69.000	1.287	21.000	002
25	-40.591	13.497	-69.888	1.287	21.000	001
25	-40.591	13.497	-69.000	1.287	21.000	001
25	-48.591	13.497	-69.000	1.287	21.000	886
6	-44.118	3.740	-59.243	0.000	30.757	-44.118
16	-44.118	3.899	-59.402	. 067	30.598	-43.626
6	-44.118	4.071	-59.574 -50.763	. 133	30.426	-43.076
6	-44.118	4.259 4.4 <b>6</b> 3	-59.762 -59.966	. 200 . 267	30.238 30.034	-42.482 -41.82
6	-44.118 -44.118	4.688	-60.191	.334	29.889	-41.109
_	-44.118	4.935	-60.438	. 400	29.562	-40.31
•	-44.118	5.200	-60.711	. 467	29.289	-39.42
	-44.118	5.511	-61.014	. 534	28.986	-38.423
ن	4.118	5.848	-61.351	. 601	28.649	-37.298
Š	++.118	6,226	-61.729	, 667	29.271	-36.02
6	-44.118	6.650	-62.153	.734	27.847	-34.559
6	-44.118	7.128	-62.631	. 801	27.369	-32.873
6	-44.118	7.669	-63.172	. 868	26.828	-38.909
6	-44.118	8.293	-63.786	. 934	26.214	-28.606
6	-44.118	8.978	-64.481	1.001	25.519	-25.85
6	-44.118	9.763	-65.266	1.068	24.734	-22.556
6	-44.118	10.638	-66.141	1.134	23.859	-18.544
6	-44.118 -44.118	11.59 <b>0</b> 12.574	-67.092 -68.077	1.201	22 <b>.908</b> 21 <b>.92</b> 3	-13.618 -7.527
6	-44.118	11.590	-67.092	1.268 1.201	21.923 22.908	-13.618
•	-44.118	11.688	-67.191	1.200	22.809	-13.866
6	-44.118	11.786	-67.289	1.215	22.711	-12.501
š	-44.118	11.884	-67.387	1.221	22.613	-11.925
6	-44.118	11.983	-67.486	1.229	22.514	-11.336
6	-44.118	12.082	-67.585	1.235	22.415	-10.735
6	-44.118	12.181	-67.684	1.241	22.316	-10.120
6	-44.118	12.279	-67.782	1.248	22.218	-9.492
6	-44.118	12.378	-67.881	1.255	22.119	-0.851
6	-44.118	12.476	-67.979	1.261	22.021	-8.196
6	-44.118	12.574	-68.877	1.268	21.923	-7.527
6	-44.118	12.671	-68.174	1.275	21.826	-6.043
6	-44.118 -44.118	12.767 12. <b>863</b>	-68.270 -68.366	1.281 1.288	21.730 21.634	-6.145 -5.431
6	-44.118	12.958	-68.461	1.295	21.539	-5.431 -4.7 <b>9</b> 3
6	-44.118	13.951	-68.554	1.301	21.557	-3.959
6	-44.118	13.144	-68.647	1.300	21.353	-3.199
6	-44.116	13.235	-68.738	1.315	21.262	-2.424

TABLE A-VI (CONT)

The state of the s

AY	BETA	THETR(RRY)	NORMAL	<b>s</b>	ALPHA2	RHO 2
26	-44.118	13.324	-68.827	1.321	21.173	-1.632
26	-44.118	13.411	-68.914	1.328	21.086	824
26	-44.118	13.324	-68.827	1.321	21.173	-1.632
26	-44.118	13.333	-60.036	1.322	21.164	-1.552
26	-44.118	13.342	-68.845	1.323	21.155	-1.472
36	-44.118	13.350	-68.853	1.323 1.324	21.147 21.138	-1.392 -1.311
26 26	-44.118 -44.118	13.359 13.368	- <b>68.862</b> - <b>68.8</b> 71	1.325	21.129	-1.238
26	-44.118	13.377	-68.889	1.325	21.120	-1.149
26	-44.118	13.385	-68.888	1.326	21.112	-1.068
26	-44.118	13.394	-68.897	1.327	21.103	987
26	-44.118	13.403	-68.986	1.327	21.094	906
26	-44.118	13.411	-68.914	1.328	21.086	824
26	-44.118	13.420	-68.923	1.329	21.077	743
26	-44.118	13.429	-68.932	1.329	21.068	661
26	-44.118	13.437	-68.940	1.330	21.960	579
36	-44.118	13.446	-68.949	1.331 1.331	21.851 21.843	497 414
26 26	-44.118 -44.118	13.455 13.463	-68.957 -68.966	1.331	21.034	33
26	-44.118	13.472	-68.975	1.333	21.025	249
26	-44.118	13.489	-68.983	1.333	21,017	16
26	-44.118	13.489	-68.992	1.334	21,000	083
26	-44.118	13.488	-68.983	1.333	21.017	166
26	-44.118	13.481	-68.984	1.333	21.816	150
26	-44.118	13.482	-68.985	1.333	21.015	150
26	-44.118	13.483	-68.986	1.334	21.014	141
26	-44.118	13.483	-68.986	1.334	21.014	13
36	-41.118	13.484	-68.987	1.334 1.334	21.013	129 11
36	-44,118	13.485	-68.9 <b>88</b> -68.989	1.334	21.012 21.011	100
26 26	-44.118 -44.118	13 <b>.486</b> 13 <b>.48</b> 7	-68.998	1.334	21.010	100
26	-44.118	13.486	-68.991	1.334	21.009	09
26	-44,118	13.489	-68.992	1.334	21,000	00
26	-44.118	13.489	-68.992	1.334	21.000	07
26	-44,118	13.490	-68.993	1.334	21.007	96
26	-44.118	13.491	-68.994	1.334	21.006	05
36	-44.118	13.492	-68.995	1.334	21.005	05
36	-44.118	13.493	-68.996	1.334	21.004	84
36	-44,118	13.494	-68.997	1.334	21.003	-, 03
36	-44,118	13.495	-68.997 -68.998	1.334	21.003 21.002	02: 01:
2 <b>6</b> 2 <b>6</b>	-44,118 -44,118	13.495 13.496	-68.778 -68.777	1.335	21.881	00
26	-44.118	13.496	-68.777	1.335	21.001	001
26	-44,118	13.496	-68.999	1.335	21.801	00
26	-44,118	13.496	-68.999	1.335	21.001	00
26	-44,118	13.496	-60.777	1.335	21.001	800

TABLE A-VI (CONT)

RRY	BETA	THETA(RAY)	HORMAL	<b>s</b>	ALPHA2	RHO 2
26	-44.118	13.497	-68.999	1.335	21.001	-,005
26	-44.118	13.497	-69.000	1.335	21.990	994
26	-44.118	13.497	-69.000	1.335	21.0 <b>00</b>	063
26	-44.118	13.497	-69.000	1.335	21.000	002
26	-44.118	13.497	-69.800	1.335	21.000	002
26	-44.118	13.497	-69.808	1.335	21.000	001

TABLE A-VII

STATE OF THE PARTY OF THE PARTY

COORDINATE (X,Y) VALUES, S, ALPHA2 AND RHO2 FOR THE FINAL DESIGN OF SURFACE NUMBER 1 IN FIGURE 20

legin LAY	Next RAY	Xsurf (next)	Ysurf (next)	S (next)	filpha2 (next)	RHO 2 (next)
1	1	. 362	. 200	. 133	21.000	~.000
i		. 465	. 949	. 133	21.966	642
ī	3	. 568	. 679	. 133	21.139	-1.324
i	2 3 4	.671	.119	. 133	21.220	-2.850
1	5	.774	. 159	. 133	21.309	-2.824
1	5 6 7	.877	. 199	. 132	21.408	-3.650
1	7	. 986	. 239	. 131	21.518	-4.534
1	8	1.082	. 289	. 130	21.648	-5.488
1	9	1.185	. 321	.129	21.778	-6.496
1	10	1.287	. 361	.127	21.932	-7.589
1	11	1.389	. 403	. 126	22.186	-8.765
1	12	1.491	. 444	.123	22.303	-10.035
1	13	1.593	. 486	. 121	22.526	-11.407
1	14	1.694	. 528	.118	22.779	-12.892
1	15	1.796	.578	.114	23.068	-14.503
1	16	1.896	.613	.110	23.399	-16.251
1	17	1.997	. 657	. 105	23.778	-18.150
1	18	2 <b>.09</b> 7	.701	.109	24.213	-28.215
1	19	2.197	.746	. 094	24.712	-22.460
1	20	2.296	.791	. 086	25.286	-24.899
1	21	2.394	. 838	. 978	25.943	-27.545
1	22	2.492	. 885	. 968	26.693	-30.408
i	23	2.589	. 934	. 057	27.543	-33.492
1	24	2.685	. 984	. 045	28.500	-36.797
1	25	2.788	1.035	. 030	29.563	-40.313
1	26	2.873	1.089	.014	30.725	-44.619

TABLE A-VIII

COORDINATE VALUES (X,Y) FOR THE RAY DIAGRAM IN FIGURE 22

AY	X0	YØ	×ı	YI	x2	Y2	Хc	Yc	×4	¥4
1	0	.110	. 287	.110	. 362	. 888	4.000	0.0	50.00	0 5
ż	ě	. 158	. 398	. 150	. 465	. 049	4.999	0.0	50.00	-1.0
3	ā	. 189	. 493	. 189	. 568	. 879	4.000	0.0	50.00	-1.6
4	ě	. 229	. 596	. 229	. 671	.119	4.000	0.0	50.00	-2.2
5	ě	. 268	. 699	. 268	.774	. 159	4.000	0.0	50.00	-2.
6	ě	. 308	. 802	. 308	.877	. 199	4.000	0.0	50.00	-3.
7	ē	. 348	. 986	. 348	. 980	. 239	4.000	0.0	50.00	-4.
8	8	.387	1.089	. 387	1.082	. 289	4.000	0.0	50.00	-5.
9	ě	. 427	1.112	. 427	1.185	. 321	4.000	0.0	50.00 50.00	-6.
19	ě	.466	1.215	. 466	1.287	. 361	4.000	9.0	50.00	-7.
11	8	. 586	1.318	. 506	1.389	. 403	4.000	0.0	50.00	-8.
12	8	. 546	1.421	. 546	1.491	.444	4.000	0.0	58.88	-9.
13	8	. 585	1.524	. 585	1.593	. 486	4.000	0.0	50.00	-10.
14	æ	. 625	1.628	. 625	1.694	. 528	4.000	0.0 0.8	30.00	-11.
15	e	. 664	1.731	. 664	1.796	.578	4.000		50.00	-13.
16	9	.784	1.834	. 704	1.896	.613	4.699	9.0	50.00	-15.
17	8	.744	1.937	.744	1.997	.657	4.000	0.0	50.00	-16.
18	9	.783	2.848	.783	2.897	.701	4.000	0.0	50.00	-19.
19		. 923	2.143	. 823	2.197	.746	4.000	8.8	50.00	-21.
20	•	. 362	2.247	. 862	2.296	.791	4.000	0.0	50.00	-23.
21	0	. 902	2.350	. 902	2.394	. 838	4.000	e.e e.e	58.00	-27.
22		. 942	2.453	. 942	2.492	. 885	4.000		30.00	-30.
23	8	. 981	2.556	. 981	2.589	. 934	4.000	0.0	50.00	-34.
24	ē	1.021	2.659	1.021	2.685	. 984	4.888	0.0	50.00	-39.
25	ē	1.060	2.762	1.060	2.788	1.035	4.000	0.0	58.88	-44.
26	ě	1.100	2.866	1.100	2.873	1.889	4.800	8.8	36.66	

## CHART PROGRAM LISTING

· •

```
10 PRINT
28 PRINT ".
30 PRINT "+
                                                    CHART
48 PRINT "+
58 PRINT "++
60
      DISP "THIS IS CHART !!!"
       HAIT 2500
80 Main: OPTION BASE 0
98
188
          COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trhoi, Rho2, Trho2
         COM F, Z3, Z4, Norm, Thetai, Tdelta
COM Bates, Plots, Familys, Charts, Hains, Maints, Flags, Y_hards
110
129
130
140
         COM Stuffs, Redraws, Digitizes, Ray_traces
COM INTEGER I, J, Y0_loop, Nray, Nray_chart, Nray_family, Nray_stuff
COM INTEGER Nray_trace, Nray_density, Add_ray, Nc, Ns, Nbeta, Flag
150
160
170
180
          CON INTEGER Line_count, Line_max, M_increment, Hit_total, Pselect, Hpib
         COM INTEGER Family, Surf_no
COM REAL Theta_critical, Tol, N1, N2, N3, Delta_ray, Y0, Ya, Yb, Aperture
190
200
210
         CON Y_bullet,Smax_family,Percent_image
CON XI(251),Y1(251),Xc(251),X2(251),Y2(251),X2max(251),Y2max(251)
228
239
248
          COM Y3(251), Y4(251), Beta(251), S2(251), Xsurfmax(251), Ysurfmax(251)
258
268
          COM Qa(251), Smax(251), Alpha2(251), Rho2(251), Hit(2001)
278
288
                               ! SET CONDITION
       Mains="Y"
       DISP ""
298
300
       PRINTER IS 16
318
       HORMAL
320
       FIXED 2
330
       PRINT PAGE
348
       OVERLAP
350
       Y##"0"
       INPUT "SERIAL OR OVERLAP FOR I/O PROCESSING (DEFAULT=OVERLAP) ? S/O", Y#
368
         IF (YS="S") OR (YS="S") THEN SERIAL
378
       CALL Blalogue
388
398
       DEG
         PRINT PAGE,
488
                           When entering values for Smax in CHART please enter reaso
nable"
410
         PRINT "values. This is required because the horizontal axis for CHART is
 divided"
         PRINT "into 10 intervals. The program takes your entry for Smax"
430
         PRINT "and divides by 10 to determine the tick spacing. The vertical
         PRINT "tick marks are under program control, enter anything you wish."
440
430
         PRINT LIN(2), "PRESS CONT"
468
         PAUSE
478
         PRINT PAGE
486 Gymnastics:
                      Y hardfe"N"
490
                      IMPUT "DO TOU HANT A HARD COPY OF THE COMPUTED DATA? YAN", Y ha
rds
500
                        GOSUS Yhard
518
                        CALL Header
520
                        GOSUS Printer
                        CALL Header_end
540
                     PRINT LIN(2)
                     ains="N" : NEST CONDITION | RESET CONDITION
558
                   Hains="H"
568 Header:
578 Initialize_run: Flag=0
                        Y@ min=Ya+(Talpha-Trhoi)/Talpha
Y@ max=Yb+(Talpha-Trhoi)/Talpha
588
590
                                                 I AVOIDS MIXED MODE ARITHMETIC
600
                        Xnrau=Nrau
                        Xnray=Nray
Dely=(Y0 max-Y0 min)/Xnray
Y0 min=Y0 min-Dely
IF Ya=0 THEN Y0 min=Y0 min+Dely
610
620
638
                        Nray=Nray+Add_ray
```

```
! COUNTER FOR THE (X,Y) ARRAY
450
                       Hs=0
668
                       Mc = 8
670
                       X1(Ns)=8
488
                        Y1(Ns)=0
690
                       Beta(0)=0
700 Y0_1cop:
                 FOR Y0_loop=1 TO Nray
                                                ! COMPUTE THE INTERCEPT OF THE INCIDENT
                                             ! AND THE FIRST SURFACE
710
                                            ! AVOIDS MIXED MODE ARITHMETIC
720
                 Xy0_loop=Y0_loop
730
                                            ! RESET FLAG
                  Flaged
748
                 X=8
750
                  Rho=Rho_initial
760
                  Trho=TAN(Rho)
779
                  Y=Y@_min+Dely#Xy@_lcop
789
                  HS=HS+L
798
                 Y1(Ns)=Y
888 One:
              CALL X1pos(X,Y)
810
           X1(Ns)=X
828 Next_y@_loop: NEXT Y@_loop
                     INPUT "ARE YOU USING THE CRT (C) OR THE 9872A PLOTTER (P) ? C/
830
P",Plot$
                       IF (Plots="C") OR (Plots="c") THEN Chart
                     INPUT "PLEASE ENTER THE SELECT CODE OF THE GRAPHICS DEVICE ODE
850
FAULT = 7 ).",Pselect
                     INPUT "PLEASE ENTER THE HPIB ADDRESS OF THE GRAPHICS DEVICE (D
868
EFAULT = 5 >.", Hpib
               CALL Chart
878 Chart:
             GOSUB Yhard_end
890
             PRINT LIN(2), "PRESS CONT"
900
             PAUSE
910
             PRINT
928
             PRINT PAGE, "
                             If the scale you have chosen did not allow the compute
930
             PRINT "to number all of the curves you may do so manually by "
             PRINT "answering yes (Y) to the next prompt."

PRINT LIN(1), " If your answere is yes, the graphics display of the
948
950
960
             PRINT "plot will come on and a cursor will be in the lower left"
             PRINT "corner. Position the cursor by using the DISPLAY" PRINT "controls. The letter or number will be drawn with it
970
788
990
             PRINT "left side over the center of the cursor. You MUST BE
CAREFUL
             PRINT "because mistakes are difficult, if not impossible to erase" PRINT "(consult the graphics rom manual (page 91) to erase a letter).
1010
             PRINT LIN(2)," When you have completed all of your lettering," PRINT "PRESS CONT."
PRINT LIN(2), "PRESS CONT"
1020
1030
1040
             PAUSE
1060
             PRINT PAGE
1070
             Y$="N"
             INPUT "DO YOU HANT TO NUMBER ANY OF THE CURVES ? Y/N",Y$
1000
               IF (YS="Y") OR (YS="Y") THEN CSIZE 2.5
IF (YS="Y") OR (YS="Y") THEN LETTER
1090
1100
               IF (YS="Y") OR (YS="y") THEN CSIZE 15/4.54
1110
1120
               IF (YS="Y") OR (YS="Y") THEN EXIT GRAPHICS
             Dump_crts="N" IMPUT "DO YOU HANT A HARD COPY OF THE PLOT ? YAN", Dump_crts
1130
1140
               IF (Dump_crts="Y") OR (Dump_crts="y") THEN GOSUS Printer
1150
1160
             Flag=0
                             ! RESET CONDITION
1170
             Y 2 - " M "
1188 INPUT "DO YOU HANT ANOTHER PLOT DRAWN TO A DIFFERENT SCALE ? Y/N", Y$
1198 IF (Y$="Y") OR (Y$="y") THEN Chart
1288 Rerun: PRINTER IS 16
1210
              PRINT PAGE
              Y$="N"
1220
              INPUT "ARE YOU GOING TO MAKE ANY MORE RUNS" YON", YE
1230
                  IF (Ys="N") QR (Ys="n") THEN Family
```

```
1250 Rerun2: Changes="N"
                           INPUT "ARE YOU GOING TO CHANGE ANY PARAMETERS (n2, n3, A1pha, Nray, OR
1260
  RHO-INITIAL)? Y/N", Changes
1270
                               IF (Changes="N") OR (Changes="n") THEN Gymnastics
1280
                           GOSUB Printer
                           INPUT "WHAT IS THE NEW VALUE OF RHO-INITIAL ?", Rho_initial
1290
                           Rho_initial=-1=ABS(Rho_initial)
Trhoi=TAN(Rho_initial)
INPUT "WHAT IS THE NEW VALUE OF ALPHA?",Alpha
1300
1319
1328
1339
                            Talpha=TAN(Alpha)
                           INPUT "WHAT IS THE NEW VALUE OF n2?",N2 INPUT "WHAT IS THE NEW VALUE OF n3?",N3
1340 H2:
1350
1368
                               IF N3>N2 THEN BEEP
                               IF N3>N2 THEN DISP "n3 MUST BE < n2, PLEASE RE-ENTER THE VALUES
1370
                               IF H3>N2 THEN HAIT 2500
1388
1398
                               IF N3>N2 THEN N2
                                IF N3<N2 THEN Theta
                                                                          critical=ASN(N3/N2)
1488
                           INPUT "WHAT IS THE NEW VALUE OF YA (INCHES) ?", YA INPUT "WHAT IS THE NEW VALUE OF YA (INCHES) ?", YA
1410 Ya:
1428
                               IF YA>=YB THEN BEEP
1430
1449
                                IF Ya>=Yb THEN DISP "Ya MUST BE < Yb; PLEASE RE-ENTER THE VALUE
1450
                               IF Ya>=Yb THEN WAIT 2500
1460
                               IF Ya>=Yb THEN Ya
1470
                           Aperture=Yb-Ya
1488 Y_bullet:INPUT "WHAT IS THE NEW VALUE OF Y_bullet < MUST BE > Yb > ?",Y_bu
liet
1498
                               IF Y_bullet(Yb THEN BEEP
                               IF Y bullet (Yb THEN DISP "Y bullet MUST BE > Yb : PLEASE RE-ENT
1500
ER Y_bulles."
1518
                               IF Y_bullet<Yb THEN WAIT 2500
                           IF Y bullet (Yb THEN Y bullet INPUT "HHAT IS THE NEW VALUE OF THE No. OF RAYS ?", New INPUT "HEAT IS THE NEW VALUE OF THE NO. OF RAYS ?", New INPUT "HEAT IS THE NEW VALUE OF THE NO. OF RAYS ?", New INPUT "HEAT IS THE NEW INPUT "HE NEW INPUT "HEAT IS THE NEW INPUT "HE NEW
1529
1538
                            INPUT "WHAT IS THE NEW VALUE OF FOCUS (INCHES) ?",F
1540
                     GOTO Gymnastics
1550
1568
          Family: Family#="N'
                           PRINTER IS 16
1379
1566
                            INPUT "DO YOU WANT TO DRAW A FAMILY OF SURFACES FROM THE DESIGN CHA
                               IF (Family = "N") OR (Family = "n") THEN Finished
1590
                           PRINT PAGE," Xmax is the maximum length along the GLM axis which y
1686 Fam1:
ou"
1610
                           PRINT "want to be displayed."
PRINT " A rule of thoumb is to add one inch to the focal length."
1620
                           PRINT "For example: if the Focal length is 4 inches, key in 5 and" PRINT "PRESS CONT."
1638
1640
1650
                            PRINT LIN(2), "PRESS CONT"
1660
                            PAUSE
1678
                              _hards="N"
1680
                            INPUT "DO YOU WANT A HARD COPY OF THE COMPUTED DATA ? Y/N",Y_hard$
                               IF (Y hards="Y") OR (Y_hards="y") THEN GOSUB Yhard CALL Family
1696
 1700
                           GOSUB Yhard end
Dump_crts="N"
INPUT "DO YOU HANT A HARD COPY OF THE PLOT ? Y/N", Dump_crts
IF (Bump_crts="Y") OR (Dump_crts="Y") THEN GOSUB Printer
 1710
 1720
1730
1740
1750
                            INPUT "DO YOU HANT TO DRAW THE PLOT USING A DIFFERENT SCALE ? Y/N",
1768
 YS
1770
                                IF (Ysa"Y") OR (Ysa"y") THEN Fami
                                                                 ! SET CONDITION
 1700
                            Hainis="Y"
                              _hard#="N"
 1790
1000
                            INPUT "DO YOU WANT A MARD COPY OF QA, Smax, Alpha2 and Rho2 ? Y/N", Y_
hards
1010
                                GOSUB Yhard
1020
                               CALL Header
```

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```
1839
                 FOR I=1 TO Nray
                    IF Line count>Line max THEN CALL Header
PRINT USING 1878; 1, Qa(I), Smax(I), Alpha2(I), Rho2(I)
1840
1858
                    Line_count=Line_count+1
IMAGE 14X,DBD,4(5X,DBD.DDD)
1860
1878
1888
                 NEXT I
1898
                    CALL Header_end
                 GOSUB Yhard end
PRINT LIN(10), "PRESS CONT"
1988
1918
1928
                                         ! RESET CONDITION
                 Main1s="N"
1930
                 PAUSE
1940 Stuff: PRINTER IS 16
1950
                PRINT PAGE, "
                                   Please study the display and choose the surface"
                PRINT "which you want to use to generate a final surface."

PRINT " When you have decided which surface to use, PRESS CONT"

PRINT LIN(1), " Key in the number of the surface you want to use."
1960
1970
1989
                                      Key in the number of the surface you want to use"
1990
                PRINT "in response to the prompt."
                PRINT LIN(1)," The computer will then determine the aperture of " PRINT "the surface and trace 250 rays through the aperture."
2988
2619
                                     When you are ready to proceed PRESS CONT."
2020
                PRINT LIN(1),"
2030
                PAUSE
                                ! IF A NOTE TO OPERATOR IS DESIRED, THEN ENTER SETGU, ! LORG 2, MOVE 2,2 ,CSIZE 2.5 ,LABEL "PRESS CONT WHEN ! READY" ,SETGU CSIZE 15/4.54 AFTER THE SECOND BEEP
2849
                GRAPHICS
                HRIT 2500
2858
2868
                REEP
2070
                WAIT 250
2000
                BEEF
2090
                PAUSE
2100
                EXIT GRAPHICS
2110
                INPUT "WHICH SURFACE (1,2,3,etc.) ?",Family
2120
                Family=INT(Family)
                IF Family<=0 THEN Family=1
IF Family>Nray_family THEN Family=Nray_family
BISP "HORKING ..."
2138
2140
2150
2160 Re_stuff: CALL Stuff
2170
                   GOSUB Yhard_end
                Dump_crts="N" INPUT "DO YOU WANT A HARD COPY OF THE PLOT ? Y/N", Dump_crts
2188
2190
                   IF (Dump_crts="Y") OR (Dump_crts="y") THEN GOSUB Printer
2200
                                   ! RESET CONDITION
2216
                F1ag=8
                Redraus="N"
2220
2230
                INPUT "DO YOU WANT ANOTHER PLOT DRAWN TO A DIFFERENT SCALE ? Y/N", Re
drau$
2240
                   IF (Redraws="Y") OR (Redraws="y") THEN Re_stuff
2250 Stuff_trace: Ys="N"
2260
                     INPUT "DO YOU WANT TO TRACE RAYS THROUGH THE COMPUTED SURFACE ?
Y/N", Y8
                     IF (Y$="N") OR (Y$="n") THEN Rerun3
DISP "MORKIN' ON THE RRY TRACE DATA..."
FOR Y8_loop=1 TO Nray_stuff
Surf_no=3
Rho2=Rho2(Y8_loop)
X=X2(Y8_loop)
Y=Y2(Y8_loop)
2278
2288
2298
2300
2318
2320
2330
2340
                           CALL Binary_search(X,Y)
2350
                        Y3(Y0_100p)=Y
2360
                        X=23
                        Surf_no=4
CRLL Binary_search(X,Y)
2370
2380
                     Y4(Y9 loop)=Y
NEXT Y9 loop
2398
2488
2410
                     Nray_trace=Hray_stuff
2420
                     Ray Traces="Y
2430
2440
                      Y$="N"
                     INPUT "BO YOU HANT A HARB COPY OF THE RAY TRACE BATA ? YVN", Y_ha
2450
rd$
2460
                        GOSUB Yhard
```

```
2470
                    CALL Header
2488 Stuff_trace1:FOR I=1 TO Nray_stuff
2498 IF Line_count>Line_max_THEN_CALL_Header
2500
                    PRINT USING 2510; 1, 0, Y1(1), X1(1), Y1(1), X2(1), Y2(1), Xc(1), 0, Z4,
Y4(1)
2510
                    IMAGE DDD,2X,D,3(2X,DD.DDD,3X,DD.DDD),2X,D.D,3X,DD.DD,3X,4D.2D
2520
                    Line_count=Line_count+1
2538
                  HEXT I
                    CALL Header_end
2548
2550
                  GOSUB Yhard end
PRINT LIN(2), "PRESS CONT"
2568
2579
                  BEEP
2588
                  PAUSE
2598 Re_graph:
                   CALL Graph
             Redraus="N"
2600
             INPUT "DO YOU WANT ANOTHER PLOT DRAWN TO A DIFFERENT SCALE ? Y/N", Re
2619
draw$
                IF (Redraws="Y") OR (Redraws="y") THEN Re_graph
2620
2630 Density: PRINTER IS 16
2640
               PRINT PAGE," The point of maximum ray density is determined by yo
u visually."
2658
                PRINT "by placing the cross-hairs (they will appear automatically)
2660
               PRINT "over the position of maximum ray density."
               PRINT "
                          This is accomplished by using the DISPLAY controls (up
2679
,down,<-,->>."
2688
               PRINT "When you the get cursor in the area of interest, use the \underline{S}
HIFT button"
               PRINT "with the BISPLAY controls (both the shift button and disp
lay control"
2799
                PRINT "should be depressed simultaneously) for fine positioing."
                PRINT LIN(2),"
                                  The position of the vertical hair is critical,"
2710
                PRINT "because its location is used for the position of the
2720
                PRINT "image plane (23) on the GLM axis."
2730
2748
                PRINT LIN(2), "CRUTION: Do not let the image plane intercept any
 rays"
2759
                PRINT "in the interior of the lens. If this is done, those rays"
2760
                PRINT "will be included in the histogram."
                PRINT LIN(2), "PRESS CONT"
2770
2788
                PAUSE
                               The histogram is an illustration of the density"
                PRINT PAGE."
2798
               PRINT "of the rays that intercept the image plane versus radial "PRINT "distance from the GLM axis."
PRINT LIN(2)," When the position has been located, PRESS CONT."
2888
2818
                PRINT LIN(2)," When the position has been located, PRESS CONT." PRINT LIN(2), "PRESS CONT"
2828
2830
2849
                PAUSE
2050
                Digitizes="Y"
                  CALL Graph
2869
2878
                  IF Plots="P" THEN Dense ! P FOR HP-9872 PLOTTER
                Dump_crt$="N"
INPUT "BO YOU WANT A HARD COPY OF THE PLOT ? Y/N", Dump_crt$
2000
2890
2900
                  IF (Dump_crt$="Y") OR (Dump_crt$="y") THEN GOSUB Printer
2910
                PRINT PAGE
               DISP "NORKIN' ON THE HISTOGRAM..."

CALL Density ! PRODUSE A HISTOGRAM OF THE RAY DENSITY
2928
                  CALL Density ! PRO
IF Plot#="F" THEN Denser
2930 Dense:
2946
2950
                Digitizes="N"
                                 ! RESET CONDITION
                INPUT "DO YOU WANT A HARD COPY OF HISTOGRAM ? Y/N", Dump crt$
2968
                  IF (Dump_crts="Y") OR (Dump_crts="y") THEN GOSUB Printer
2978
               Y$="H"
2988 Denser:
                INPUT "DO YOU WANT TO REDRAW THE HISTOGRAM FOR A DIFFERENT IMAGE P
2990
LANE ? Y/H".YS
                  IF (Ys="Y") OR (Ys="y") THEN Flag=0
                  IF (Ys="Y") OR (Ys="y") THEN Re_graph
3610
3028 Ray_traces="N" 3030 Rerun3: YS="H"
3040
              INPUT "DO YOU WANT TO TRY ANOTHER SURFACE (THIS MEANS STARTING OVER
```

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```
> ? Y/N",Y$
3858
                    IF (Y#="Y") OR (Y#="y") THEN Main
                GOTO Finished
3868
3878 Printer: PRINTER IS 16
3686
                     IF (Changes="Y") OR (Changes="y") THEN Y_hards="N"
3898
                     IF (Dump_crt#="Y") OR (Dump_crt#="y") THEN Y_hard#="Y"
                    ir (bump_crts="1") UR (bump_crts="y") THEN Y_hards="y"
IF (Y_hards="Y") OR (Y_hards="y") THEN PRINTER IS 0
IF (Y_hards="Y") OR (Y_hards="y") THEN PRINT CHRs(27)&"&100T"
IF (Bump_crts="Y") OR (Bump_crts="y") THEN Crt
3188
3110
3120
3138
                  FIXED &
3148
                  FIXED 2
                  IF Dates="" THEN 3170
PRINT "DATE: "; Dates
3150
3160
                  PRINT LIN(1), "Alpha = ";Alpha; "degrees"; TAB(48); "Rho-initial = ";R
3170
ho_initial
                  PRINT "TAN(Alpha) = ";Talpha;TAB(48);"TAN(RMO-INITIAL) = ";Trhoi
PRINT LIN(1), "RHO1 = ";Rho1;"degrees";TAB(48);"Theta(critical) =
3198
;Theta_critical;"degrees"
                  PRINT LIN(1), "GLM Radius = ";Y_bullet;"inches"
3200
                  PRINT "Aperture = "; Aperture; TAB(24); "Ya = "; Ya; "inch"; TAB(48); "Yb
 " ";Yb; "inches"
3220
                  FIXED 5
3230
                  PRINT LIN(1), "n1 = "; N1; TAB(24); "n2 = "; N2; TAB(48); "n3"; N3
3248
                  FIXED &
3250
                  PRINT LIN(1), "Number of Rays = "; Nray
3260
                  FIXED 2
3278
                  PRINT LIN(1), "Design Focal Point = ";F;" inches"
3280
                  PRINT
                  IF (Dump_crt*="Y") OR (Dump_crt*="y") THEN DUMP GRAPHICS
IF (Y hard*="Y") OR (Y hard*="y") THEN PRINT CHR*(27)% % 136T"
IF (Dump_crt*="Y") OR (Dump_crt*="y") THEN PRINTER IS 16
Change*="N" ! RESET CONDITION
3290 Crt:
3300
3310
3320
                  Bump_crt*="N"
Y_hard*="N"
3338
3340
3358
               RETÜRN
3480
            RETURN
3439
                  RETURN
      Finished: DISP "FINISHED"
3440
3450
            END
3460
      SUB Snell
3478
         OPTION BASE 0
3480
3490
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
3500
         COM F, 23, 24, Norm, Thetai, Tdelta
3510
         COM Dates, Plots, Familys, Charts, Mains, Main1s, Flags, Y_hards
3520
3530
         CON Stuffs, Redraws, Digitizes, Ray_traces
        COM INTEGER I, J, Y0 loop, Nray, Nray chart, Nray family, Nray stuff
COM INTEGER Nray trace, Nray density, Add_ray, Nc, Ns, Nbeta, Flag
3540
3550
3568
        COM INTEGER Line_count,Line_max,N_increment,Hit_total,Pselect,Hpib COM INTEGER Family,Surf_no COM REAL Theta_critical,Tol,N1,N2,N3,Delta_ray,Y8,Ya,Yb,Apenture
3578
3588
3590
3600
3610
       DEG
3628 One: Thetai #98-(Alpha+ABS(Rho))
                                                   ! RHO MUST BE DECLARED ELESHHERE
             Alpha2=Alpha
3630
3640
             Norm=Alpha2-98
3650
             Sin_iprime=N1/N2+SIN(Thetai)
3660
             Thetar=ASN(Sin_iprime)
```

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3670

Rhoi=Aipha2+Thetar-98

A TAT THE PARTY

! USE ALPHA2 INSTEAD OF NORM BECAUSE THE

```
3688
                                           ! SIGN OF THE ANGLE IS DESIRED
3690
            Trho1=TAN(Rho1)
3760 SUBEND
3719 SUB Plat
3720
        OPTION BASE 0
3730
3748
        COM Alpha, Talpha, Rho, Trho, Rho_initial, Trho1, Rho1, Trho1, Rho2, Trho2
3750
        COM F, 23, 24, Norm, Thetai, Tdelta
3760
        CON Bates, Plots, Familys, Charts, Mains, Mainis, Flags, Y_hards
3770
3788
        COM Stuffs, Redraws, Digitizes, Ray_traces
3790
        COM INTEGER I.J. 78 loop, Nray, Nray chart, Nray family, Nray stuff
COM INTEGER Nray trace, Nray density, Add_ray, Nc, Ns, Nbeta, Flag
3888
3810
        COM INTEGER Line count, Line max, N_increment, Hit_total, Pselect, Hpib COM INTEGER Family, Surf_no COM REAL Theta_critical, Tol, N1, N2, N3, Delta_ray, Y0, Ya, Yb, Apenture
3850
3838
3848
3850
        COM Y_bullet,Smax_family,Percent_image
COM XI(+),Y1(+),Xc(+),X2(+),Y2(+),X2max(+),Y2max(+)
3860
3878
3888
        COM Y3(+), Y4(+), Beta(+), $2(+), Xsurfmax(+), Ysurfmax(+)
3090
3900
        CDM Ga(+). Smax(+). Alpha2(+). Rho2(+). Hit(+)
3910
3920
         ! THE ORIGINAL OF THIS ROUTINE HAS OBTAINED FROM THE HP UTILITIES LIBRARY
                9845B UTILITY LIBRARY
3930
3740
                PROGRAM CARTRIDGE 2
3950
                89845-19285
3968
                PROGRAM REGPLT
3970
           SUB LAXES HAS ALSO BORROHED FROM THE LIBRARY
3900
3990
               THIS ROUTINE IS USED TO SET UP THE LIMIT, LOCATE, SCALE AND CLIP STATE
MENT
4666
         ! STATEMENTS FOR THE FOLLOWING ROUTINES:
4010
                     1) CHART
4820
                     2) FRHILY
4030
                     3) STUFF
4040
                     4) DENSITY
4050
                     5) RAY_TRACE
4060
        flaga=flagc=0
4878
4000 Set_up:
                    IF (Plots="P") OR (Plots="p") THEN P9872a
4090 Crt: PLOTTER IS 13, "GRAPHICS"
4198
             GOTO 4120
4110 P9872a: PLOTTER IS Pselect, Hpib, "9872A"
                 GCLEAR
4120
4130
                 LINE TYPE 1
4140
                 LDIR .
4150
                 LORG 5
4160
                 LIMIT 0.184.0.146
                                                 ! ALL UNITS IN HILLIMETERS
4170
         DATA -2,-1,1,2
         READ Um, Dm, Md, Mu
4180
4190
          DATA .39794,.69897,.87506
4280
          READ Log2, Log5, Log?
4210
            IF (Bigitizes="Y") OR (Bigitizes="y") THEN Bigit_scale
IF (Ray_traces="Y") OR (Ray_traces="y") THEN Ray_trace
IF (Charts="Y") OR (Charts="y") THEN Chart
IF (Familys="Y") OR (Familys="y") THEN Family
4220
4230
4248
4250
            IF (Stuffs="Y") OR (Stuffs="y") THEN Stuff
4260
4270
4280 Chart: Xmin=0
4290
               INPUT "WHAT IS THE MINIMUM VALUE OF & (INCHES) (DEFRULT = 0 INCH) ?"
, Xmin
4300
               INPUT "WHAT IS THE MAXIMUM VALUE OF S (INCHES) (DEFAULT = 2.0 INCH)
4318 -
?",Xmax
```

```
4329
              IF Flage=1 THEN 4380
4330
            Ymin=Alpha-1
4340
            Ymax=90
4350
            INPUT "WHAT IS THE MINIMUM VALUE OF ALPHA2 (DEGREES) (DEFAULT = ALPH
A-1 DEG> ?", Ymin
4360
            INPUT "WHAT IS THE MAXIMUM VALUE OF ALPHA2 (DEGREES) (DEFAULT = 90 D
EG> ?", Ymax
4378
              IF Flaga=1 THEN 4430
4388
              IF Xmin>Xmax THEN BEEP
              IF Xmin>Xmax THEN DISP "Smin IS > Smax : PLEASE RE-ENTER VALUES IN
4398
 CORRECT ORDER"
              IF Xmin>Xmax THEN HAIT 2500
4498
              IF Xmin>Xmax THEN Flagc=1
4410
4428
              IF Xmin>Xmax THEN Chart
4430
              IF Ymin>Ymax THEN BEEP
4448
              IF Ymin>Ymax THEN DISP "ALPHA2min IS > ALPHA2max : PLEASE RE-ENTER
 VALUES IN CORRECT ORDER"
4450
              IF Ymin>Ymax THEN WAIT 2500
4460
              IF Ymin>Ymax THEN Flaga=1
              IF Ymin>Ymax THEN 4330
4478
4488
            Xorg=Xmin
4490
            Yorg=Ymin
4588
            Flaga=Flagc=0
4518
          GOTO Chart_scale
4528 Family: Xmin=Ymin=Xorg=Yorg=0
             Ymax=Y_bullet
Xmax=5
4530
4540
             INPUT "WHAT IS THE MAXIMUM VALUE OF X (INCHES) (DEFAULT = S INCHES)
4550
 ?",Xmax
4560
               IF Xmax<=Xmin THEN BEEP
               IF Xmax = Xmin THEN DISP "Xmax MUST BE > Xmin. PLEASE RE-ENTER T
4578
HE VALUES IN THE CORRECT ORDER."
4586
               IF Xmax(=Xmin THEN WAIT 2500
4578
               IF Xmax<=Xmin THEN Family
4600 Family_scale: LOCATE 15,130,35,180
4618
                     GOSUS Same
4628
                    SCALE Xmin-.5*ABS(Ytic), Xmax+.5*ABS(Ytic), Ymin-.5*ABS(Ytic), Y
 bullet+.5#ABS(Ytic)
                    CLIP Xmin-.5*ABS(Ytic), Xmax+.5*ABS(Ytic), Ymin-.5*ABS(Ytic), Y
4430
bullet+.5#ABS(Ytic)
4648
                     GOSUB Same_axes
4650
                SUBEXIT
4668 Stuff: Xmin=Ymin=Xorg=Yorg=8
4678
            Xmax=5
4680
            Ymax=Y bullet
INPUT "MHAT IS THE MAXIMUM VALUE OF X (INCHES) (DEFAULT = 5 INCHES)
4698
?",Xmax
4700
              IF Xmax<=Xmin THEN BEEP
              IF Xmax (=Xmin THEN DISP "Xmax MUST BE > Xmin. PLEASE RE-ENTER TH
4718
E VALUES IN THE CORRECT ORDER."
              IF Xmax<=Xmin THEN HAIT 2500
IF Xmax<=Xmin THEN Stuff
4726
4730
4740 Stuff_scale: LOCATE 15,138,35,100
4750
                     GOSUE Same
4768
                  SCALE Xmin-.5+ABS(Ytic), Xmax+.5+ABS(Ytic), Ymin-.5+ABS(Ytic), Y_
bullet+.5+ABS(Ytic)
                   CLIP Xmin-.5+ABS(Ytic), Xmax+.5+ABS(Ytic), Ymin-.5+ABS(Ytic), Y_
4770
bullet+. SeABS(Ytic)
                    GOSUB Same_axes
4788
                SUBEXIT
4790
4888 Ray_trace: Xmin=Xorg=Yorg=8
4810
                Xmax=5
4820
                INPUT "WHAT IS THE HAXIMUM VALUE OF X (INCHES) (DEFAULT = 5 INCH
ES) ?", XBAX
4638
                  IF Xmax<=Xmin THEN BEEP
4848
                  IF Xmax = Xmin THEN DISP "Xmax HUST BE > Xmin. PLEASE RE-ENTE
R THE VALUES IN THE CORRECT ORDER."
```

K

The Party

```
IF Xmax<=Xmin THEN HAIT 2500
4858
                    IF Xmax (=Xmin THEN Ray_trace
4868
4878
                  Ymax=Y_bullet
Ymin=-Ymax
4888
4890 Ray_trace_scale: LOCATE 15,130,25,100
4900
                           GOSUB Same
                         SCALE Xmin-.5*ABS(Ytic), Xmax+.5*ABS(Ytic), -Y_bullet-.25*AB
4918
S(Ytic), Y_bullet+.25*ABS(Ytic)
4929
                          CLIP Xmin-.5+ABS(Ytic), Xmax+.5+ABS(Ytic), -Y_bullet-.25+AB
S(Ytic), Y_bullet+.25#ABS(Ytic)
                           GOSUB Same_axes
4930
4948
                         CLIP Xmin, 180, Ymin, Ymax
4958
                       SUBEXIT
                                                  ! ALL UNITS IN GDU'S
4960 Chart_scale: LOCATE 18,133,28,108
                                                  ! DRAW THE DESIGN CHART
4978
                      GOSUS Same
4988
                    Xtic=(Xmax-Xmin)/10
                    SCALE Xmin, Xmax+.25+ABS(Xtic), Ymin, Ymax+.25+ABS(Ytic)
4998
                    CLIP Xmin, Xmax, Ymin, Ymax
5000
                       GOSUB Same_axes
5010
                    FRAME
5020
5030
                  SUBEXIT
5040 Digit_scale: LOCATE 0,130,30,100
                                                   ! ALL UNITS IN GDU'S
5050
                    Xmax=Y_bullet
                                                       DRAH THE HISTOGRAM
                    Xmin=-Xmax
5060
5070
                    Xorg=Yorg=6
5080
                    Ymax=1
                    Yein=0
5090
5100
                      GOSUB Same
5110
                    SCALE -Y_bullet-.15#ABS(Ytic), Y_bullet+.15#ABS(Ytic), -.15#ABS(
Ytic), 1+.15+ABS(Ytic)
                     CLIP -Y_bullet-.15+ABS(Ytic),Y_bullet+.15+ABS(Ytic),-.15+ABS(
5120
Ytic),1+.15+ABS(Ytic)
                       GOSUB Same_axes
5130
                  SUDEXIT
5140
5158 Same_axes:
dge,Ymax>
5168
                    CALL Laxes (Xtic, Ytic, Xorg, Yorg, 1, 1, 2, Xmin-Xfudge, Xmax, Ymin-Yfu
                  CLIP Xmin, Xmax, Ymin, Ymax
5178
                 RETURN
5188 Same: Lx=LGT(Xmax-Xmin)
            Ly=LGT(Ymax-Ymin)
5198
5200
            Xfudge=.28+(Xmax-Xmin)
5210
            Yfudge=.28+(Ymax-Ymin)
5220 Tic_marks: Testxtic=FRACT(Lx)+(Lx(0)
5230
                 Xtic=18^(INT(Lx)-1)*(1+1.5*((Testxtic>Log2) AND (Testxtic<Log5))
+4*((Testxtic>=Log5) AND (Testxtic(=Log7))+6.5*(Testxtic>Log7))
5240
                  Testytic=FRACT(Ly)+(Ly(0)
                  Ytic=18^(INT(Ly)-1)+(1+1.5+((Testytic>Log2) AND (Testytic(Log5))
5258
+4*((Testytic>=Log5) AND (Testytic(=Log7))+6.5*(Testytic>Log7))
5268
               RETURN
          SUBEXIT
5270
$288 SUB Laxes(Xtic, Ytic, Xorg, Yorg, Xmaj, Ymaj, Minticsize, Xmin, Xmax, Ymin, Ymax)
5290
       OPTION BASE &
5300
5310
       COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
5320
       COM F, Z3, Z4, Norm, Thetai, Tdelta
5330
       COM Bates, Plots, Familys, Charts, Mains, Main18, Flags, Y_hards
5340
5350
       COM Stuffs, Redraws, Digitizes, Ray_traces
       COM INTEGER I, J, YB loop, Nray, Nray chart, Nray family, Nray stuff
COM INTEGER Nray trace, Nray density, Add_ray, Nc, Ns, Nbeta, Flag
5360
5370
3388
       COM INTEGER Line_count,Line_max,N_increment,Hit_total,Pselect,Hpib
COM INTEGER Family,Surf_no
COM REAL Theta_critical,Tol,N1,N2,N3,Delta_ray,Y8,Ya,Yb,Apenture
5390
5466
5410
5420
5430
       COM Y builet, Smax family, Percent image
       CON XI(+), Y1(+), Xc(+), X2(+), Y2(+), X2max(+), Y2max(+)
3440
```

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K TALL DE CASE

```
5450
        COM Y3(+), Y4(+), Beta(+), S2(+), Xsurfmax(+), Ysurfmax(+)
5460
5470
        COM Qa(+), Smax(+), Alpha2(+), Rho2(+), Hit(+)
5480
5498
5500
              THIS ROUTINE IS USED TO DRAW AND LABEL THE AXES FOR THE FOLLOWING
          ROUTINES:
5510
5520
                    1) CHART
5530
                    2) FAMILY
5549
                    3) STUFF
5550
                    4) DENSITY
5568
                    5) RAY_TRACE
5578
         Flag=1
5589
5590
         DEG
         LINE TYPE 1
5698
5619
         LDIR 0
         LORG 5
5628
5630
           IF (Xmin>=Xmax) OR (Ymin>=Ymax) THEN SUBEXIT
         GRAPHICS
5640
5650
         Xfudge=.02+(Xmax-Xmin)
5668
         Yfudge=.02+(Ymax-Ymin)
5670
         Xmaj=1
5688
         Ymaj=1
5698
         Minticize=2
5798
              IF (Digitizes="Y") OR (Digitizes="y") THEN Digit_axis
             IF (Ray traces="Y") OR (Ray traces="y") THEN Ray trace_axis
IF (Charts="Y") OR (Charts="y") THEN Chart_axis
IF (Familys="Y") OR (Familys="y") THEN Family_axis
5710
5729
5739
              IF (Stuff#="Y") OR (Stuff#="y") THEN Stuff_axis
5748
5750 Chart_axis: LINE TYPE 3
5768
                    GRIB Xtic, Ytic, Xorg, Yorg, Xmaj, Ymaj, 2*Minticsize
5778
                    LINE TYPE 1
                    GOTO Labelx
5780
5798 Family_axis: AXES Xtic, Ytic, Xorg, Yorg, Xmaj, Ymaj, Minticsize
                     GOTO Labelx
5806
5818 Stuff_axis: AXES Xtic, Ytic, Xorg, Yorg, Xmaj, Ymaj, Minticsize
5820
                    GOTO Labelx
5830 Ray_trace_axis: AXES Xtic, Ytic, Xorg, Yorg, Xmaj, Ymaj, Hinticsize
5848
                        GOTO Labelx_ray
5850 Digit_axis: AXES .1,.1,0,0,1,1,2
5868
                    GOTO Labelx_d
5870 Labelx: FIXED 3
5000
               LDIR 90
5090
5900 Parx:
               LORG 8
               FOR A=Xorg TO Xmax STEP ABS(Xtic)
MOVE A, Yorg-Yfudge
LABEL USING 5950; A
IMAGE DB. D
5918
5920
5930
5948
                 IMAGE DD. DD
                 IMAGE .. K
5950
5960
               HEXT A
5978 Labely: LDIR 6
5980
               LORG 8
5990 Pary:
               FOR A=Yorg TO Ymax STEP ABS(Ytic)
                                                              ! FOR CHART AND FAMILY
                   MOVE Xorg-Xfudge,A
6010
                 LABEL USING 5950;A
6020
               NEXT A
6838
               GOTO Label
6848 Labelx_ray: LDIR 98
4050
                    LORG 8
                    FOR A=Xorg TO Xmax STEP ABS(Xtic)
HOVE A, Yorg-Yfudge
LABEL USING 5950; A
6060 Parx_ray:
6878
6000
                    HEXT A
6890
6100 Labely_ray: LDIR
                    LORG #
```

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A STATE OF THE PARTY OF THE PAR

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FOR A=-Y_bullet TO Y_bullet STEP ABS(Ytic)
MOVE Xorg-Xfudge, A

IF A=0 THEN LABEL USING 5950; A

IF A=0 THEN Next_a
6120 Pary_ray:
                                                                                                ! FOR RAY_TRACE
6130
6148
6150
                              LABEL USING 6170; A
6160
6170
6188 Hext_a:
                           NEXT A
                           GOTO Label
6190
6200 Labelx_d: LDIR 90
6210
                     LORG 8
                     FOR A=-Y bullet TO Y bullet STEP .1

MOVE A, Yorg-Yfudge
6220
6230
                           IF A=0 THEN LABEL USING 5950; A IF A=0 THEN GOTO Next_aa
6248
6250
6260
                         LABEL USING 6179;A
6278 Next 44:
                    NEXT A
6288 Labely_d: LDIR 0
6290
                     LORG 8
                     FOR A=0 TO Y_bullet STEP .1

MOVE Xorg-Xfudge,A

IF A=0 THEN LABEL USING 5950;A

IF A=0 THEN GOTO Nexta
6300
6318
6328
6330
6340
                         LABEL USING 6170; A
6350 Nexta:
                      NEXT A
6360 Label_: SETGU
6370
                  LDIR .
6388
                  LORG 5
6390
                   CSIZE 2.5
6400
                     IF (Digitizes="Y") OR (Digitizes="y") THEN Digit_label
                     IF (Bigitizes="Y") OR (Bigitizes="y") INEM Bigit_label
IF (Ray_traces="Y") OR (Ray_traces="y") THEN Ray_trace_label
IF (Charts="Y") OR (Charts="y") THEN Chart_label
IF (Familys="Y") OR (Familys="y") THEN Family_label
IF (Stuffs="Y") OR (Stuffs="y") THEN Stuff_label
6418
6420
6430
4440
6450 Chart_label: Centerx=74.88
6460
                          Centery=64
6470
6480
                             MOVE .5+Centerx.9
                          LABEL USING 6500; F
IMAGE "Design Focal Point: ", DD. DD, " inches"
6490
6500
6510
                             MOVE 1.5+Centerx,9
                          LABEL USING 6538; Nray chart
IMMGE "Number of Rays : ",K
6520
6538
                             MOVE .5+Centerx,5
6540
                          LABEL USING 6360; Alpha
IMAGE "Alpha: "DD.DD" deg"
6550
6568
                             MOVE 1.5+Centerx,5
6578
                          LABEL USING 6390; H2
IMAGE "n2 : ", D. DDDDD
4520
6590
6600
6618
                          CSIZE 3
6620
                            MOVE Centerx, 15
                          LABEL "8 : Distance Along Refracted Ray in the Lens ( Inches )
6630
6640
                          HOVE .8, Centery
LABEL "Alpha 2: Angle of the Tangent Line at"
6650
6660
6670
                            HOVE 4.8, Centery
6680
                          LABEL "the Second Surface ( Degrees )"
6690
6700 GOTO End_label
6710 Family_label: Centerx=Centerx_family=72.5
6720 Centery=Centery_family=66.5
6730
                              IF (Stuffs="Y") OR (Stuffs="y") THEN Stuff_label
6746
6750
                              MOVE .5.Centerx,9
6760
                           LABEL USING 6500; F
                              MOVE 1.5.Centerx.9
```

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```
LABEL USING 6530; Nray_family .
6720
6790
                           MOVE . S+Centerx, 5
                         LABEL USING 6560; Alpha
6818
                            MOVE 1.5*Centerx,5
4828
                         LABEL USING 6590; N2
6830
                         HOVE Centerx,23
LABEL "Distance Along GLM Axis (inches)"
CSIZE 3
6848
6950
6860
                         MOVE Centerx, 15
LABEL "FAMILY OF SURFACES"
6879
6988
6878
                         LDIR 98
                           MOVE 1.5, Centery
6910
                         LABEL "Radial Distance from the Axis (inches)"
4924
6936 GOTO End_label
6940 Stuff_label: Centerx=72.5
6950
                       Centery=66.5
6960
6970
                          HOVE .5+Centerx,9
                       LABEL USING 6500; F
HOVE 1.5+Centerx, 9
6980
6990
                        LABEL USING 6538; Hray_stuff
7000
7910
                          HOVE .5*Centerx,5
7020
                        LABEL USING 6560; Alpha
                       MOVE 1.3+Centerx,5
LABEL USING 6590; N2
7030
7848
                       MOVE Centerx,5
LABEL USING 7070; Aperture
IMAGE "Aperture: "DD. DDD" inch"
7050
7868
7070
7000
7090
                          MOVE Centerx, 23
7100
                        LABEL "Distance Slong GLM Axis (inches)"
7110
                        CSIZE 3
7120
                          MOVE Centerx, 15
                        LABEL USING 7148; Family
IMAGE "SURFACE NUMBER "K
7130
7140
7158
7160
                       LDIR 90
                       MOVE 1.5, Centery
LABEL "Radial Bistance from the fixis (inches)"
7170
7188
7196
7266 GOTO End_label 7218 Ray_trace_label: Centerx=72.5
                                                                  ! CHANGE IN GRAPH AS WELL
7228
                             Centery=62.5
7230
7240
                               HOVE 1.5*Centerx, 5
7250
                             LABEL USING 6538; Nray_trace
                             MOVE .5*Centers, 18
LABEL USING 7288; Rho_initial
INAGE "Incident Ray Angle : ",38.88," deg"
7260
7270
7200
                               MOVE .5-Centerx, 6
7290
                             LABEL USING 7070: Aperture
                               HOVE 1.5+Centerx,6
7310
                             LABEL USING 6590; NZ
7330
                               HOVE .5+Centerx, 2
                             LABEL USING 6560; Alpha
                             HOVE Centerx, 23
LRBEL "Distance Along the GLM fixis ( inches )"
7350
7360
7370
                             CRIZE 3
                             MOVE Centerx, 15
LABEL USING 7410; Family
IMAGE "SURFACE HUMBER ",K
7418
7430
7440
                             LDIR 90
                             MOVE 1.3, Centery
```

```
7450
                             LABEL "Radial Distance From the fixis ( inches )"
7460
7470 GOTO End_label
7488 Digit_label: Centerx=61.56
7498
                        Centery=65
7500
7510
                          MOVE 1.5+Centerx,13
                        LABEL USING 6530; Nray trace
7520
7530
                          MOVE Centerx/2,9
                        LABEL USING 7550; Hit_total IMAGE "Number of Hits on the Image Plane: ",K
7540
7550
                          MOVE 1.5*Centerx, 9
7568
                        LABEL USING 7580; Percent image IMAGE "% of Rays to Image Plane: ",30.00
7570
7588
7598
                          MOVE 1.5*Centerx,5
                        LABEL USING 7610; 23
IMAGE "Image Plane: ", DD. DD, " inches"
7688
7610
                        MOVE .5+Centerx, 5
LABEL USING 7640; N_increment
7628
7630
7640
                        IMAGE "Number of Increments [0,1.1] : ",K
7658
                        CSIZE 3
7660
                          MOVE Centerx, 28
7680
                        LABEL "Normalized Number of Hits vs Distance from the GLM Ax
                          MOVE Centerx/2,13
7698
                        LABEL USING 7710; Family IMAGE "SURFACE NUMBER ", K
7788
7718
7729
7730 End_label: CSIZE 15/4.54
7748
7759
                     LDIR 0
7760
                     SETUU
7778
                  SUBEND
7788 SUB X1pos(X,Y)
7798
         OPTION BASE 0
7880
7818
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
7828
         INTEGER 2
7839
7848
       DEG
       DEF FNY1(Y)=Y+Talpha/(Talpha-Trhoi) ! FINDS THE Y-VALUE OF THE INTERCEPT ! OF THE RAY AND THE FIRST SURFACE DEF FNX1(Y)=Y/Talpha ! FINDS THE X-VALUE OF THE INTERCEPT OF THE RAY
7859
7860
7878
7880
                                       ! AND THE FIRST SURFACE
7890
             Y=FHY1(Y)
             X=FNX1(Y)
7910
             SUBEND
7920
                                                      SUB Char
7938 One: FOR Z=8 TO 79
7940
7956
                   IF Z=79 THEN 7960
                 PRINT CHR#(228);
7960
7970
                   IF Z=79 THEN PRINT CHR$(228)
              HEXT Z
           SUBEXIT
7988
7998
       SUBEND
      SUB Dialogue
...
         OPTION BASE 0
8020
1030
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
1040
         COM F, 23, 24, Norm, Thetai, Tdelta
8050
         COM Dates, Plots, Familys, Charts, Mains, Mainis, Flags, Y_hards
-
9979
        COM Stuffs, Redraws, Bigitizes, Ray_traces
COM INTEGER I, J, Y0_loop, Nray, Nray_thant, Nray_family, Nray_stuff
COM INTEGER Nray_trace, Nray_density, Add_ray, Nc, Ns, Nbeta, Flag
2026
0070
8106
```

```
.110
         COM INTEGER Line_count, Line_max, N_increment, Hit_total, Pselect, Hpib
        COM INTEGER Family, Surf no
COM REAL Theta_critical, Tol, N1, N2, N3, Delta_ray, Y0, Ya, Yb, Aperture
8120
8130
$140
         COM Y_bullet,Smax_family,Percent_image
COM_XI(+),Y1(+),Xc(+),X2(+),Y2(+),X2max(+),Y2max(+)
8150
8160
8178
         COM Y3(+), Y4(+), Beta(+), S2(+), Xsurfmax(+), Ysurfmax(+)
8180
8190
         COM Qa(+), Smax(+), Alpha2(+), Rho2(+), Hit(+)
8288
....
              THIS ROUTINE INITIALIZES MOST OF THE VARIABLES USED IN THE PROGRAM
8228
6230
       DEG
8248
      Initialize_top: fipha=21
8250
                        Talpha=TAN(Alpha)
0260
                        To1 -. 00001
8278
8288
                        Z3=Z4=50
6290
                        N1=1
6300
                        H2=4
8318
                        H3=1
8328
                        Fed
6336
                        Y_bullet=1.1
                                                 ! WHEN YA # 0 THEN THEN THE BORDERS OF THE
9349
                        YASS
8350
                                                 ! APERTURE ARE ILLUSTRATED BY DRAWING A
                        Yb=Y bullet
                                                 ! RAY AT Y=Y& AND Y=Yb. THIS IS DOME BY ! ADDING A RAY TO ALL NRAY_X DECLARATIONS
                        Aperture=Yb-Ya
8368
8378
                        Add rause
8388
                        Nray-10
                        Rho_initial=Rho=0
Trhoi=Trho=TAN(Rho_initial)
8390
8400
8410
                        Line_count=0
                        Line_max=45
8428
8430
                        H_increment=100
8440
                        Paelect=7
8458
                        Hp15=5
                        P101#="C"
2448
                        Dates="
8478
0400
                        Familys="N"
8490
                        Stuffs="H"
1500
                        Digitizes="H"
                        Redrause"H"
8510
                        Ray_traces="H"
8520
         PRINT PAGE, "Note to the operator: "PRINT LIN(2)," When a request for information is placed on the screen"
0530
         PRINT LIN(2)," When a re
PRINT "two options exist:"
9549
8558
                        ," 1) key in the required information and PRESS CONT."

2) PRESS CONT if the data/parameter or other response "
         PRINT LIN(1),"
PRINT " 2)
8568
8576
         PRINT "
                            has not or will not change from the previous entry. If in"
2524
         PRINT "
                            doubt, key in the correct response or data and PRESS CONT.
2590
2600
         PRINT LIN(2), "PRESS CONT"
0610
         PAUSE
         PRINT PAGE, "The sign convention is :"
0620
8630
         PRINT LINCES,"
                                  1) the origin is placed at the vertex of the first su
rface"
8648
                                       and the GLH axis."
         PRINT "
                         2) distances: positive to the right of the origin."
positive above the origin (Radial distance)."
1656
         PRINT "
1660
9670
9690
                         positive out of the meridian plane (screen)."
(ie. a right hand system.)"
3) angles: POSITIVE IF counter-clockwise"
         PRINT "
         PRINT "
9690
9700
         PRINT "
         PRINT " rotation from the GLM axis to the ray"
PRINT LIN(2), "PRESS CONT"
0710
8720
         PRUSE
               PRINT PAGE," Alpha is the angle of inclination (ie. the cone" PRINT "half-angle) of the FIRST surface with respect to the GLM-axis
6736 Ripha: PRINT PAGE,"
```

```
PRINT LIN(3)," The current value of ALPHA is";Alph INPUT "WHAT IS NEW VALUE OF ALPHA (DEGREES)?",Alpha
8759
                                 The current value of ALPHA is":Alpha: "degrees"
8760
              Talpha=TAN(Alpha)
8776
                                The lens system is assumed to be operating in air."
8788 Index: PRINT PAGE,"
2790
         PRINT "Therefore the first index of refraction is defined as ni= 1.00000
2222
         PRINT LIN(2),"
PRINT "
                              It is assumed that n1 < n2"
8818 PRINT " and n2 > n3."
8828 N2: INPUT "WHAT IS n2 (DEFAULT VALUE = 4) ?",N2
8838 N3: INPUT "WHAT IS n3 (DEFAULT VALUE = 1) ?",N3
             IF N3CN2 THEN Theta_critical=ASN(N3/N2)
IF N3ON2 THEN BEEP
8848
8858
             IF N3>N2 THEN DISP "n2 MUST BE > n3. PLEASE RE-ENTER n2 AND n3."
8860
8879
             IF N3>N2 THEN HALT 4000
             IF N3>N2 THEN N2
....
8890 Rho_initial: PRINT PAGE,"
                                       The rays incident on the first surface are "
1700
                     PRINT "assumed to be parallel to the GLM-axis.
8918
                     PRINT LIN(5), "PRESS CONT"
8920
                     PAUSE
                     Rho=Rho_initial
2932
2548
                     Trho=TAN(Rho)
8958
                                           ! COMPUTE RHO!
                       CALL Snell
8968 Y_bullet: PRINT PAGE,"
                                  The GLM is assumed to be symmetric around the long
itudinal'
2978
                  PRINT "axis. The maximum radius, called Y_bullet, is ";Y_bullet;"
inches."
1786
                  PRINT LIN(2),"
                                     If your design requires a different radius, plea
50°
8998
                  PRINT "enter the new value now."
9000
                  INPUT "Y_bullet (INCHES) ?",Y_bullet
9018 Aperture: PRINT PAGE,"
                                   The aperture is the difference in radial distance
from the GLM axis,
9828
                  PRINT "projected onto the first surface, into which light is allo
ued to enter"
                 PRINT "the GLM optical system. The parameter values are:"
9838
                 PRINT LIN(2),"
9848
                                        Ya = the lower aperture limit (default value =
 ": Y4; "inch) "
9858
                  PRINT "
                                Yb = the upper aperture limit (default value = ":Yb:"
inch)"
9060
                  PRINT "
                                      and is always less than or equal to Y_bullet."
                  INPUT "WHAT IS YA (INCHES) ?", YA
INPUT "WHAT IS YB (INCHES) ?", YB
9978
9080
9090
                    IF YA>=Yb THEN BEEP
9100
                    IF Ya>=Yb THEH DISP "Ya MUST BE < Yb. Please enter correct valu
9110 IF Ya>=Yb THEN HAIT 3000
9120 IF Ya>=Yb THEN Aperture
9130 IF Yb>Y bullet THEN BEEP
9140 IF Yb>Y_bullet THEN DISP "Y_bullet MUST BE > Yb: PLEASE RE-
ENTER Y_bullet, Ya_AND Yb."
                 IF Yb)Y_bullet THEN HALT 3000
IF Yb>Y_bullet THEN Y_bullet
Apenture=Yb-Ya
9150
7168
9170
                    IF YaC'S THEN Add_ray=1
9180
                             The program will trace"; Nray; " rays through the system
9190 Nray: PRINT PAGE,"
 usless
9288
             PRINT "you specify another value."
9210
            PRINT LIN(2), "CAUTION: Entering too many lines will clutter the des
ign chart."
9228
                     PRINT "
                                        Try"; Nray; " rays, then decide if you want more
 or less rays."
9230
             INPUT " HOW MANY RAYS DO YOU WANT THE PROGRAM TO TRACE ?", Newy
               IF Nray(2 THEN BEEP
IF Nray(2 THEN DISP "YOU MUST USE AT LEAST TWO (2) RAYS. PLEASE R
9240
9250
E-ENTER THE CORRECT VALUE."
               IF Mray<2 THEN WAIT 2500
IF Mray<2 THEN Mray
9278
```

```
9288 Focus: PRINT PAGE,"
                                  The focal point is the location on the GLM-axis at wh
ich "
9298
                PRINT "you want all of the rays to pass through."
9388
                PRINT LIN(2),"
                                       The minimum value of the focal point is ";Y_bullet/
Talpha; " inches. "
9318
                PRINT "This value has been Chosen to prevent the angle of the tangen
t line"
9320
                PRINT "of the second surface from exceeding 90 degrees at y = "; Y_b u
1101
9336 PRINT "(ie. at y = Y bullet inches )."
9340 PRINT LIN(2)," The default value is ";F;" inches."
9350 INPUT "WHAT IS THE VALUE OF THE FOCAL POINT ?",F
9368 Date: PRINT PAGE
              INPUT "WHAT IS TODAY'S DATE ?", Dates
9378
9380 Start: PRINTER IS 16
9390 Gymnastics: SUBEND
9488 SUB Chart
9410
         OPTION BASE 0
9428
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rhoi, Trhoi, Rho2, Trho2
COM F, Z3, Z4, Norm, Thetai, Tdelta
9438
9448
9450
         COM Bates, Plots, Familys, Charts, Mains, Main1s, Flags, Y_hards
9468
         COM Stuffs, Redraus, Digitizes, Ray_traces
COM INTEGER I, J, Y@ loop, Nray, Nray_thant, Nray_family, Nray_stuff
COM INTEGER Nray_trace, Nray_density, Add_ray, Nc, Ns, Nbeta, Flag
9478
9489
9498
9588
         COM INTEGER Line count, Line max, N_increment, Hit_total, Pselect, Hpib
COM INTEGER Family, Surf_no
COM REAL Theta_critical, Tol, N1, N2, N3, Delta_ray, Y0, Ya, Yb, Aperture
9510
9528
9538
9548
9550
         COM Y_bullet, Smax_family, Percent_image
9568
         COM XI(+), Y1(+), XC(+), X2(+), Y2(+), X2max(+), Y2max(+)
9578
         CON Y3(+), Y4(+), Beta(+), $2(+), Xsurfmax(+), Ysurfmax(+)
9588
7570
         COM Qa(+), Smax(+), Ripha2(+), Rho2(+), Hit(+)
7690
9610
              THIS ROUTINE COMPUTES AND DRAWS A FAMILY OF CURVES REPRESENTING THE
           RELATIONSHIP BETHEEN THE DISTANCE ALONG THE RAY REFRACTED AT THE FIRST SURFACE OF THE LENS AND THE SLOPE (DERIVED FROM SNELL'S LAW) REQUIRED
9620
9630
9648
            TO SUCCESSFULLY REFRACT THAT RAY THROUGH THE DESIRED FOCAL POINT.
9650
9668
              THE NOTABLE VARIABLES ARE:
                    1) BETA: THE ANGLE OF A LINE BRAWN FROM THE FOCAL POINT TO THE INTERCEPT OF THE RAY AND THE FIRST SURFACE
2) RHO1: THE ANGLE OF THE REFRACTED FROM THE FIRST SURFACE WITH
9678
9688
9698
9700
                                 RESPECT TO THE GLM-AXIS (REF)
                    3) RHOZ : THE REQUIRED ANGLE OF THE REFRACTED RAY FROM THE SECOND
9710
                                 SURFACE HRT REF
9720
9730
                    4) HIGH : RHO1 > BETR
9748
                    5> LOH : RHO1 < BETA
                    6) ALPHA2 : THE SLOPE OF THE SECOND SURFACE HRT REF REQUIRED TO
9750
9760
                                    SATISFY SHELL'S LAW
9778
                    7) S : THE DISTANCE ALONG THE RAY REFRACTED FROM THE FIRST
                    SURFACE, MEASURED FROM THE FIRST SURFACE

3) 9: INTERCEPT POINT OF THE INCIDENT RAY AND THE FIRST SURFACE

5) A: X-INTERCEPT OF THE RAY REFRACTED AT Q
9788
9798
9000
9818
                  18) OR : BISTANCE FROM O TO A
9020
9030
          DEG
         Nray_chant=Nray
IF (StuffS="Y") OR (StuffS="y") THEN Nray_chant=Nray_stuff
9040
9850
7868
         Chart#="Y"
9878
           CALL Header
         F1 ag=0
9898 Draw axes:
                      CALL Plot
```

```
9900 Beta: FOR I=1 TO Mray chart
                                          ! COMPUTE BETA FOR EACH RAY
               Theta=Y1(1)/(X1(1)-F)
9910
9928
               Beta(I)=ATN(Theta)
9930
               A=X1(I)-Y1(I)/Trhol
                                             ! COMPUTE THE DISTANCE ALONG THE REFRACTED
9948
               Qa2=(X1(I)-A)^2+Y1(I)^2 ! RAY TO THE X-INTERCEPT
9950
               Qa(1)=SQR(Qa2)
                                             ! THIS IS THE MAX ALLOWED VALUE OF S
9968
            NEXT I
9978 Chart: FOR Nbeta=1 TO Nray_chart ! COMPUTE ALPHR2 AND S FOR EACH RAY
9988
                58=8
9990
                Smax=Qa(Nbeta)
10000
                Hstep=Smax/20
10010
                J=8
18828 S: FOR S=S0 TO Smax STEP Nates
10030
              J=J+1
18849
                IF ABS(Beta(Nbeta))>ABS(Rho1) THEN High
                IF S(8 THEN Next_beta
CALL_Low_region(S,Alpha2,Nbeta)
10050
10060 Lou:
10679
                IF Tdelta(0 THEN Negative
                IF Rho2>8 THEN Negative
10000
10090
                IF Alpha2>=98 THEN Negative
              IF Line_count>Line_max THEN CALL Header
PRINT USING Image_data; Nbeta, Beta(Nbeta), Thetai, Norm, Rho2, S, Alpha2
19189
16118
18128
              Line_count=Line_count+1
                GOSUB Graph
10130
             GOTO Next s

CALL High region(S, Alpha2, Nbeta)

IF Tdelta(0 THEN Negative
10140
18158 High:
10160
                IF Rho2>0 THEN Negative
IF 81pha2>=90 THEN Negative
10170
10180
             IF Line count>Line max THEN CALL Header
PRINT USING Image_data; Nbeta, Beta(Nbeta), Theta; Norm, Rho2, S, A1 pha2
10190
10200
10216
              Line_count=Line_count+1
                GOSUS Graph
18228
             GOTO Next_s
18238
18248 Zero_cross_over:A=F*SIN(A1pha)/SIN(A1pha+ABS(Beta(Nbeta)))
                         B=S+COS(ABS(Beta(Mbeta))-ABS(Rhol)) ! CONDITION EXISTS IN D=A-B ! HIGH WHEN ALPHA2 > 90 DEGREES
10250
18268
10270
                          E=S+SIN(ABS(Beta(Nbeta))-ABS(Rho1))
10280
                          Tdelta=E/D
16290
                          ArhoZ=ABS(Beta(Nbeta))+ATN(Tdelta)
18388
                            IF Arho2<8 THEN Negative
10310
                          Rho2=-1+Arho2
18328 Horm_z_cross: A=COS(Rho2)-N2/N3+COS(Rho1)
10330
                      B=N2/H3+SIH(ABS(Rho1))-SIH(ABS(Rho2))
18348
                      Inora=B/A
18356
                      Norm=ATH(Inorm)
10360
                      Thetai=Norm+ABS(Rhol)
18378
                      Thetar=Norm+ABS(Rho2)
10300
                      Alpha2=Norm+98
             IF Line_count>Line_max THEN CALL Header
PRINT USING Image_data; Nbeta, Beta(Nbeta), Thetai, Norm, Rho2, S, Alpha2
Line_count=Line_count+1
GOSUB Graph
19390
10400
10410
16426
19436 Hext_s:Smax(Nbeta)=8
18448
               Alpha2(Nbeta)=Alpha2
18450
               HEXT S
18448
               S=S-Nates
18478
                IF S(Qa(Nbeta) THEN Negative
18488 Hext_beta: IF Line_count>Line_max THEN CALL Header
                  PRINT
18498
10500
                  Line_count=Line_count+1
Flag=2
10510
                                                  ! LABEL THE PLOT WITH NBETA
                     GOSUB Graph
10520
10530
                  Flagel | RESET
10540
                HEXT Hoesa
10550 -
             F1 ag=3
                                                       ! TELL GRAPH THIS IS THE LAST BETA
10560
                CALL Graph
```

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```
19570
                Chart#="N"
                   CALL Header_end
10500
10590
                SUBEXIT
19688 Hegative: IF Nstep<Tol THEN Next beta
19618 S=S-Nstep ! RH02 < 0 FOR LOW OR ALPHA2 > 0 FOR HIGH OR LOW
10620
                    S8=S
19638
                    Hstep=Hstep/10
18648
                    Rho2=8
10650
                    GOTO S
18668 Graph: GRAPHICS
19670
                  SETUU
10680
                 LINE TYPE 1
10690
                 LDIR 0
10700
                  LORG 2
10710
                  CSIZE 2.5
10728
                    IF J=1 THEN MOVE S, Alpha2
                    IF J=2 THEN DRAW S,Alpha2 ! DO NOT CHANGE
IF (J>=3) AND (Flag<>2) THEN DRAW S,Alpha2 ! DO NOT CHANGE
IF Flag=2 THEN LABEL USING 10770; Nbeta
10730
18748
1975A
10760
                  CSIZE 15/4.54
10779
                  IMAGE K
10780
             RETURN
        Image data:IMAGE DDD,4X,3(4D.3D,5X),4D.3D,5X,2D.3D,5X,4D.3D
! IMAGE STATEMENT IS FOR Nbeta, Beta(Nbeta), Thetai, Norm, Rho2, S, Alpha2
10790
10800
16616
         SUBEND
10020
        SUB Low region(S, Alpha2, INTEGER N)
10030
         OPTION BASE 0
19648
10050
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
10060
         COM F, 23, 24, Norm, Thetai, Tdelta
10878
         COM Dates, Plots, Familys, Charts, Mains, Main1s, Flags, Y_hards
10000
         COM Stuffs, Redraws, Digitizes, Ray_traces
COM INTEGER I, J, Y0_loop, Nray, Nray_chart, Hray_family, Nray_stuff
COM INTEGER Nray_trace, Nray_density, Add_ray, Nc, Ns, Nbeta, Flag
10890
18988
16918
10920
         COM INTEGER Line_count, Line_max, N_increment, Hit_total, Pselect, Hpib COM INTEGER Family, Surf_no COM REAL Theta_critical, Tol, Hi, N2, N3, Delta_ray, Y0, Ya, Yb, Aperture
19939
10940
10950
10968
         COM Y_bullet,Smax_family,Percent_image
COM XI(+),Y1(+),Xc(+),X2(+),Y2(+),X2max(+),Y2max(+)
COM Y3(+),Y4(+),Beta(+),S2(+),Xsurfmax(+),Ysurfmax(+)
18970
10700
10990
11000
11010
         COM Qa(+), Smax(+), Alpha2(+), Rho2(+), Hit(+)
11020
11030
         DEG
11646 Tdelta: A=SIN(Alpha+ABS(Beta(N))) ! COMPUTE RHO2 = f(S)
11050
                 B=F+SIN(Alpha)/A
11060
                  C=$+CO$(AB$(Rho1)-AB$(Beta(N)))
11070
                  D=R-C
11000
                  E=$#$IN(ABS(Rhol)-ABS(Beta(N)))
11896
                  Tdelta=E/D
11100
                  Delta=ATH(Tdelta)
11110
                  Arho2=ABS(Beta(N))-Delta
11120
                  Rho2=-1+Arho2
11130 Normal: A=COS(Rho2)-H2/H3+COS(Rho1) ! COMPUTE ALPHA2 = f(RHO2)
11140
                  B=$IH(AB$(Rho2))-H2/H3+$IH(AB$(Rho1))
11150
                  Tanorn=3/A
                  AnormeRTN(Tanorm)
11160
                  Thetai=Anorm-ABS(Rho1)
11170
11180
                  Thetar=Anorm-ABS(Rho2)
11190
                  Norme-1#Anorm
11200
                  Alpha2=98+Horm
11210 SUBEND
11228 SUB High region(S.Alpha2, INTEGER N)
11236 OPTION BASE 9
```

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```
11240
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2 COM F, Z3, Z4, Norm, Thetai, Tdelta
11250
11260
11278
          COM Bates, Plots, Familys, Charts, Mains, Mainls, Flags, Y_hards
11200
11298
          COM Stuffs, Redraws, Bigitizes, Ray_traces
         COM INTEGER I, J, YO loop, Nray, Nray chart, Nray family, Nray stuff COM INTEGER Nray trace, Nray density, Add_ray, Nc, Ns, Nbeta, Flag
11366
11310
11329
11338
         COM INTEGER Line_count, Line_max, N_increment, Hit_total, Pselect, Hpib COM INTEGER Family, Surf_no COM REAL Theta_critical, Tol, N1, N2, N3, Delta_ray, Y0, Ya, Yb, Apenture
11340
11350
11360
11379
         COM Y_bullet,Smax_family,Percent_image
COM X1(+),Y1(+),Xc(+),X2(+),Y2(+),X2max(+),Y2max(+)
11380
11390
          COM Y3(*), Y4(*), Beta(*), S2(*), Xsurfmax(*), Ysurfmax(*)
11400
11418
         COM Qa(+), Smax(+), Alpha2(+), Rho2(+), Hit(+)
11429
11430
        DEG
11440 High: A=SIN(Alpha+ABS(Beta(N))) ! COMPUTE RHO2 = f(S)
11458
             B=F+SIN(Alpha)/A
11468
             C=S+COS(ABS(Beta(N))-ABS(Rho1))
11470
             D=2-C
11480
             E=S#SIN(ABS(Beta(N))-ABS(Rho1))
11496
             Tdelta=E/D
11500
             Arho2=ABS(Beta(N))+ATN(Tdelta)
11510
             Rho2=-1*Arho2
11528 Hormal: A=N2/N3+SIN(ABS(Rho1))-SIN(ABS(Rho2)) ! COMPUTE ALPHA2 = f(RHO2)
11530
                B=N2/N3*COS(Rho1)~COS(Rho2)
11540
                Tanorm=A/B
11556
                Anorm=ATN(Tanorm)
11560
                Thetai=ABS(Rho1)-Anorm
11570
                Thetar=ABS(Rho2)-Anorm
11500
                Norm=-1+Anorm
                Alpha2=90+Horm
11590
11600 SUBEND
11619 SUB Family
11628
         OPTION BASE 0
11639
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2 COM F, 23, 24, Norm, Thetai, Tdelta
11648
11650
11660
          COM Dates, Plots, Familys, Charts, Mains, Main1s, Flags, Y_hards
11670
11680
         COM Stuffs, Redraws, Digitizes, Ray_traces
         COM INTEGER I.J. 70 loop, Nray, Nray chart, Nray family, Nray stuff
COM INTEGER Nray trace, Nray density, Add_ray, Nc, Ns, Nbeta, Flag
11690
11798
11710
11720
         COM INTEGER Line_count,Line_max,N_increment,Hit_total,Pselect,Hpib
         COM INTEGER Family, Surf_no
COM REAL Theta_critical, Tol, N1, N2, N3, Delta_ray, Y0, Ya, Yb, Aperture
11730
11740
11760
         COM Y_bullet,Smax_family,Percent_image
COM XI(+),Y1(+),Xc(+),X2(+),Y2(+),X2max(+),Y2max(+)
11770
          COM Y3(+), Y4(+), Beta(+), S2(+), Xsurfmax(+), Ysurfmax(+)
11780
11790
11800
         COM Ga(+), Smax(+), Alpha2(+), Rho2(+), Hit(+)
11810
11820
               THIS ROUTINE COMPUTES AND DRAWS A FAMILY OF SURFACES USING THE
11836
           THE DESIGN CHART DRAWN IN SUBROUTINE CHART
11840
               THE ROUTINE TAKES THE END POINTS OF EACH CURVE OF ALPHA2 VS S
           AND DRAWS A SURFACE USING ALPHAR TO DRAW A LINE TO INTERCEPT THE HEXT
11850
          RAY, THESE SURFACES ARE THEN THE HAXIMUM SURFACES FOR EACH PARAMETER BETA.
11860
11870
11880
11090
               WHEN STUFFS="Y" THE ROUTINE GOES THROUGH THE I LOOP ONCE (ie FOR
11700
          ONE SURFACES AND THE J LOOP HRAY STUFF TIMES.
```

```
11910
11920
        DEG
11930
        Familys="Y"
11948
          CALL Header
11950
       Ymax=Y_bullet
LINE TYPE 1
11960
11970
        LDIR 8
11980
        LORG 5
11990
        CSIZE 15/4.54
12009
                         ! RESET CONDITION
        F1 ag=0
       Nray family=Nray
IF (Stuffs="Y") OR (Stuffs="y") THEN Nray family=Nray stuff
12010
12020
12030 Draw_axes: CALL Plot
                                                      ! DRAWS AND LABELS THE AXES
12848 Step_family=INT(Nray_family<19)
12850 IF Step_family<=0 THEN Step_family=1
12860 First_surfiLINE TYPE 8 ! DRAW THE FIRST SURFACE
12078
                      HOVE 8,8
12080
                   X=Ymax/Talpha
12090
                   DRAH X, Ymax
12166
                   DRAH 100, Ymax
                      IF (Stuff#="Y") OR (Stuff#="y") THEN Delta_b
12110
                   EXIT GRAPHICS
12120
12130
                   BEEP
12140
                    Y$="H"
                   INPUT "DO YOU WANT TO DRAW IN THE INCIDENT RAYS ? Y/N",Y#
                      IF (Ys="H") OR (Ys="n") THEN Delta b
12168
                   GRAPHICS
12170
12188
                   LINE TYPE 3
                   FOR I=Step_family TO Mray_family STEP Step_family MOVE 0, YI(I)
12190
12200
12210
                      DRAW X1(I), Y1(I)
12220
                      A=X1(I)-Y1(I)/Trho1
12239
                      DRAH A, 0
12248
                   NEXT I
12250 Delta_b:GRAPHICS
                  IF (Stuff#="Y") OR (Stuff#="y") THEN Step_family=1
12268
                B1=Y1(Step_family)-X1(Step_family)+Trho1
B2=Y1(Step_family+1)-X1(Step_family+1)+Trho1
Deltab=B2-B1
12270
12288
12290
12300 Starting points:FOR I=Step_family TO Nray_family STEP Step_family 12310 J=I ! PRINTING PURPOSES
                                                               PRINTING PURPOSES
               Flag_over=0
12320
                                                               RESET CONDITION
12330
                                                               RESET CONDITION
               Flag_neg=0
12340
               Sfirst=Slast=Smax(I)
12350
                 IF (Stuff#="Y") OR (Stuff#="y") THEN Sfirst=Slast=Smax(Family)
               $2(1)=$1 ast
12360
                                                             ! FOR STUFF ONLY
12370
               Belta_xsurf=$2(I)+COS(Rho1)
12300
               Belta_vsurf=$2(I)+$IN(Rho1)
12390
               Xsurf21=X1(I)+Belta_xsurf
               Ysurf21=Y1(I)+Delta_ysurf
IF (Stuff8="Y") OR (Stuff8="y") THEN Xsurf21=X1(Family)+Delta_xsu
12400
12419
rf
12420
                 IF (Stuffs="Y") OR (Stuffs="y") THEN Ysurf21=Y1(Family)+Delta_ysu
rf
12430
                 IF Ysurf21<8 THEN GOSUB Neg_ysurf
                                                              ! THE STARTING POINT
12440
               X2(I)=Xsurf21
                                                             I IS BENEATH THE X-AXIS
12450
               Y2(I)=Ysurf21
12460
               Xsurfmax(I)=Xsurf21 !THESE ARE THE MAXIMUM (X,Y) COORDINATES OF THE
12470
               Ysurfmax(I)=Ysurf21 ! RAY IN THE LENS
               IF Flag neg=1 THEN GOSUB New s
Trho21=Y2(I)/(X2(I)-F)
12480
12490
12500
               Rho2(1)=ATN(Trho21)
12510
               Alpha2i=Alpha2(I)
                 IF (Stuffs="Y") OR (Stuffs="y") THEN Alpha21=Alpha2(Family)
12520
                 IF Alpha21>=90 THEN Next_i
12538
12540
               Talpha21=TRN(A1pha21)
               Bsurf21=Ysurf21-Xsurf21+Talpha21
12550
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12568
                Xsurflast=Xsurf21
12570
                 Ysurflast=Ysurf21
12580
                 Bsurflast=Bsurf21
                IF Line count Line max THEN CALL Header
PRINT USING 13470; I, J, Rho2(J), Xsurflast, Ysurflast, Slast, Alpha2i
12590
12600
                Line_count=Line_count+1
LINE_TYPE_1
12610
12628
12630
                   CSIZE 2.5
12640
                   LORG 2
12659
                   MOVE Xsurf21, Ysurf21
                                                                   ! THE STARTING POINT
12660 Surfaces:FOR J=I+1 TO Nray family
12670 Bnext=B1+(J-1)+Deltab
                                                                  ! DRAN THE PARTICULAR SURFACE
                     Numxsurf=Bnext-Bsurflast
12688
12690
                     Xsurfnext=Numxsurf/(Talpha2i-Trho1)
12788
                      Ysurfnext=Xsurfnext+Trho1+Bnext
                     X2(J)=Xsurfnext ! ONLY USED FOR STUFF, DON'T USE AN IF Y2(J)=Ysurfnext ! STATEMENT IN ORDER TO SAVE TIME
12718
12728
12730
                     X1=0
                        CALL Xipos(Xi, Ysurfnext)
IF Xsurfnext(=Xi THEN GOSUB Yi
BRAN Xsurfnext, Ysurfnext
12740
12750
12760
12770
                     Xs2=(X1(J)-Xsurfnext)^2
                                                                   ! COMPUTE NEXT VALUE OF S BY
                                                                   ! EXTENDING THE RAY FROM THE ! PRESENT POINT TO THE NEXT
                      Ys2=(Y1(J)-Ysurfnext)^2
12780
12790
                      Snext=SQR(Xs2+Ys2)
12800
                     $2(J)=Snext
                                                                   ! ALPHA2 VS S LINE
12010
                   IF ASS(Seta(J))>ASS(Rho1) THEN CALL High_region(Snext, Alpha21, J)
12820
                   IF ABS(Beta(J))(=ABS(Rho1) THEN CALL Lou_region(Snext, Alpha21, J)
12830
                Rho2(J)=Rho2
12846
                Alpha2(J)=Alpha2i
                IF Line count >Line max THEN CALL Header PRINT USING 13478; I, J, Rho2(J), X2(J), Y2(J), S2(J), A1pha2(J)
12858
12868
                Line_count=Line_count+1
IF Alpha2i>=90 THEN Next_i
12878
12220
                Talpha2i=TAN(Alpha2(J))
12890
                Bsurfnext=Ysurfnext-Xsurfnext+Talpha2i
12900
12910
                 Baurflast = Baurfnext
12920
                Xsurflast=Xsurfnext
                Ysurflast=Ysurfnext
12930
12940
                   IF (Stuffs="Y") OR (Stuffs="y") THEN 12970
12950
                X2max(I)=Xsurflast
                                            ! USED TO DETERMINE APERTURE FOR STUFF
12968
                 Y2max(I)=Ysurflast
12978
                   IF flag_over=1 THEN Next_i
12980 Hext_j:
                   HEXT J
12990 Next_1:
                   IF Line_count>Line_max THEN CALL Header
                PRINT
13000
                Line_count=Line_count+1
IF (Stuffs="y") OR (Stuffs="y") THEN 13030
IF Flag_over=0 THEN GOSUB Labe1_surf
IF (Stuffs="y") OR (Stuffs="y") THEN 13000
13010
13020
13030
13040
13050
             HEXT I
           LORG 5
13060
                                 ! RESET
13070
           CSIZE 15/4.54
13000
             IF (Stuffs="Y") OR (Stuffs="y") THEN GOSUS YE
           Flag=3
13090
13100
             CALL Graph
                    Family = "N"
13110
                      CALL Header_end
13126
                 SUBEXIT
13138
13146 YI: flag over=1
13156 Xsurfnext=Bsurflast/(Talpha=Talpha2))
            Ysurfnext=Xsurfnext+Talpha
13160
13170
              MOVE Xsurfnext, Ysurfnext
                                                          ! THE ENDPOINT
13180
            CSIZE 3
13190
            LORG 1
               IF (Stuffswin") OR (Stuffswin") THEN LABEL USING 13410; I
IF (Stuffswin") OR (Stuffswin") THEN LABEL USING 13410; Family
13200
13210
13228
               MOVE Xsurfnext, Ysurfnext
                                                   ! PLACE THE PEN BACK ON TOP OF THE POINT
```

```
13236
        RETURN
13248 New_s: Sy2=Y2(I)-Y1(I)
13250
               $x2=X2(I)-X1(I)
13268
               $2(1)=$QR($x2+$y2)
13276
            RETURN
13280 Neg_ysurf: Flag_neg=1
                                               ! IF, FOR SOME NUMERICAL REASON YB1 < 0
13298
                   A=XI(I)-Y1(I)/Trho!
                      IF (Stuffs="Y") OR (Stuffs="0") THEN A=X1(Family)-Y1(Family)/
13300
Trhai
                                                ! START AT THE X-INTERCEPT
13318
                   Xsurf21=A
13328
                    Ysurf21=0
13338
                 RETURN
13340 Label_surf:
                      MOVE Xsurflast, Ysurflast ! THE ENDPOINT
13358
                     CSIZE 3
13360
                     LORG 1
                       IF (Stuffs="N") OR (Stuffs="n") THEN LABEL USING 13+10; I
13370
13388
                       IF (Stuffs="Y") OR (Stuffs="y") THEN LABEL USING 13410; Fam: 1
13390
                       MOVE Xsurflast, Ysurflast ! PLACE THE PEN ON TOP OF THE POINT
13400
                   RETURN
13410
        IMAGE K
      Yb: Bsm=Y2max(Family)-X2max(Family)+Trho1 ! COMPUTE THE UPPER LIMIT X1=Bsm/(Talpha-Trho1) ! OF THE APERTURE. THIS IS THE FINAL VALUE OF
13429
13438
                                      ! THE APERTURE
13448
           Yb=Y1=X1+Talpha
13450
           Aperture=Yb-Ya
13469
         RETURN
        IMAGE 2x, DDD, 5x, DDD, 5(5x, DDD. DDD)

THE IMAGE STATEMENT IS FOR: I, J, Rho2(J), X2(J), Y2(J), S2(J), A1pha2(J)
13478
13488
13490
      SUBEND
13500 SUB Ray trace
13510
         OPTION BASE 8
13520
13530
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
13546
         CON F, Z3, Z4, Norm, Thetat, Tdelta
13550
         CON Dates, Plots, Familys, Charts, Mains, Main18, Flags, Y_hards
13568
13578
         COM Stuffs, Redraus, Digitizes, Ray_traces
         COM INTEGER I, J, YO loop, Nray, Nray chart, Nray family, Nray stuff
COM INTEGER Nray trace, Nray density, Add_ray, Nc, Ns, Nbeta, Flag
13588
13598
13600
13618
         COM INTEGER Line_count,Line_max,N_increment,Hit_total,Pselect,Hpib
COM INTEGER Family,Surf_no
COM REAL Theta_critical,Tol,N1,N2,N3,Delta_ray,Y8,Ya,Yb,Aperture
13620
13630
13640
13650
         COM Y bullet, Smax family, Percent_image
13660
         COM XI(+), Y1(+), XC(+), X2(+), Y2(+), X2max(+), Y2max(+)
13670
         COM Y3(+), Y4(+), Beta(+), S2(+), Xsurfmax(+), Ysurfmax(+)
13680
13690
         COM Ga(+), Smax(+), Alpha2(+), Rho2(+), H(t(+)
13700
13710
              THIS ROUTINE CONTROLS THE RAY DIAGRAM FOR AN ARBITRARY NUMBER
13720
13736
         I OF RAYS WHICH IS ENTERED BY THE OPERATOR IN RESPONSE TO A PROMPT
13740
13750
              THE ROUTINE CONTROLS THE FITTING OF A POLYNOMIAL TO A SET OF POINTS
13760
           WHEN AN ARBITRARY RAY DOES NOT COINCIDE WITH A RAY COMPUTED IN STUFF
13770
13788
        DEG
13790
        Ray_traces="Y"
13800
        Select=16
13810
        EXIT GRAPHICS
13828
13030
        INPUT "DO YOU WANT A HARD COPY OF ALL OF THE GENERATED COEFICIENTS ? Y/N"
, Y$
13840
          IF (Y#="Y") OR (Y#="y") THEN Select=0
13858 - Graphics=1
13060
      Xei
```

一 一

```
13870
        N=4
13888
          CALL Driver(N, Select, X, Graphics)
13890
        Ray_traces="N"
        SUBEND
13900
13910
      SUB Driver(N, Select, Input, Graphics)
13928
13930
         OPTION BASE 1
13948
13950
         COM Ripha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
13960
         COM F, 23, 24, Norm, Thetai, Tdelta
13978
         COM Dates, Plots, Familys, Charts, Mains, Main1s, Flags, Y_hards
13980
13998
         COM Stuffs, Redraws, Digitizes, Ray_traces
         COM INTEGER 1, J, YO loop, Nray, Nray chart, Nray family, Nray stuff COM INTEGER Nray trace, Nray density, Add ray, Nc, Ns, Nbeta, Flag
14888
14018
14828
         COM INTEGER Line_count, Line_max, N_increment, Hit_total, Pselect, Hpib COM INTEGER Family, Surf_no
14838
14848
14950
14868
         DIM Xx(N), Yy(N), A#[2], B#[2], Coeffs(0:10)
14070
         PRINTER IS Select
14000
14090
      P: Degree=3
14100
            CALL Polynomial(Xx(+), Yy(+), N, Degree, Coeffs(+), Regss, Resss, Totalss, Re
gas, Re
       sms, F, Dfreg, Dfres, Dftot, Abort)
14118
          PRINT "Coefficients:
14120
          FOR I=0 TO Degree
            PRINT USING 14148; I, Coeffs(I)
14130
            IMAGE "A("DDDD")=",K
14148
          NEXT I
14150
          PRINT LINCE
14168
14170
          GOSUB Acutable
            IF Graphics AND (Select=16) THEN WAIT 2000
IF Graphics THEN CALL Plot_cubic(Q,A,B,Coeffs(+),Xx(+),Yy(+),N,Degree
14188
14190
e.Select)
14200
      SUBEXIT
14218 Print: PRINTER IS Select
14229
               PRINT LIN(2), SPA(12); "DATA"
14230
               FOR I=1 TO N
14240
                 PRINT USING 14250; 1, Xx(I), Yy(I)
                 IMAGE "Point #"BBBB":",5X,"X2="BBB.DBBB,5X,"Y2="DBB.DBBB
14256
               NEXT I
14260
14276
               PRINT LIN(2)
14290
               PRINTER IS 16
            RETURN
14298
      RETURN

Howtable: PRINT USING 14318

THACE "Source "5X" Df"11X" $8"13X" H8"12X"F",/
14300
14318
                   PRINT USING 14330; Dfreg, Regss, Regms, F
14320
                   INAGE "Regression"5X, NDD, 4X, M7D.3D, 4X, M7D.3D, 5X, M4D.3D
PRINT USING 14350; Dfres, Resss, Resss
14330
14340
                   IMAGE "Residual "5x, MDB, 4x, M7B. 3B, 4x, M7B. 3B
14350
14360
                   PRINT USING 14370; Dftot, Totalss
14370
                   IMAGE "Total
                                       "5X, MDD, 4X, M7D. 3D, /, /, /, /, /
14300
                RETURN
14390
           SUBEND
14466 SUB Polynomial(X(+),Y(+),H,Degree,Coeffs(+),Regss,Resss,Totalss,Regms,Resm
s, F, Bfreg, Bfres, Dftot, Abort)
14418
         OPTION BASE 0
14428
         DIM Matrix(Degree, Degree), Inv(Degree, Degree), B(Degree)
14430
         REDIH Coeffs(Degree)

IF Degree>N-2 THEN SUBEXIT ! Check for higher degree than possible
14440
14450
         Bfreq=Bearee
14460
         Dfres=N-1-Degree
14478
         Dftot=Dfreq+Dfres
14480
         FOR K=8 TO Degree
                                            Set up system of equations
           FOR J=K TO Degree
14490
```

.

14500

( )

Hatrix(K,J)=0

**(** ;

```
14510
                 FOR I=1 TO N
                   Matrix(K, J)=Matrix(K, J)+FNG(K)+FNG(J)
14520
14530
14549
              Matrix(J,K)=Matrix(K,J)
14550
            NEXT J
14568
            B(K)=0
              FOR I=1 TO N
14579
                B(K)=B(K)+Y(I)+FNG(K)
14500
              NEXT I
14598
         HEXT K
14600
         MAT Inv=INV(Matrix)
MAT Coeffs=Inv+B
                                         ! Solve the system of equations
14610
14628
         FOR I=1 TO N
X1=X1+X(I)
14630
14640
14650
            X2=X2+X(I)+X(I)
14660
            Y1=Y1+Y(I)
14678
            Y2=Y2+Y(1)+Y(1)
            Z=Z+X(1)+Y(1)
14688
          NEXT I
14690
14700
          Y1=Y1/N
14710
          X1=X1/N
                                             ! Total Sum of Squares
          Totalss=Y2-N+Y1+Y1
14728
                                             ! Regression Sum of Squares
          GOSUB Regss
Ress=Totalss-Regss
14730
                                             ! Residual Sum of Squares
14740
          Regms=Regss/Dfreg
14759
          Resms=Ress=/Dfres
14768
          F=Regms/Resms
14778
14788 SUBEXIT
14790 Regss:
                 Regss=0
14886
                 FOR I=1 TO N
14819
 14820
                      FOR L=8 TO Degree
                         J=J+X(1)^L+Coeffs(L)
 14830
                      NEXT L
 14849
                      Regss=Regss+(J-Y1)^2
 14859
                 NEXT I
 14868
 14879
               RETURN
14880
             SUBEXIT
 14898 DEF FHG(H)=X(I)^H
 14900 SUBEND
 14910 SUB Plot_cubic(Q, R, B, Coeffs(+), X(+), Y(+), N, Degree, Select)
             IF Whichdevice=1 THEN GRAPHICS
 14920
 14930
          DATA -2,-1,1,2
          READ Um, Dm, Hd, Hu
DATA .39794,.69897,.87586
 14948
 14950
          READ Log2, Log5, Log7
Xmin=fNHin(X(+), N)
 14960
 14970
 14900
          Xmax=FNMax(X(+), N)
          Lx=LGT(Xmax-Xmin)
 15000
           Ymin=FNMin(Y(*), N)
 15010
           Ymax=FNHax(Y(+),H)
          Ly=LGT(Ymax-Ymin)
 15020
 15030
           Xfudge=.20+(Xmax-Xmin)
 15848 Yfudge".28*(Ymax-7min)
15858 Setup: IF Plots="P" THEN P9872
15868 Crt: PLOTTER IS "GRAPHICS"
15878 GOTO 15898
15888 P9872: PLOTTER IS Pselect, Hpib, "9872A"
                 GCLEAR
 15090
                 GRAPHICS
                 LOCATE 23,123,0,100
 15110
                 FRAME
 15120
 15130
                 LINE TYPE 1
                 SCALE Xmin-Xfudge, Xmax, Ymin-Yfudge, Ymax
Testxtic=FRACT(Lx)+(Lx(0)
 15140
 15150
                 Testytic=FRACT(Ly)+(Ly(8)
 15160
```

4 1 1 1 1 1 1

```
15170
               Xtic=18^(INT(Lx)-1)+(1+1.5+((Testxtic>Log2) AND (Testxtic<Log5))+4+
((Testxtic>=Log5) AND (Testxtic(=Log7))+6.5+(Testxtic>Log7))
               Ytic=10^(INT(Ly)-1)+(1+1.5+((Testytic>Log2) AND (Testytic(Log5))+4+
15180
((Testyt
         ic>=Log5> AND (Testytic(=Log7)>+6.5+(Testytic>Log7)>
15190
                 CALL Laxes_cubic(Xtic, Ytic, Xmin, Ymin, 1, 1, 2, Xmin-Xfudge, Xmax, Ymin-
Yfudge, Ymax)
15200
               LORG 5
15210
               FOR I=1 TO H
15220
                 MOVE X(I),Y(I)
15238
                 LABEL USING 15240; "+"
15248
                 IMAGE A
               NEXT I
15250
15260
               LORG 1
15278
               PENUP
15289
               EXIT GRAPHICS
15290
               SUBEXIT
15398 Polynomial: SETUU
                              ! CHECK THE EARLIER PROGRAM FOR THESE PARAMETER VALUES
15310
                     CLIP 0,123,0,100
15320
                     LINE TYPE 1
15336
                     LINE TYPE 6
15340
                     FOR I=Xmin TO Xmax+Xfudge STEP (Xmax+Xfudge-Xmin)/30
15350
                       J=0
15360
                         FOR L=0 TO Degree
15370
                            J=J+I^L#Caeffs(L)
                         HEXT L
15398
15390
                       PLOT I, J, Md
                                                  1 OR DRAW ????
                     NEXT I
15488
                     PENUP
15410
15429
                     EXIT GRAPHICS
15430
                  SUBEXIT
15440 DEF FHMax(X(+), N)
15450
           X=X(1)
15460
           FOR 1=2 TO N
15470
             X=MAX(X,X(I))
15466
           NEXT I
15498
        RETURN X
15500 DEF FNHin(X(+), N)
15510
           X=X(1)
15320
           FOR I=2 TO N
15530
             X=MIN(X,X(I))
15540
           NEXT 1
         RETURN X
15558
15560 SUB Header
15570
         OPTION BASE 0
15586
15590
         COM Ripha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
15600
         CON F, 23, 24, Norm, Thetai, Tdelta
15610
         COM Dates, Plots, Familys, Charts, Mains, Maints, Flags, Y_hards
15620
15630
         COM Stuffs, Redraws, Digitizes, Ray_traces
15640
        COM INTEGER I, J, YO loop, Nray, Nray chart, Nray family, Nray stuff
COM INTEGER Nray trace, Nray density, Add_ray, Nc, Ns, Nbeta, Flag
15650
15660
15670
        COM INTEGER Line_count,Line_max,N_increment,Hit_total,Pselect,Hpib
COM INTEGER Family,Surf_no
COM REAL Theta_critical,Tol,N1,N2,N3,Delta_ray,Y8,Ya,Yb,Aperture
15600
15690
15700
        CON Y_bullet,Smax_family,Percent_image
CON XI(+),Y1(+),Xc(+),X2(+),Y2(+),X2max(+),Y2max(+)
15710
15728
         COM Y3(+), Y4(+), Beta(+), $2(+), Xsurfmax(+), Ysurfmax(+)
15730
15740
15750
         COM @a(+), $max(+), #1pha2(+), Rho2(+), Hit(+)
15760
15770
         INTEGER Z, Ztab1, Ztab2, Ztab3, Char_min, Char_max
15788
             THIS ROUTINE DRAWS THE HEADER FOR PRINTED OUTPUT FOR THE FOLOWING
15790
15000
           ROUTINES:
```

D

0

```
15010
                     1) CHART
15820
                     2) FAMILY
15839
                     3) STUFF
15840
                     4) RAY_TRACE
15858
15860
15878
15080
                THIS ROUTINE DRAWS AND PRINTS THE HEADERS FOR TABULAR DATA.
15898
15900
          DEG
15910
          Ztab1=35
                         ! THE ZTAB'S CAN BE USED TO POSITION TABLE HEADINGS
                         ! FOR THE PRINTED OUTPUT
15920
          Zt ab2=27
15930
          Zt ab3=13
15940
            IF (Mains="Y") OR (Mains="y") THEN Main
15950
            IF (Main1s="Y") OR (Main1s="y") THEN Main1
            IF (Ray traces="Y") OR (Ray traces="y") THEN Ray trace
IF (Charts="Y") OR (Charts="y") THEN Chart
IF (Familys="Y") OR (Familys="y") THEN Family
15960
15970
15988
            IF (Stuffs="Y") OR (Stuffs="y") THEN Family
15998
16000 Hain: PRINT PAGE; LIN(2)
              GOSUB Char_long
PRINT LIN(1);TRB(Ztab2);"INITIAL PARAMETER VALUES";LIN(1)
16919
16828
               GOSUS Char_long
PRINT LIN(2)
16030
16040
16050
            SUBEXIT
                IF Line count>Line_max THEN GOSUB Header_end_long
PRINT PAGE;LIN(2)
16068 Main1:
16080
                Line_count=0
                GOSUB Char_long
PRINT LIN(1); TAB(Ztab3), "RAY
16090
16100
                                                            28
                                                                                         Alpha2
                                                                           Smax
  RHO 2", LIN(1)
16110
                          DISP TAB(Ztab3), "RAY
                                                            QR
                                                                           Smax
                                                                                         Alpha2
  RHO 2"
16120
                  GOSUB Char_long
                PRINT LIN(2)
16130
             SUBEXIT
16148
                IF Line count>Line_max THEN GOSUB Header_end_long PRINT PRGE;LIN(2)
16158 Chart:
16160
                Line_count=0
GOSUB Char_long
PRINT LIN(1), "RAY
ALPHA 2";LIN(1)
DISP "RAY
16170
16180
16190
                                             BETA
                                                           THETRI (RAY)
                                                                              HORMAL
                                                                                               RHO 2
           $
16200
                                             BETA
                                                           THETAI (RAY)
                                                                              HORMAL
                                                                                               RHO 2
                      ALPHA 2"
           $
16210
                  GOSUB Char_long
                PRINT LIN(2)
16226
16230
             SUBEXIT
                 IF Line couns >Line_max THEN GOSUB Header_end_long PRINT PRGE;LIN(2)
16240 Family:
16250
                 Line_count=8
GOSUB Char_long
PRINT LIN(1); 1
16260
16270
16280
                                       Begin
                                                            Xsurf
                                                                             Ysurf
                                                 Hext
   Alpha2
                  RHO 2"
16290
                         PRINT "
                                       Ray
                                                 Ray
                                                             (next)
                                                                            (next)
                                                                                            (next)
   (next)
                   (next)";LIN(1)
                                       Begin
16300
                          DISP "
                                                 Next
                                                            Xsurf
                                                                             Ysurf
                  RHQ 2"
   Alpha2
16310
                   GOSUB Char_long
                 PRINT LIN(2)
16320
16230
              SUBEXIT
16348 Ray_trace:
                     IF Line_count>Line_max THEN GOSUB Header_end_long PRINT PAGE;LIN(2)
16350
                    PRINT PROEJECTION
Line_count=0
GOSUS Char_long
PRINT LIN(1), "RAY X0
Y4 ";LIN(1)
16360
16378
16300
                                                                          Y1
                                                    40
                                                                Χt
                                                                                      X2
                                                                                                Y2
     Χe
            Y¢
                               DISP "RAY
16390
                                            XS
                                                     YB
                                                                XI
                                                                          Y1
                                                                                      X2
                                                                                                Y2
```

```
X4 Y4 GOSUB Char_long
      Χc
             Yc
16400
                       PRINT LIN(2)
16418
16420
                    SUBEXIT
16438 Char_long: FOR Z=8 TO 79
                             IF Z=79 THEN PRINT CHR$(228)
IF Z=79 THEN 16470
16440
16450
16460
                          PRINT CHR#(228);
16470
                       HEXT 2
16400
                    RETURN
16499 Char_short: Char_min=12
16399 Char_max=64
                                           ! THIS ROUTINE CAN BE USED FOR SMALL TABLES
                          FOR Z=Char_min TO Char_max

IF Z=Char_min THEN PRINT TAB</r>
Char_min;

IF Z=Char_max THEN PRINT CHR$</228)
16518
16520
16538
                            IF Z=Char max THEH 16569
PRINT CHR#(228);
16548
16554
16568
                          NEXT Z
16570
                       RETURN
16580 Header_end_long: PRINT LIN(2)
                               GOSUB Char_long
16590
16600
                             RETURN
16610 Header_end_shor: PRINT LIN(2)
16620
                               GOSUB Char_short
16630
                             RETURN
16640
           SUBEND
16650 SUB Header_end
16669
           COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
COM F, Z3, Z4, Norm, Thetai, Tdelta
16670
16688
           COM Dates, Plots, Familys, Charts, Mains, Mainls, Flags, Y_hards
16698
16700
           INTEGER 2, Charmin, Charmax the final bottom line of a table. Sub header above boraks the bottom lines on pages of tables while output is still being
16718
16728
16730
16740
             CALCULATED
16750
16760
           PRINT LIN(2)
16770
           FOR Z=0 TO 79
                IF Z=79 THEN PRINT CHR$(228) '
IF Z=79 THEN 16818
16788
16790
16000
             PRINT CHR#(228);
16810
           HEXT Z
16020 SUBEXIT
                                       ! THIS ROUTINE CAN BE USED TO FINISH A SMALL TABLE
16838 Short: Char_min=28
                                      ! TO USE, INSERT AN IF STATEMENT AFTER THE PRINT LIN
16848
                  Char_max=60
(2) ABOVE
                 FOR Z=Char_min TO Char_max
IF Z=Char_min THEN PRINT TAB(Char_min);
IF Z=Char_max THEN PRINT CHR#(228)
IF Z=Char_max THEN 16988
PRINT CHR#(228);
16850
16068
16870
16000
16090
16900
                  NEXT Z
16910
             SUBEXIT
16920 SUB Stuff
16930
           OPTION BASE 9
16940
16950
           COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rhoi, Trhoi, Rho2, Trho2
16960
           COM F, 23, 24, Norm, Thetai, Tdelta
           COM Dates, Plots, Familys, Charts, Hains, Hain18, Flags, Y_hards
16980
           COM Stuffs, Redraws, Digitizes, Ray_traces
COM INTEGER I, J, Y@ loop, Nray, Nray_thart, Nray_family, Nray_stuff
COM INTEGER Nray_trace, Nray_density, Add_ray, Nc, Ns, Nbeta, Flag
16990
17000
17020
           COM INTEGER Line_count, Line_max, N_increment, Hit_total, Pselect, Hpib COM INTEGER Family, Surf_no
17036
```

THE REAL PROPERTY.

```
17050
         CON REAL Theta_critical, Tol, N1, N2, N3, Belta ray, Y6, Ya, Yb, Aperture
17060
17878
         CON Y_bullet, Smax_family, Percent_image
17888
         CON XI(+), Y1(+), XC(+), X2(+), Y2(+), X2max(+), Y2max(+)
         COM Y3(+), Y4(+), Beta(+), S2(+), Xsurfmax(+), Ysurfmax(+)
17090
17100
17110
         CON Qa(+), Smax(+), Alpha2(+), Rho2(+), Hit(+)
17120
17130
              THIS ROUTINE COMPUTES 250 POINTS OF THE SURFACE CHOSEN IN FAMILY
17148
           THESE POINTS ARE THEN USED IN OTHER ROUTINES TO TRACE AN ARBITRARY NUMBER OF RAYS THROUGH THE DESIGN SURFACE
17130
17160
17170
17180
17190
         DEG
17280
            IF Y2max(Family)=Y1(Family) THEN Yb=Y1(Family)
17210
            IF Y2max(Family)=Y1(Family) THEN Initialize
17220
17230
       Yb: Bsm=Y2max(Family)-X2max(Family)+Trho1 ! COMPUTE THE UPPER LIMIT
           XI=Bsm/(Talpha-Trhol) ! OF THE APERTURE. THIS IS AN ESTIMATE FOR Yb=Y1=X1=Talpha ! THE APERTURE MAY CHANGE IN THE FINAL DESIGN Aperture=Yb-Ya ! THE ESTIMATE IS REQUIRED TO CALCULATE DELY BELOH
17240
17258
17260
17270 Initialize: IF (Redraus="Y") OR (Redraus="y") THEN Redrau! INDICATES
                      Ya=Y1(Family)
17288
17298
                      Aperture=Yb-Ya
                      YO min=Ya=(Talpha=Trhoi)/Talpha ! REDRAW TO ANOTHER SCALE
YO max=Yb+(Talpha=Trhoi)/Talpha
17300
17310
17320
                      NEW STUFF = 250 INPUT "HOW MANY RAYS DO YOU WANT TO DRAW THE SURFACE WITH ( DE
17330
FRULT = 250 MAX> ?", Nray_stuff
                        IF Ya=0 THEN Add_ray=0
IF Ya<>0 THEN Add_ray=1
17340
17350
17360
                      Xnray=Nray_stuff
                                                      ! AVOIDS MIXED MODE ARITHMETIC
                      Dely=(YO max-YO min)/Xnray
YO min=YO min-Dely
IF Ya=O THEN YO min=YO min+Dely
17370
17388
17390
17400
                      Hray_stuff=Hray_stuff+Add_ray
17410
                      Flag=0
17428
                      Mesa
17430
                      X2(Na)=0
17448
                      Y2(Na)=8
17450
                      Beta(Ns)=0
17468 Start: Stuffs="Y
               FOR I=1 TO Nray_stuff
17478
                                             I COMPUTE THE COORDINATES OF THE INTERCEPT
17488
                  Flag=6
                                              ! OF THE INCIDENT RAY AND THE FIRST SURFACE
17490
                  X=6
                  Rho=Rho_initial
Trho=TAN(Rho)
17500
17510
17520
                  Y=Y@_min+Dely+I
17530
                  Hs=Ns+1
17540
                  YI(Ns)=Y
17558
                    CALL X1pos(X,Y)
17568
                  X1(Ns)=X
17570 Next_1: NEXT I
17586
                 DEEP
17590
                 Y8="H"
                 INPUT "BO YOU WANT A HARD COPY OF THE COMPUTED DATA ? Y/N",YS

IF (YS="Y") OR (YS="y") THEN GOSUB Yhard
17600
17610
17620
                   CALL Chart
17630
                 BEEP
17640
                 Y$="N"
17656
                 INPUT "DO YOU HANT A HARD COPY OF THE CHART ? Y/N",Y$
17668
                   IF (Ys="Y") OR (Ys="y") THEN GOSUS Dump_it
17470
                 Yes-Me
                INPUT "BO YOU WANT A HARD COPY OF THE COMPUTED DATA ? Y/N",YS IF (YS="Y") OR (YS="y") THEN GOSUB YHARD
17600
17698
17700
                   CALL Family
```

```
17710
                   Stuffs="H"
17720
                SUBEXIT
17730 Redrau: $tuff#="Y"
                     CALL Plot
LINE TYPE &
17740
17750
                     MOVE 9,6
DRAM Y_bullet/Talpha,Y_bullet
DRAM 100,Y_bullet
MOVE X2(1),Y2(1)
17760
17778
17798
17800
                      LINE TYPE I
                   FOR I=2 TO Nray stuff
BRAM X2(I), Y2(I)
17818
17830
                   NEXT I
17848
                     HOVE X2(1-1), Y2(1-1)
17850
                   LORG 2
17860
                   LABEL USING 17879; Family
17879
                   IHAGE K
                Redraus="H"
17880
17898
                F1 ag=3
17900
                  CALL Graph
17910
               SUBEXIT
17928 Dump_it: PRINTER IS 8
                    PRINT CHR#(27)4"4188T"
17930
17940
                     DUMP GRAPHICS
                     PRINT CHR#(27)&"&136T"
17950
17968
                    PRINTER IS 16
                  RETURN
17986
        Yhard: Flags="1"
17990
                  PRINTER IS 0
15000
               RETURN
18610
              SUBEXIT
18828 SUB Binary search(X,Y)
18838 OPTION BASE 8
18040
           COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rhoi, Trhoi, Rho2, Trho2
COM F, 23, 24, Norm, Thetai, Tdelta
COM Bates, Plots, Familys, Charts, Mains, Mainis, Flags, Y_hards
18656
18060
18070
18000
18090
           COM Stuffs, Redraws, Digitizes, Ray_traces
COM INTEGER I, J, Y8_loop, Wray, Wray_thant, Wray_family, Wray_stuff
COM INTEGER Wray_trace, Wray_density, Add_ray, Nc, Ns, Nbeta, Flag
12100
18118
10120
           COM INTEGER Line_count, Line_max, N_increment, Hit_total, Pselect, Hpib
COM INTEGER Family, Surf_no
COM REAL Theta_critical, Tol, N1, N2, N3, Delta_ray, Y8, Ya, Yb, Apenture
10130
18140
18150
10160
           CON Y_bullet,Smax_family,Percent_image
CON XI(+),Y1(+),XC(+),X2(+),Y2(+),X2max(+),Y2max(+)
18170
10100
           CON Y3(+), Y4(+), Beta(+), $2(+), Xsurfmax(+), Ysurfmax(+)
18200
           COM Ga(+), Smax(+), Alpha2(+), Rho2(+), Hit(+)
18216
18220
19230
                 THIS ROUTINE FINDS THE INTERCEPT OF THE RAY WITH THE FOLLOWING:
18240
10250
10260
                        1) FIRST SURFACE
18278
                        2) SECOND SURFACE
18288
                        3> FIRST IMAGE PLANE
10270
                        4) SECOND IMAGE PLANE
19300
10310
10320 DEG
18338 DEF FNA(X,Y)=X-Y/Trho2
 18348 DEF FHA!(X,Y)=X-Y/Talpha
                                                    ! FINDS THE INTERCEPT OF THE RAY AND Y=-Y_B
18350 DEF FNXn(A)=A-Y_bulles/Trhol
ULLET
19360
                                       ! RHO2 MUST BE DECLARED ELSENHERE
           Trhe2=TAN(Rhe2)
```

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```
IF Surf_no=4 THEN Four Xc(Y0_1oop)=FNA(X,Y)
18370
18388
                                               ! FIND THE X-INTERCEPT OF RHO2
18390 Three: Dy=(Z3-X)+Trho2
10400
                 Y=Y+By
18418
                 X=Z3
18420
              SUBEXIT
18438 Four: By=(Z4-X)+Trho2
18440
                Y=Y+By
18458
                X=24
18468
             SUBEXIT
18478 SUB Graph
18480
          OPTION BASE &
18498
18500
          COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trhoi, Rho2, Trho2
COM F, Z3, Z4, Norm, Thetai, Tdelta
18510
18520
          COM Dates, Plots, Familys, Charts, Mains, Main18, Flags, Y_hards
19530
18546
          COM Stuffs, Redraws, Digitizes, Ray_traces
          COM INTEGER 1, J, Y0 loop, Nray, Nray chart, Nray family, Nray stuff COM INTEGER Nray trace, Nray density, Add_ray, Nc, Ns, Nbeta, Flag
18550
18568
19570
          COM INTEGER Line count, Line max, N_increment, Hit_total, Pselect, Hpib COM INTEGER Family, Surf_no COM REAL Theta_critical, Tol, N1, N2, N3, Delta_ray, Y8, Ya, Yb, Apenture
18588
18598
18688
18610
18620
          COM Y_bullet,Smax_family,Percent_image
COM X1(*),Y1(*),Xc(*),X2(*),Y2(*),X2max(*),Y2max(*)
18638
18640
          COM Y3(+), Y4(+), Beta(+), S2(+), Xsurfmax(+), Ysurfmax(+)
10650
          COM Qa(+), Smax(+), Alpha2(+), Rho2(+), Hit(+)
18678
18688
                 THIS ROUTINE DRAWS THE GLM FOR STUFF AND RAY_TRACE SUBROUTINES
19690
            AND DIGITIZES THE IMAGE PLANE POSITION (23)
18790
18718
18729 DEG
         IF Flag=3 THEN Hait1
18738
18740
          IF (Digitize$="Y") OR (Digitize$="y") THEN Digit
18750 Drau_axes:
                          CALL Plot
18768 First_surf: FIXED 2
18778
                       LINE TYPE 8
18780
                          HOVE 0,0
                       X=Y_bullet/Talpha
DRAW X,Y_bullet
DRAW 166,Y_bullet
10790
19860
18010
18820
                          HOVE 8,0
                       DRAW X,-Y_bullet
DRAW 100,-Y_bullet
18036
18848
                MOVE X2(1), Y2(1)
FOR I=2 TO Nray_stuff
DRAW X2(1), Y2(1)
18858 X2pos:
18868
19979
10000
                NEXT I
18898 X2neg:
                   MOVE X2(1),-Y2(1)
                FOR 1=2 TO Neap_stuff
BRAN X2(1), -Y2(1)
18910
                 NEXT !
18920
18938
                EXIT GRAPHICS
10940
                 YS="N"
18950
                 INPUT "DO YOU WANT A HARD COPY OF THE PLOT WITHOUT RAYS ? Y/N", YS
18948
                   IF (Y=="Y") OR (Y=="y") THEN GOSUB Dump_it
18978
                GRAPHICS
18700
                   IF (Redraws="Y") OR (Redraws="y") THEN Second_image
18998
               image: LINE TYPE 5
19000 HOVE 23,7 bullet
19010 BRAN 23,-7 bullet
19020 Second image: LINE TYPE 6
```

```
19839
                          MOVE Z4,Y bullet
                        DRAW Z4, -Y_bullet
19040
19858 REM DRAW THE RAYS
        IF (Ray_traces="Y") OR (Ray_traces="y") THEN Nray_graph=Nray_trace
IF (Stuffs="Y") OR (Stuffs="y") THEN Nray_graph=Nray_stuff
19070
19000 First_: LINE TYPE 1
                CLIP 0,100,-Y_bullet,Y_bullet
FOR I=1 TO Nray_graph
MOVE 0,Y1(I)
19898
19100
19110
19120
                   DRAW X1(I),Y1(I)
19130
                HEXT I
19148 Second: FOR I=1 TO Nray graph
19158 MOVE X1(I),Y1(I)
19168 DRAW X2(I),Y2(I)
19170
                 NEXT I
DRAH 23, Y3(1)
19200
                         NEXT I
19210
19220 Decision: HAIT 2006
19230
                   EXIT GRAPHICS
19240
                   BEEP
19250
                   YS="N"
                   INPUT "DO YOU WANT TO PLOT TO THE SECOND IMAGE PLANE ? YAN", YS
19260
19270
                   GRAPHICS
19288 IF (Ys="N") OR (Ys="n") THEN Wait1
19298 Second_image_p: FOR I=1 TO Nray_graph
19388 HOVE 23,Y3(T)
                             DRAH Z4, Y4(1)
19310
                          HEXT I
19320
19330 Hait1: BEEP
                     ! THIS ROUTINE PRESENTS THE PLOT TO THE OPERATOR
               WAIT 250 ! IF A NOTE TO THE OPERATOR IS DESIRED, ENTER SETGU, LORG 2
DEEP ! MOVE 2,2,CSIZE 2.5,LABEL "PRESS CONT",CSIZE 15/4.54,
19340
19350
19360
               PAUSE
                           ! SETUU AFTER THE SECOND BEEP
19370
               EXIT GRAPHICS
                  IF (Flag=6) OR (Flag=3) THEN EXIT GRAPHICS
19388
19390
             SUBEXIT
19400 Digit: GRAPHICS
                                             ! THIS ROUTINE CHANGES THE ANALOG POSITION
                                             OF THE IMAGE PLANE ON THE GRAPHICS DEVICE TO DIGITAL DATA FOR PROCESSING
               POINTER F, 8
19418
               DIGITIZE Z3,Y
19428
19439
               LINE TYPE 5
               MOVE Z3, Y bullet
BRAN Z3, -Y bullet
19448
19458
19460
               SETGU
19470
               LDIR 0
17480
               LINE TYPE 1
               LORG 5
19490
19500
               CSIZE 2.5
                                       ! CHANGE IN LAXES AS HELL
19510
               Centerx=72.5
19520
                  HQVE 1.5*Centerx,2
19530
                LABEL USING 19540; 23
19540
               IMAGE "Image Plane : ", DD. DD, " inch"
19550
               SETUU
19560
               CRIZE 15/4.54
19579
               HAIT 2506
EXIT GRAPHICS
19500
19590
             SUBEXIT
19600 Bump_it: PRINTER IS 0
                  PRINT CHR$(27)&"&190T"
19610
19620
                  DUMP GRAPHICS
19630
                  PRINT CHR$(27)4"&136T"
19640
                  PRINTER IS 16
19650
               RETURN
19660
             SUBEHD
19678 SUB X1neg(X,Y)
17680
       · OPTION BASE 0
19690
```

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19788
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trhoi, Rho2, F, Z3, Z4
19718
19720 DEG
19738 Alphan=-1#Alpha
19749 Talphan=TRN(Alphan)
19758 DEF FNY1(Y)=Y+Talphan/(Talphan-Trho) ! FINDS THE Y-VALUE OF THE INTERCEPT
                                                    ! OF THE RAY AND THE FIRST SURFACE
19760
19778 DEF FNX1(Y)=Y/Talphan
                                    ! FINDS THE X-VALUE OF THE INTERCEPT OF THE RAY
                                    I AND THE FIRST SURFACE
19780
19790
            Y=FNY1(Y)
19800 Hoops:X=FNX1(Y)
19810 SUBEND
19826 SUB Density
19838
         OPTION BASE 0
19848
19858
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Rho1, Trho1, Rho2, Trho2
19868
         COM F, 23, 24, Norm, Thetai, Tdelta
19870
          COM Dates, Plots, Familys, Charts, Mains, Main1s, Flags, Y_hards
19880
         COM Stuffs, Redraws, Digitizes, Ray_traces
COM INTEGER I, J, Y0_loop, Nray, Nray_chart, Nray_family, Nray_stuff
COM INTEGER Nray_trace, Nray_density, Add_ray, Nc, Ns, Nbeta, Flag
19898
19988
19910
19928
         COM INTEGER Line_count, Line_max, N_increment, Hit_total, Pselect, Hpib
COM INTEGER Family, Surf_no
COM REAL Theta_critical, Tol, Hi, N2, N3, Delta_ray, Y0, Ya, Yb, Aperture
19930
19940
19950
19968
         COM Y_bullet,Smax_family,Percent_image
COM XI(+),Y1(+),XC(+),X2(+),Y2(+),X2max(+),Y2max(+)
19978
19986
19990
          COM Y3(+), Y4(+), Beta(+), S2(+), Xsurfmax(+), Ysurfmax(+)
20000
20010
          COH Qa(+), Smax(+), Alpha2(+), Rho2(+), Hit(+)
20020
20030
          INTEGER Inc, K, L, M, Lines
28848
20050
          DEG
20060
            THIS ROUTINE COMPUTES THE RAY DENSITY IN ONE DIMENSION.
20070
            ASSUMPTIONS:
20060
                 1) THE POINT OF MAXIMUM RAY DENSITY HAS BEEN FOUND VIA A
20090
                     DIGITIZE STATEMENT.
20100
                 2) THE VALUES OF Y3 HAVE NOT BEEN CHANGED TO REFLECT THE
20110
                     NEW VALUE OF Z3
20120
20130
         PRINTER IS 16
20140 Nray_density=Nray_stuff
20150 Re_draw: FOR I=1 TO Nray_density
                                                          ! RECOMPUTE THE VALUE OF Y3
20168
                     A=Xc(I)
20170
                     XeX2(I)
                     Y=Y2(I)
20180
20190
                     Rho2=Rho2(I)
20200
                     Trho2=TAN(Rho2)
20210 Same:
                     Beltay=(Z3-X)+Trho2
20220
                     Y3=Y+Deltay
20230
                     Y3(1)=Y3
                     De1tay=(Z4-Z3)+Trho2
20240
20250
                     Y4(1)=Y3(1)+Beltay
20260 Next_1: NEXT I
20270 Hit_zero: MAT
                     MAT Hit=ZER(2001)
                                                                                ! ZERO THE ARRAY
                                                     ! FIND THE No. OF HITS IN THE INTERVAL
20200
                    Inc=0
                    Ylast=-Y bullet
Belta=Y bullet/N increment
Ynext=Ylast+Belta/2
                                                     ! [-Y_BULLET, -Y_BULLET+DELTA/2]
20290
20300
20310
20320
                    Hit(Inc)=0
                    FOR I=1 TO Nray density
IF (Y3(I)>=Ylast) AND (Y3(I)(Ynext) THEN Hit(Inc)=Hit(Inc)+1
20330
20340
                   HEXT I
20350
                                                     ! FIND THE No. OF HITS IN THE INTERVAL
20360 Hit_middle:
```

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20379
                                               ! [-Y_bullet+DELTA/2, Y_bullet-DELTA/2)
20380
                    FOR L=1 TO 2*N_increment-1
20390
                      Inc=Inc+i
20480
                       Hit(Inc)=8
20410
                       Ylast=Ynext
20420
                       Ynext=Ylast+Delta
20430
                         FOR I=1 TO Nray_density
20448
                           IF (Y3(1)>=Y1ast) AND (Y3(1)(Ynext) THEN Hit(Inc)=Hit(In
c)+1
2845B
                         NEXT I
28460
                      NEXT L
20470 Hit_last: Inc=2*N_increment
                                          ! FIND THE No. OF HITS IN THE LAST INTERVAL
20480
                  Hit (Inc)=0
                                             [Y_bullet-DELTA/2, Y_bullet]
                  Ylast=Y_bullet=Delta/2
Ynext=Y_bullet
FOR I=1 TO Nray_density
20490
20500
29518
20520
                    IF (Y3(I)>=Ylast) AND (Y3(I)(=Ynext) THEN Hit(Inc)=Hit(Inc)+1
20530
                  NEXT I
      Normalize: Hit_total=0 ! NORMALIZE THE FOR I=0 TO 2*H_increment ! IMAGE PLANE Hit_total=Hit_total+Hit(I) ! No. OF HITS NEXT I
20540
                                                     ! NORMALIZE THE No. OF HITS ON THE
29538
                                                      IMAGE PLANE (23) TO THE TOTAL
29569
28578
20588
                   IF Hit_total=0 THEN Hone FOR I=0 TO 2*N_increment
20590
20600
                     Hit(I)=Hit(I)/Hit_total
20618
20620
                   NEXT I
                   Pct=Hit_total/Nray_density
Percent_image=Pct+100
28638 None:
                                                         ! % OF RAYS THAT ARRIVE AT THE
29640
                                                          IMAGE PLANE
29659 Graph: CALL Plot
                                                         ! PLOT AND LABEL THE AXES
      IF Hit_total=0 THEN Label_
First_bar: Xlast=-Y_bullet
20668
28678
                                                         ! DRAW THE HISTOGRAM
                   Xnext=Xlast+Delta/2 ! INTERVAL t-Y_bullet, -Y_bullet+DELTA/2)
20688
20694
                   IF Hit(Inc)=0 THEN Middle bars
CLIP Xlast, Xnext, 9, Hit(Inc)
28799
26719
20720
                   FRAKE
29730
                   GOSUB Delt
20740 Middle_bars: FOR I=1 TO 2*N_increment-1
                                                       ! INTERVAL
28758
                                              ! (-Y_bullet+DELTA/2, Y_bullet-DELTA/2)
                       Inc=Inc+1
20768
                       Xlast=Xnext
20770
                       Xnext=X1ast+Delta
                         IF Hit(Inc)=0 THEN Next_im
20780
                       CLIP Xiast, Xnext, 0, Hit(Inc)
20790
20800
                       FRAME
20018
                       GOSUB Delt
20020 Next_i_n:
                     HEXT I
! INTERVAL [Y_bullet-BELTA/2, Y_bullet]
20000
                  FRAME
                  GOSUS Delt
20900 Label_: Bigitizes="H"
20910
               Flage3
20920
                  CALL Graph
20936
             SUBEXIT
20940 Delt: Lines=18
20950
             Belt=(Xnext-Xlast)/Lines
20960
             X=Xlast-Delt
20976
             FOR J=1 TO Lines
29900
               X=X+Belt
20990
                  HOVE X,0
21000
                  DRAW X. HIS (Inc)
21010
             HEXT J
21020
           RETURN
```

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```
21030 SUBEND
21040 SUB Min(Xm(+),X,INTEGER M)
21050 OPTION BASE 0
21060 !
21070 DIM Xm(M)
21080 !
21090 ! THIS ROUTINE FINDS THE MINIMUM ELEMENT IN A ONE DIMENSIONAL ARRAY
21100 !
21110 Y=Xm(0)
21120 FOR I=1 TO M
21130 X=Min(X,Xm(I))
21140 NEXT I
21150 SUBEND
21160 SUB Max(Xm(+),X,INTEGER M)
21170 OPTION BASE 0
21190 JIM Xm(M)
21200 !
21210 ! THIS ROUTINE FINDS THE MAXIMUM ELEMENT IN A ONE DIMENSIONAL ARRAY
21220 !
21210 X=Xm(0)
21240 FOR I=1 TO M
21250 X=Mm(X(X,Xm(I))
21260 NEXT I
21270 SUBEND
```

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## APPENDIX B

## TRACE PROGRAM DESCRIPTION AND PROGRAM LISTING

**(** )

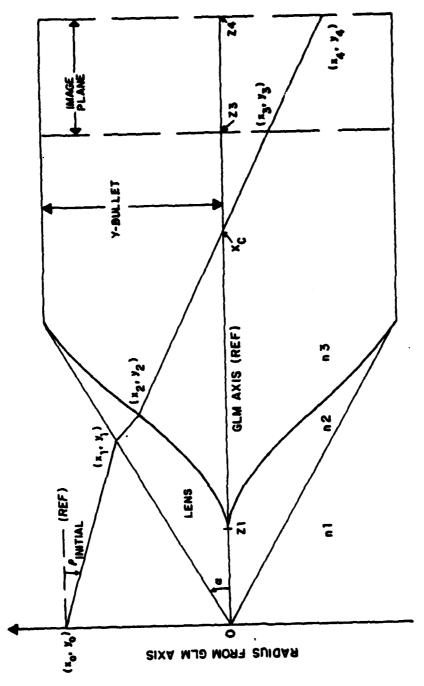
1

TRACE was the first program written for this thesis.

TRACE was written for the purpose of automating the task of drawing the ray diagram produced when tracing rays through a conical lens with various second surfaces. The program consists of a set of subroutines called from a control program which are designed to perform a specific task(s). A detailed description of each subroutine will not be given because TRACE has extensive documentation included within the program. However, an abbreviated discussion of the geometric relationships at the first and second surfaces and the bisection routine in subroutine BINARY SEARCH follows.

TRACE occupies approximately 145 Kbytes of memory which is approximately 77% of available memory (11). A listing of TRACE is at the end of this appendix.

TRACE was designed to calculate the trajectory of up to 250 rays incident upon the first surface in the upper half-plane as illustrated in figure B-1. All of the parameters shown in figure B-1 are provided by the operator except Z4, the location of the permanent Image plane, which is set for Z4 = 50 inches. All of the parameter values provided by the operator have default values declared either in subroutine DIALOGUE, line number 13810 or the MAIN routine, line number 10.



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Figure B-1. Symbol Definition for the GLM.

TRACE calculates the complete trajectory of each ray before proceeding to the next ray. Each surface is assigned a number with the vertical axis, y, defined as the zeroth surface. All incident rays originate on the y-axis and are assumed to be parallel with the source at infinity. The first surface shown in figure B-2 encountered is the exterior of the conical spike which, in two dimensions, is a plane perpendicular to the meriodional plane, the paper, with a cone half-angle  $\alpha$ . The incident angle makes an angle of incidence  $\theta_{\rm I}$  with the first surface normal  $\hat{n}$  at point T according to

$$\theta_{I} = \frac{\pi}{2} \quad (\alpha + |\rho_{I}|)$$

Noting that  $\alpha = \alpha_2$ ,  $\rho_R = |NORM| - \theta_R$ ,  $NORM = \alpha_2 - \frac{\pi}{2}$  (B-1)

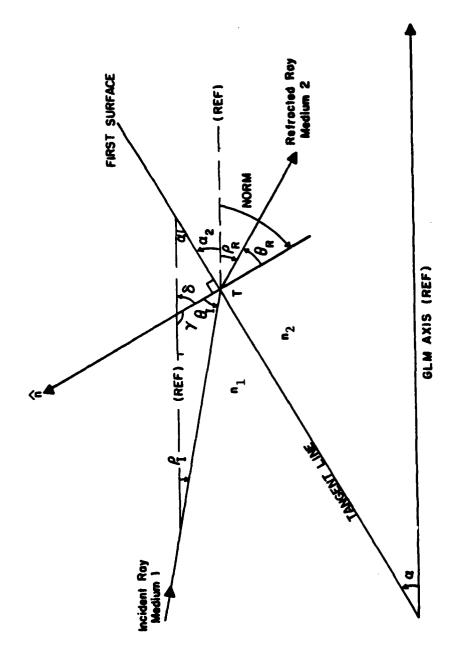
and applying Snell's Law  $\sin \theta_R = (n_1/n_2) \sin \theta_I$  (B-2) yields

$$\rho_{R} = \alpha_{2} + \theta_{R} - \frac{\pi}{2}$$

the ray angle in the lens referred to as  $\rho_1$  in chapter III and Appendix F. As the incident ray angle  $\rho_{\rm I}$  increases the angle of incidence  $\theta_{\rm I}$  decreases to zero when the incident causing  $\theta_{\rm I}$  to transition through the normal as shown in figure B-3, subroutine SNELL in TRACE detects this transition as a change in sign in  $\theta_{\rm I}$ . Snell's Law is defined with all arguments positive. Therefore the magnitude of  $\theta_{\rm I}$  is used to determine  $\theta_{\rm R}$  and thus  $\rho_{\rm R}$  according to  $\sin\theta_{\rm R} = (n_2/n_1)\sin\theta_{\rm I}$  yielding

$$\theta_{R} = \alpha_{2} + \theta_{R} - \frac{\pi}{2} \tag{B-3}$$

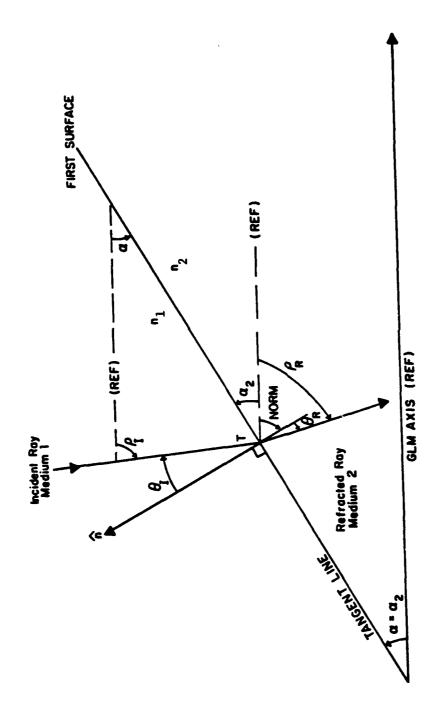
which is the same result for  $\theta_{\tau} > 0$ .



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Geometry and Symbol Definition for the Application of Snell's Law at the First Surface of the Conical Lens. Figure B-2.



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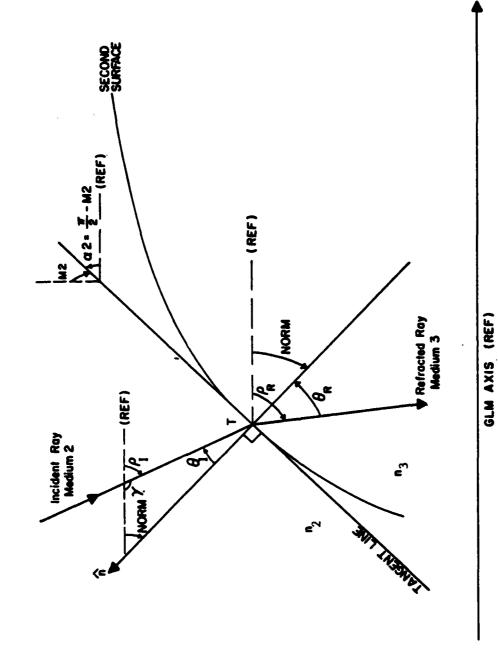
Geometry and Symbol Definition for the Application of Snell's Law at the First Surface of the Conical Lens for  $\theta_{\rm I}$  < 0. Figure B-3.

The application of Snell's Law at the second surface of the lens is very similar to the first surface. The geometry for  $\theta_{\text{I}}$  > 0 is shown in figure B-4 and for  $\theta_{\text{I}}$  < 0 in figure B-5. Some of the rays inside the lens may întercept the GLM axis at x < 21 and therefore may intercept the branch of the second surface in the lower half-plane. The geometry for this case is shown in figure B-6. A significant difference between rays intercepting the positive and negative branches of the second surface is the definition of the normal direction  $\hat{n}$ . In figures B-4 and B-5 the direction of  $\hat{n}$  is into the lens where in figure B-6, n is defined to be out of the lens. Practically, this contradiction in definition has no effect on TRACE because the angle of the normal used in applying Snell's Law has always been the acute angle as labeled in all of the figures. The direction of  $\hat{n}$  in figure B-6 was changed to reflect the change in sign of NORM.

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The search for and calculation of the intercept of the ray refracted at the first surface and the second surface is accomplished in subroutine BINARY SEARCH. The primary method used is the bisection method illustrated in figure B-7. The bisection method can only be applied where the ray in the lens is known to intercept the second surface of the lens. Examples of rays which do not intercept the second surface are shown in figures C-2, C-5 and C-10. The method used for the rays which do not intercept the second surface is discussed later.

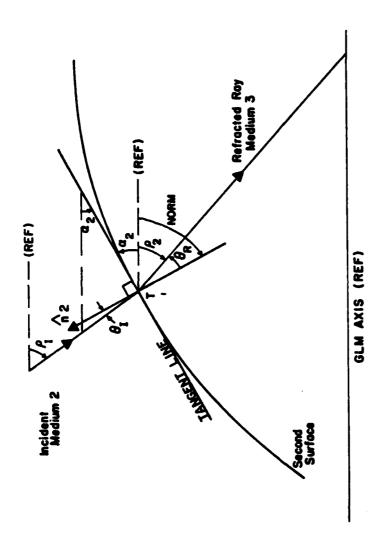


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Geometry and Symbol Definition for the Application of Snell's Law at the Positive Branch of the Second Surface of the Conical Lens. Figure B-4.

**のできるのでは、中での日本ののは間では、日本の中では、中でのできる。これでは、これでは、これでは、これでは、これのできる。** 



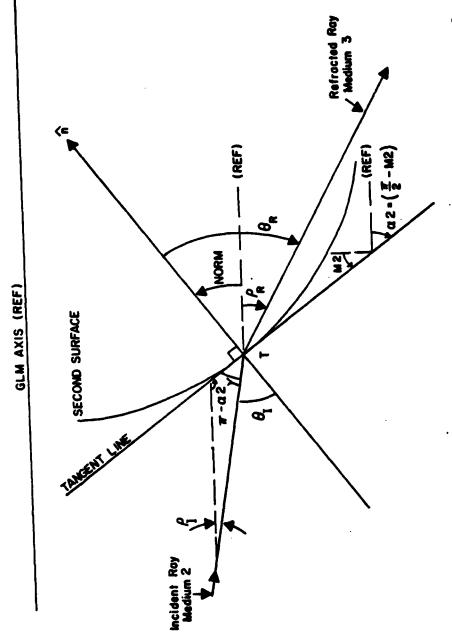
....

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()

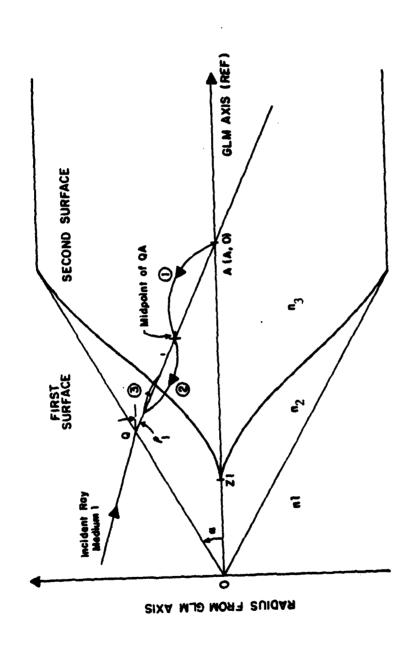
Geometry and Symbol Definition for the Application of Snell's Law at the Positive Branch of the Second Surface of the Conical Lens and  $\theta_{\rm I}$  < 0. Figure B-5.

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Geometry and Symbol Definition for the Application of Snell's Law at Negative Branch of the Second Surface of the Conical Lens. Figure B-6.



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Illustration of the Bisection Method Used in Subroutine BINARY SEARCH. Figure B-7.

The bisection method converges to the intercept value quickly, especially if the ray is nearly normal to the second surface. The sequence of events is depicted in figure B-7 by the circled numbers 1 , 2 , etc. Assuming  $\rho_1$  is known, the intercept of the GLM axis, A, of the ray in the lens is found. The first step in the bisection sequence, 1 is to find the midpoint of QA. The midpoint of QA, (x<sub>mid</sub>, y<sub>mid</sub>) is calculated under label Recurse p, line 7440 of TRACE. The midpoint is then compared to the value of the second surface at y=ymid. The midpoint in figure B-7 is behind the second surface. Step 2 finds one midpoint of the line segment from Q to the midpoint of QA. A comparison is again made with the second surface. Now, the present location is ahead of the second surface. Step 3 is executed and the location is again compared with the second surface. The process continues until the difference between the present location on the ray  $(x_{mid}, y_{mid})$  and the true value of the intercept  $(x_2, y_{mid}), |x_{mid}-x_2|$  is less than a specified tolerance, tol =  $10^{-5}$ . Once the intercept of the ray and the second surface has been found then go to label Done, line 8140, to define the (x, y) coordinates of the intercept. The xcoordinate is defined as the average of the present location on the ray,  $x_{mid}$ , and x2, the value of the second surface at Y=Ymid.

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The ray may pass ahead, shown by A < 21, of the second surface. The test for A < 21 is conducted in line 6860.

If the test is true a jump to line 7720 is performed. A test is conducted in line 7870 to determine if the ray intercepts the negative branch of the second surface. If the test is true then a jump to line 8080 is made to prepare to enter the bisection method for the negative branch, which is identical to the method for the positive branch described above. The test performed in line 7870 will not detect a ray that is just tangent to the second surface. The slow march method, lines 7840 to 8000, is employed to search and find the intercept (A, 0) and marches down the ray until the second surface intercept is found within the tolerance, or the wall of the GLM, y = -Y bullet is reached. If y = -Y bullet then the march is terminated and a jump to line 8250 via 8150 is made to exit the subroutine.

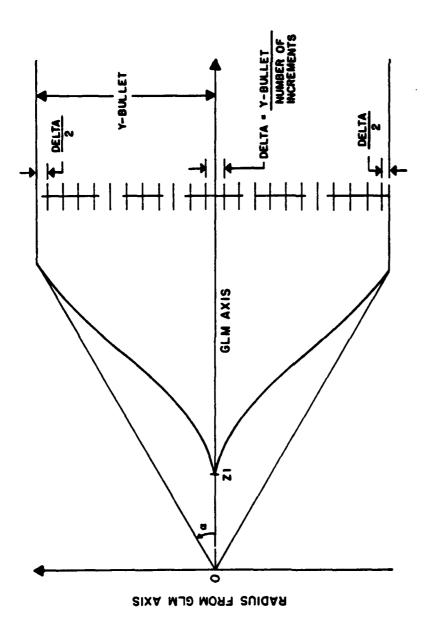
A special case exists when  $\theta_{\rm I}$  < 0. The ray in the lens could intercept the positive branch. A test is conducted in line 7010 to determine if the ray intercepts the positive branch. If the test is true a jump is made to line 7330 for entry into the bisection method. If the test fails then the marching method is used. The application of the marching method for this case is made from line 7100 to 7320.

Another special case exists when the polynomial used to describe the second surface causes the second surface to intercept the first surface at  $|y| < Y_{\rm bullet}$ . The test for this case is conducted in line 7370 for the positive branch and line 7770 for the negative branch. If the test

()

is true, then a jump is made to line 8280 and the subroutine is exited.

The "success" of a conical lens is whether light rays can be focused to a point. Success is determined two ways. first is the ray diagram; compare figures 14, 22, C-2, C-10 and C-16 for the ability of each lens to focus light rays. The second method is by a histogram of the ray distribution on the image plane. The desired histogram is a delta function at the origin as shown in figures 15 and 23. Undesirable histograms are shown in figures C-3, C-7, C-13, C-14 and C-17. The histogram is calculated by dividing the image plane in the upper half-plane into an even number of intervals equal to N increment. The division of the image plane is also performed in the lower half plane as shown in figure B-8. The intervals are arranged such that the GLM axis is straddled by the center interval, thus adding a half-interval to each extremity of the image plane. Hence, the total number of intervals is then 2\*N increment +1. The generation of the histogram is executed in subroutine DENSITY, line 17920. The algorithm checks each interval for an intercept of a ray with the image plane in lines 18440 to 18820, DENSITY then normalizes the distribution to the number of hits on the image plane, not the total number of rays in lines 18830 to 18930. The percentage of the rays striking the image plane is calculated in lines 18920 and 18930 and displayed to the operator by subroutine LAXES in lines 12870 and 12880. The



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Illustration of Dividing the Image Plane into a Set of N-Increment Intervals Used to Generate a Histogram of a Ray Diagram. Figure B-8.

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percentage label serves to remind the operator that the histogram represents the distribution of the rays actually striking the image plane within the boundaries of the GLM.

The subroutines in Table B-1 were copied or derived from the HP-9845B utilities library for use in TRACE.

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TABLE B-I
SUBROUTINES DERIVED FROM THE HP-9845B UTILITIES LIBRARY

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Name	Line No.
Main	18
Plot	10170
Laxes	11430
Dialogue	13810

# TRACE PROGRAM LISTING

1

```
18 NORMAL
20 PRINTER IS 16
38 PRINT PAGE
40 FIXED 2
58 PRINT **
68 PRINT "+
78 PRINT "#
                                                      TRACE
SO PRINT ".
90 PRINT
100 DISP "THIS IS TRACE"
110 HAIT 1500
120 Main: OPTION BASE 0
130
140
        COM INTEGER I, J, Curve, Np, Nn, N, Nr, REAL Aneg(17), Apos(17), A(17), Z1, Z3, Z4
       COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2
COM N1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
150
160
170
180
        COM INTEGER Y0_loop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_total
198
        COM INTEGER Linecount, Linemax
200
        COM INTEGER Pselect, Hpib
218
228
        COM REAL Nmin, Nmax, RO_max
       COM Ray traces, Digitizes, Grins, Gs, Grincs, Plots, Dates
COM X(1250), Y(1250), Xc(250), N(250), R(250)
238
248
250
268
       COM Rho(750), Phi(250), C(250), Y3(250), Hit(2001)
278
280
        INTEGER Zz, Char_max
290
        DISP
        OVERLAP
300
                                 ! SEE THE 9845 OPERATING AND PROGRAMMING MANUAL
310
        CALL Dialogue
320
       DEG
338 Comments:
                        FLAGS ARE USED THROUGHOUT THE PROGRAM TO INDICATE VARIOUS
                     CONDITIONS WHICH INFLUENCE THE BEHAVIOR AND TREATMENT OF THE LIGHT RAY AS IT PASSES THROUGH THE LENS SYSTEM. THE EXPLANATION OF FLAGS USED IN THE GENERATION OF THE RAY DIAGRAMS
340
350
368
378
                     AND THE DECLARATION LOCATION IS GIVEN BELOW:
388
                       FLAG:
1> 8 => DECLARED IN MAIN AND BINARY SEARCH
398
400
418
                                      RESET CONDITION
420
                            2) 1 => DECLARED IN BINARY SEARCH
438
                                      RAY INTERCEPTS THE NEGATIVE BRANCH
440
                            3> 5 => DECLARED IN SHELL
                            Theta I < 0 DEGREES
4) 10 => DECLARED IN SNELL
460
478
                                        TOTAL INTERNAL REFLECTION
480
                            5) 15 => DECLARE IN SNELL
                                       THE RAY LEAVES THE SECOND SURFACE WITH ABS(RHO) > 98 DEGREES (THE RAY HILL NOT INTERCEP
498
500
519
                                       THE IMAGE PLANE
                           6) 28 => DECLARED IN BINARY SEARCH
THE RAY MISSES BOTH THE POSITIVE AND NEGATIVE
BRANCHES FOR ThetaI > OR < 9 DEGREES
7) 38 => DECLARED IN BINARY SEARCH
529
538
540
550
560
                                        THE SECOND SURFACE BENDS AROUND AND CROSSES THE
570
                                        FIRST SURFACE
580
590
600
                       \frac{\text{F1ag2}}{\text{1}}: \frac{\text{9}}{\text{9}} => Declared in Main and Binary Search
610
629
                                      RESET CONDITION
630
640
                            2> 1 => DECLARED IN BINARY SEARCH
                                      THE RAY INTERCEPTS THE NEGATIVE BRANCH
650
                     NOTE: THESE ARE NOT ALL OF THE FLAGS, JUST THE ONES AFFECTING
440
```

```
678
                           RAYS.
688
698 Gymnastics:
                      Y_hard#="H"
788
                      Fīag2#="1"
                      INPUT "DO TOU WANT A HARD COPY OF THE COMPUTED DATA? Y/N", Y_ha
710
rd#
                        IF (Y_hards="N") OR (Y_hards="n") THEN f1ag2$=$6 GOSUB Yhard
728
730
                        GOSUB Printer
749
                      REEP
750
760
                      PAUSE
                        IF (G$="Y") OR (G$="y") THEN GOSUB Header_grin
IF (G$="Y") OR (G$="y") THEN Initialize_run
778
780
                        hards="H"
798
                      INPUT "DO YOU HANT A HARD COPY OF THE COEFICIENTS PRINTED ? Y/
808
N", Y_hard$
                        IF (Y_hards="N") OR (Y_hards="n") THEN 1808 GOSUB Yhard
818
929
                     GOSUB Header_coef
FOR I=0 TO Np
IF Linecount>Linemax THEN GOSUB Header_coef
839
848
850
868
                        PRINT USING Image_p; I, Apos(I)
870
                        Linecount=Linecount+1
                      NEXT I
IF Linecount>Linemax THEN GOSUB Header_coef
AAA
898
988
918
                      Linecount=Linecount+1
920
                      FOR I=0 TO Nn
                        IF Linecount>Linemax THEN GOSUB Header_coef
938
                        PRINT USING Image_n; I, Aneg(I)
940
958
                        Linecount=Linecount+1
                     . NEXT I
968
                      IMAGE 25%, "Apos("DD") = ",K
IMAGE 25%, "Aneg("DD") = ",K
978 [mage_p:
980 [mage_n:
                      GOSUB Header coef end
PRINT LIN(2), "PRESS CONT"
990
1000
1010
                      PAUSE
                        IF Flag2#="1" THEN Y_hard#="Y"
1929
                        GOSUB Yhard
GOSUB Header
1838
1040
1959 Initialize_run:Surf_no=0
1969 Z1=Apos(0)
                          IF (G$="Y") OR (G$="y") THEN Z3=15
1878
1686
                        Y8_min=Ya+(Talpha-Trhoi)/Talpha
                        Y8_max=Yb+(Talpha-Trhoi)/Talpha
1098
1100
                        Xnray=Nray
                                           ! TO KEEP FROM USIN MIXED MODE ARITHMETIC
                        Dely=(Y0_max-Y0_min)/Xnray
Y0_min=Y0_min=Dely
IF Ya=0 THEN Y0_min=Y0_min+Dely
1110
1120
1130
                        1140
1150
1160
                        Nr=-1
                        Xc(8)=0
1170
1180
                        H(8)=8
1190
                        Phi(8)=8
                        C(0)=0
1290
1218 Y9_100p:
                  FOR YO_100p=1 TO Nray
                                                  ! RESET FLAG
1220
                  F1ag=0
1230
                  F1 ag_2=0
1240
                  X=0
                  Rho=Rho_initial
Trho=TAN(Rho)
1250
1268
                  Xy@_loop=Y@_loop
Y=Y@_min+Dely#Xy@_loop
1270
1280
                  NasHa+1
1290
1306
                  Hr#Nr+1
```

and free

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X(Ns)=X

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1329
                 Y(Na)=Y
1338
                 Rha(Nr)=Rha
1340 One: Surf_no=1
1350
           Hs=Hs+L
1360
           Hr=Hr+1
1370
             CALL Binary_search(X,Y)
1388
           X(Ns)=X
1390
           Y(Ns)=Y
1400
             CALL Smell(X,Y)
1418
           Rho(Nr)=Rho
             IF (Gs="Y") OR (Gs="y") THEN Phi(Y0_1oop)=Phi
1420
1430
     Two: Surf_no=2
1448
           Ha=Hs+1
1450
           Hr=Hr+1
1460
             CALL Binary_search(X,Y)
           X(Ns)=X
1488
           Y(Ns)=Y
1490
             IF (Gs="Y") OR (Gs="y") THEN Blind
             IF Flag=28 THEN Blind
IF Flag=38 THEN Flag_38
1500
1510
             CALL Snell(X,Y)
1528
1539
           Rho(Nr)=Rho
1548 Flag_15: IF Flag<>15 THEN Flag_18
               GOTO Blind
IF Flag(>10 THEN Three
1550
1560 Flag_18:
                                                ! FLAG_30 WHEN FIXED
1578
                Xc (Y@_1oop)=0
1580
                Rho(Nr)=6
1598
                GOTO Blind
                    IF Flag<>30 THEN Three
1600 Flag_30:
                Xc(Y0_100p)=0
1619
1620
                Rha(Nr)=8
                GOTO Blind
1630
1640 Three: Surf_no=3
                            ! FIRST (MOVABLE) IMAGE PLANE
1650
             Hs=Hs+1
                CALL Binary_search(X,Y)
1678
              X(Ns)=X
1689
              Y(Ns)=Y
1698 Four: Surf_no=4
            H==H=+1
1700
               CALL Binary_search(X,Y)
1719
1728
            X(Ns)=X
1730
            Y(Ns)=Y
            1740
1750 Blind: Ns=Ns+1
1769
              X(Ns)=8
                          ! AND WAS NOT REFRACTED
              Y(N4)=9
1788
              Hs=Ns+1
              X(Ns)=0
1800
              Y(Ns)=0
1818 Next_y8_100p: FIXED 2
1829
                      Nsp=Ns-1
                        IF (Gs="Y") OR (Gs="y") THEN Print_grin
1830
1848
                        IF Linecount >Linemax THEH GOSUB Header
1858 PRINT USING Image_data;X(Nsp-3);Y(Nsp-3);X(Nsp-2);Y(Nsp-2);X(Nsp-1);Y(Nsp-1);X(Y6_1op);8;X(Nsp);Y(Nsp);Rho
1860
                     Linecount=Linecount+1
1870
                      GOTO Continue
1888 Print_grin: IF Linecount>Linemax THEN GOSUB Header_grin
1898 PRINT_USING Image_data_g;X(Nsp-3);Y(Nsp-2);Y(Nsp-2);X(Nsp-1);Y(Nsp-1);X(Y@_loop);Rho
1898 Inaccustations (NSP-1);X(Y@_loop);Rho
                   Linecount=Linecount+1
1900
1918 Continue: NEXT YE_loop
1920
1930
1940 | Image_data: | IMAGE_X<2<0.DD,X,DD.DD,3X>,DD.DD,X,DD.DD,1X,6D.DD,X,D.DD,3X,3D.DD,X,40.DD,3X,40.DD
1950 | Image_data: IMAGE D,2x,DD.DD,3x,DD.DD,2x,DD.DD,3x,DD.DD,2x,DDD.DD,3x,5D.2
```

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D,2x,D,3x,DD.DD,2x,5B.DD,3x,4D.DD \cdot! USE THIS FOR Y_BULLET \geq 10 INCHES
1968
1970 Image_data_g: IMAGE 7X(2(D.DD,XD.DD,3X),DD.DD,X,DD.DD,3X,3D.DD,X,D.DD,3X,DD
.DD,3x,4D.DD)
1986
1998
                 GOSUB Header_end
GOSUB Yhard_end
PRINT LIN(2),"FINISHED"
2888
2010
2020
2030
                 BEEP
                 HAIT 250
2948
2050
                 DEEP
2060
                   IF (G$="Y") OR (G$="y") THEN Graph_grin
2978
                  traces="H"
              INPUT "DO YOU HANT TO PLOT THE RESULTS OF THE TRACE ? Y/N", Ray_trace
2080
             IF (Ray traces="N") OR (Ray traces="n") THEN Rerun INPUT "ON WHICH DEVICE: CRT (C) OR THE 9872 (P) ? P/C",Plots IF (Plots="C") OR (Plots="c") THEN Graph
2098
2100
2118
              INPUT "PLEASE ENTER THE SELECT CODE OF THE GRAPHICS DEVICE (DEFAULT
2128
      .Pselect
= 7 )
2130
              INPUT "PLEASE ENTER THE HPIB ADDRESS OF THE GRAPHICS DEVICE (DEFAULT
 = 5 )", Hpib
2148 Graph:
                CALL Graph
2150
              Y$="N"
              INPUT "DO YOU WANT ANOTHER PLOT DRAWN TO A DIFFERENT SCALE ? Y/N", YS
2160
2170
                IF (Y$="Y") OR (Y$="y") THEN Graph
2186 Bensity: PRINTER IS 16
2198
                PRINT PAGE," The point of maximum ray density is determined by yo
u visually."
2288
                PRINT "by placing the cross-hairs (they will appear automatically)
221A
                PRINT "over the position of maximum density."
                PRINT .
                           This is accomplished by using the DISPLAY controls (up
2228
 down. <-, ->>.
                PRINT "When you get cursor in the area of interest, use the SHIFT
2238
 button"
2248
                PRINT "with the DISPLAY controls (both shift and display control
2250
                PRINT "should be depressed simultaneously) for fine positioing."
2260
                PRINT LIN(2),"
                                   The position of the vertical hair is critical,
                PRINT "because its location is used for the position of the "
2270
                PRINT "image plane (23) on the GLM axis."
PRINT LIN(2), "CRUTION : Bo not let the image plane intercept any
2289
2290
 rays"
2300
                PRINT "in the interior of the lens. If this is done, those rays"
                PRINT "will be included in the histogram."
2319
                PRINT "PRESS CONT"
2328
2336
                PAUSE
                PRINT PAGE."
2340
                                 The histogram is an illustration of the density"
2350
                PRINT "of the rays that intercept the image plane versus radial "
                PRINT "distance from the GLM axis."
2360
2370
                PRINT LIN(2),"
                                   When the position has been located, PRESS CONT."
2380
                PAUSE
2390
                Digitize#="Y"
2400
                  CALL Graph
2410
                  IF Plot#="P" THEN 2468 ! P FOR HP-9872 PLOTTER
                Dump_crts="N"
INPUT "BO YOU MANT A MARD COPY OF THE PLOT ? Y/N", Dump_crts
IF (Dump_crts="Y") OR (Dump_crts="y") THEN GOSUB Printer
DISP "MORKIN' ON THE HISTOGRAM..."
2428
2430
2448
2450
                                        ! PRODUSE A HISTOGRAM OF THE RAY DENSITY
                  CALL Bensity
2468
                  IF Plots="P" THEN 2528
2470
2480
                Digitize#="N"
                                  . RESET CONDITION
                Dump_crts="N"
INPUT "DO YOU WANT A HARD COPY OF HISTOGRAM ? Y/N",Dump_crts
2490
2500
```

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2518
                     IF (Bump_crts="Y") OR (Bump_crts="y") THEN GOSUB Printer
2529
                  Y#="H
2530
                  INPUT "DO YOU WANT TO REDRAW THE HISTOGRAM FOR A DIFFERENT IMAGE P
LANE ? Y/N",Y$
2548
                     IF (Y#="Y") OR (Y#="y") THEN Z3=50
                     IF (Y#="Y") OR (Y#="y") THEN Graph
2550
2560
                  Digitizes="N"
                                                ! RESET CONDITION
2570 Rerun: PRINTER IS 16
2588
               Y$="N"
               INPUT "ARE YOU GOING TO MAKE ANY MORE RUNS? YAN",YS
2598
                   IF (YS="N") OR (YS="n") THEN Finished
2688
               Changesa"H" INPUT "ARE YOU GOING TO CHANGE ANY PARAMETERS (n2,n3,Alpha,Nnay, OR
2618
2620
RHO-INITIAL)? Y/H", Changes
2638
                  IF (Changes="N") OR (Changes="n") THEN Gymnastics
               GOSUB Printer
PRINT " If you do NOT want to change a particular parameter"
PRINT "PRESS CONT in respose to the prompt."
INPUT "WHAT IS THE NEW VALUE OF RHO-INITIAL ?",Rho_initial
2648
2658
2669
2678
2680
               Rho_initial=-1+ABS(Rho_initial)
               Trhoi=TAN(Rho initial)
INPUT "HHAT IS THE NEW VALUE OF ALPHA?", Alpha
2698
2700
2719
                Talpha=TAN(Alpha)
               INPUT "WHAT IS THE NEW VALUE OF Y_BULLET ?",Y_bullet INPUT "WHAT IS THE NEW VALUE OF YA ?",Ya INPUT "WHAT IS THE NEW VALUE OF Yb ?",Yb
2728
2738
2748
2758
               Add_ray=0 ! RESET CONDITION

IF Ya>=Yb Then Beep

IF Ya>=Yb Then DISP "Ya MUST BE < Yb. PLEASE RE-ENTER YA AND Yb.
2768
2778
                  IF Ya>=Yb THEN WAIT 2500
IF Ya>=Yb THEN 2730
2780
2790
                  IF YDDY bullet THEN BEEP IF YD HUST BE < Y bullet. PLEASE RE-ENT
2888
2919
ER.
                  IF Yb>Y_bullet THEN WAIT 2508
IF Yb>Y_bullet THEN 2720
2828
2838
               Aperture=Yb-Ya
2849
               IF Ya()& THEN Add_ray=1
INPUT "WHAT IS THE NEW VALUE OF n2?",N2
INPUT "WHAT IS THE NEW VALUE OF n3?",N3
INPUT "WHAT IS THE NEW VALUE OF Z3 ?",Z3
INPUT "WHAT IS THE NEW VALUE OF THE No. OF RAYS?",Nray
2050
2869
2879
2888
2890
               INPUT "WHAT IS THE HEN No. OF INCREMENTS (1888 MAX ) ?", N_increment
2900
2910
               Changes="Y"
2920
           GOTO Gymnastics
2930
      Graph_grin: J=1
2940
                      FOR I=1 TO Nray
2950
                        R(I)=89R(X(J)^2+Y(J)^2)
2960
                        C(I)=N(I)+R(I)+SIN(Phi(I))
2970
                        J=J+5
2988
                      HEXT I
                      Y4="N"
2990
                      INPUT "DO YOU WANT TO PRINT A TABLE OF GRIN AND THE GRIN CONSTA
3000
NT ? Y/H",Y$
3016
                        IF (Y#="N") OR (Y##"n") THEN 3150
                      hards="N"
3020
                    INPUT "DO YOU HANT A HARD COPY OF THE TABLE ? Y/N", Y_hards
3030
3846
                      GOSUS Yhard
3050
                      GOSUB Header_c
3060
                   FOR I=1 TO Nray
3070
                        IF Linecount > Linemax THEN GOSUB Header
3080
                      PRINT USING 3090; I, N(1), R(1), Ph((1), SIN(Ph((1)), C(1)
3090
                      IMAGE 3X,4D,5(5X,4D.4D)
3100
                      Linecount=Linecount+1
3110
                   NEXT I
3126
                     GOSUB Header_end
```

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3130
                        GOSUB Yhard_end
3148
                     INPUT "DO YOU WANT TO PLOT THE RESULTS OF THE TRACE ? Y/N",Y*
3150
                        IF (YS="N") OR (YS="n") THEN Grinc
3168
3178
                     INPUT "ON WHICH DEVICE: CRT (C) OR THE 9872 (P) ? C/P ".Plots
3180
                        CALL Graph
3190
                      Y$="N"
3280
                     INPUT "DO YOU HANT ANOTHER PLOT DRAWN TO A DIFFERENT SCALE ? Y/N"
, Y$
3218
                        IF (Y#="Y") OR (Y#="y") THEN CALL Graph
                     Dump_crts="N" INPUT "DO YOU WANT A HARD COPY OF THE PLOT ? Y/N", Dump_crts
3229
3230
3244
                        IF (Dump_crts="Y") OR (Dump_crts="y") THEN GOSUB Printer
3250 Grinc: Grinc#="N"
                 INPUT "DO YOU WANT A GRAPH OF THE GRIN CONSTANT C(r) Us r ? Y/N", Gri
3268
nc $
                 IF (Grinc#="N") QR (Grinc#="n") THEN Rerun_grin INPUT "ON WHICH DEVICE: CRT (C) QR THE 9872 (P) ? C/P ",Plos#
3270
3286
3290 Grinc1: Grincs="Y"
3300
                    CALL Graph
3318
                  Grine#="N"
                                          ! RESET CONDITION
3320
                 Dump_crt#="H"
3336
                     INPUT "DO YOU HANT A HARD COPY OF THE PLOT ? Y/N", Dump crt$
                    IF (Dump_crt$="Y") OR (Dump_crt$="y") THEN GOSUB Printer
3340
3350
                 V4-"N"
                 IMPUT "DO YOU HANT ANOTHER PLOT DRAWN ? Y/N",Y$
3368
3370
                   IF (Ys="Y") OR (Ys="y") THEN Grinc1
3388 Rerun_grin: Ys="N"
                        G##"Y"
3390
                                         ! INSURANCE
                        INPUT "ARE YOU GOING TO MAKE ANOTHER RUN ? Y/N",Y#
IF (Y8="N") OR (Y8="n") THEN Finished
3400
3410
3428
                        Changes="N"
                        INPUT "ARE YOU GOING TO CHANGE ANY PARAMETERS (n2, n3, Alpha, Nray
 OR RHG-INITIAL)? Y/H", Changes
3440
                           IF (Changes="N") OR (Changes="n") THEN Gymnastics
3450
                        GOSUB Printer
                        PRINT " If you do NOT want to change a particular parameter" PRINT "PRESS CONT in respose to the prompt."

Add_ray=8 ! RESET CONDITION
INPUT "HHAT IS THE NEW VALUE OF RHO~INITIAL ?",Rho_initial
Rho_initial=-!sABS(Rho_initial)
3468
3478
3488
3498
3500
                        INPUT "WHAT IS THE NEW VALUE OF ALPHA?", Alpha
INPUT "WHAT IS THE NEW VALUE OF Nmin ?", Nmin
IF (Grins="C") OR (Grins="c") THEN 3578
3510
3520
3530
3540
                        INPUT "MHAT IS THE NEW VALUE OF NMAX ?", NMAX INPUT "WHAT IS THE NEW VALUE OF RO_MAX ?", RO_MAX INPUT "WHAT IS THE NEW VALUE OF n3?", N3
3550
3560
3570
3588
                        INPUT "WHAT IS THE NEW VALUE OF THE No. OF RAYS?", Nray
                        INPUT "HHAT IS THE NEW VALUE OF YA ?", YA
INPUT "HHAT IS THE NEW VALUE OF YB ?", YB
3590
2444
                          IF YA)=Yb Then Beep
IF Ya>=Yb Then Disp "Ya must be < yb. Please enter again"
3610
3620
                           IF YA>=Yb THEN HAIT 2500
IF YA>=Yb THEN 3590
3636
3640
3650
                        Aperture=Yb-Ya
3660
                          IF YAC'S THEN Rdd_ray=Rdd_ray+1
                        Changes="Y"
3678
                           GOSUS Printer
3686
3698
                        Changes="N"
                                                     ! RESET CONDITION
3700
            GOTO Gymnastics
3710 Printer:
                      IF (Changes="Y") OR (Changes="y") THEN Y_hards="N"
                      IF (Changes="Y") OR (Changes="y") THEN Y hards="N"

IF (Bump_crt$="Y") OR (Dump_crt$="y") THEN Y hard$="Y"

IF (Y hard$="Y") OR (Y hard$="y") THEN PRINTER IS 8

IF (Y hard$="Y") OR (Y hard$="y") THEN PRINT CHR$(27)&"&1901"

IF (Dump_crt$="Y") OR (Bump_crt$="y") THEN Crt
3720
1730
3740
3750
                      GOSUS Header initial
```

105 .

```
3778
                     IF (G$="Y") OR (G$="y") THEN Grin1
3788
                  FIXED 0
3798
                     IF Linecount>Linemax THEN GOSUB Header_initial IF Bates="" THEN 3830
3898
3818
                  PRINT "Curve No: "; Curve, TAB(48); "Date: "; Dates
3820
                   GOTO 3840
3836
                   PRINT "Curve No: "; Curve
3848
                   Linecount=Linecount+1
3950 Grin1:
                  FIXED 2
3868
                     IF Linecount > Linemax THEN GOSUB Header initial
3878
                  PRINT LIN(1), "RHO(INITIAL) = "; Rho_initial; "degrees"; TAB(48); "Alph
a = ";Alpha;"degrees"
3888
                  Linecount=Linecount+1
3898
                     IF Linecount > Linemax THEN GOSUB Header_initial
                  PRINT "TAN(RHO-INITIAL) = "; Trhoi; TAB(48); "Tan(Alpha) = "; Talpha
3988
3910
                  Linecount=Linecount+1
3928
                  FIXED 5
3938
                     IF (GS="N") OR (GS="n") THEN Grin2
                  IF Linecount>Linemax THEN GOSUB Header_initial
PRINT LIN(1), "n1 = ";N1;TAB(48);"n3 = ";N3
IF (Grin$="C") OR (Grin$="c") THEN 4010
3950
3968
                  IF Linecount>Linemax THEN GOSUB Header_initial
PRINT LIN(1), "Nmin = "; Nmin; TAB(48); "Nmax = "; Nmax
3978
3988
                  Linecount=Linecount+1
3990
                  GOTO 4040
IF Linecount>Linemax THEN GOSUB Header_initial
4888
4818
                  PRINT LIN(1), "Nmin = "; Nmin
4828
4030
                  Linecount=Linecount+1
4848
                     IF Linecount > Linemax THEN GOSUB Header_initial
4959
                  PRINT
4969
                  Linecount =Linecount +1
4878
                  FOR I=1 TO Nray STEP 3
                    IF Linecount>Linemax THEN GOSUB Header_initial IF 1>=250 THEN PRINT USING 4140; I, N(I) IF I>=250 THEN 4120 PRINT USING 4130; I, N(I), I+1, N(I+1), I+2, N(I+2)
4080
4898
4100
4110
4128
                     Linecount=Linecount+1
                     IMAGE 3(5X, "n2("3D") = ",2D.5D)
4138
4148
                     IMAGE 5X, "n2("3D") # ",20.5D
                  HEXT I

IF Linecount>Linemax THEN GOSUB Header_initial

PRINT LIN(1), "R0_max = ";R0_max;" inches"
4158
4168
4170
4189
4190
                     GOTO Grins
                  IF Linecount>Linemax THEN GOSUS Header_initial PRINT LIN(1), "n1 = ";N1;TAS(24);"n2 = ";N2;TAS(48);"n3 = ";N3
4288 Grin2:
4218
4228
                  Linecount=Linecount+1
4230 Grin3:
                  FIXED 3
4248
                    IF Linecount > Linemax THEN GOSUB Header_initial
4250
                  PRINT LIN(1), "Aperture = ";Aperture;TAB(24); "Ya = ";Ya;" inch ";TA
                ;Yb;" inch "
IF (Gs="Y") OR (Gs="y") THEN Grin4
3(48): "Yb =
4268
4270
                  Linecount=Linecount+1
4288
                  FIXED 2
                  IF Linecount>Linemax THEN GOSUB Header initial PRINT LIN(1), "Z3 = ";Z3;"inches";TAB(48);"Z4 = ";Z4;" inches"
4290
4380
4310
                  Linecount=Linecount+1
4320 Grin4:
                  FIXED 0
                    IF Linecount > Linemax THEN GOSUS Header_initial
4338
                  PRINT LIN(1), "Number of Rays = "; Hray
4348
                 Linecount=Linecount+1
IF (GS="Y") OR (GS="y") THEN Grin5
IF Linecount>Linemax THEN GOSUB Header_initial
4358
4368
4370
4380
                  PRINT LIN(1), "Number of Increments = "; N_increment
4390
                  Linecount=Linecount+1
4400 Grin5:
                  FIXED 2
                    IF Linecount > Linemax THEN GOSUB Header_initial
```

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4428
               PRINT
4430
               Linecount=Linecount+1
4440
                 GOSUB Header_end
                 IF (Dump_crt5="Y") OR (Dump_crt5="y") THEN DUMP GRAPHICS
IF (Y_hard5="Y") OR (Y_hard5="y") THEN PRINT CHR5(27)4"&136T"
4458 Crt:
4469
               Changes="H"
                                     ! RESET CONDITION
4470
               Dump_crts="N"
Y_hard$="N"
4488
4499
4590
             RETÜRN
IF Flags="1" THEN PRINT CHR$(27)&"&100T
4548
4550
           RETURN
4560 Yhard end: IF (Flags="1") OR (Flags="0") THEN PRINT CHR$(27)&"&136T"
4570 IF (Flags="1") OR (Flags="0") THEN PRINTER IS 16
4589
               RETURN
4590 Header_coef:
                     IF Linecount >Linemax THEN GOSUB Header_coef_end
4688
                    Linecount=0
4618
                   PRINT PAGE; LIN(5)
                   GOSUB Char short
PRINT LIN(1); SPA(6); "COEFFICIENTS"; LIN(1)
GOSUB Char_short
4628
4639
4640
                   PRINT LIN(2)
4658
4660
                 RETURN
4679 Header_coef_end: PRINT LIN(2)
                         GOSUB Char_short
4688
4698
                    RETURN
4700 Header_c:
                  IF Linecount > Linemax THEN GOSUB Header end
4710
                Linecount = 0
4728
                PRINT PAGE: LIN(5)
4738
                  GOSUB Char
                PRINT LINCLO,"
4748
                                                 n(I)
                                                                r(I)
                                                                              Phi(I)
     Sin(Phi)
                      C(I)";LIN(1)
4750
                                                 n(I)
                                                                r(I)
                                                                              Phi(I)
     Sin(Phi)
                      e(I)
4768
                  GOSUB Char
                PRINT LIN(2)
4778
4786
              RETURN
4798 Header_c_end:
                       GOSUB Header end
                  RETURN
4810 Header_initial:
                        IF Linecount > Linemax THEN GOSUB Header end
4829
4838
                       PRINT PAGE; LIN(5); TAB(28); "INITIAL PARAMETER VALUES"; LIN(1)
4848
                        GOSUE Char
4858
                       PRINT LIN(2)
                    RETURN
4868
HEXT Z
4920
4936
               RETURN
4948 Header:
                IF Linecount >Linemax THEN GOSUB Header_end
4950
              Linecount =0
4968
              PRINT PAGE, LIN(5)
                GOSUB Char
4978
              PRINT LIN(1)," (XI RHO";LIN(1)
                                < X9, Y9>
4988
                                               (X1, Y1)
                                                             (X2, Y2)
                                                                             (Xc, Yc)
     (X3, Y3)
4990
                GOSUS Char
5000
              PRINT LIN(2)
5010
                      DISP
                                (MP, YO)
                                               (X1, Y1)
                                                             (X2, Y2)
                                                                             (Xc.Yc)
     (X3,Y3)
RETURN
5020
5030 Header_grin:
                     IF Linecount > Linemax THEN GOSUB Header_end
3040
                  Linecount=8
```

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5950
                        PRINT PAGE, LIN(5)
5868
                           GOSUB Char
                        PRINT LIN(1),"
5070
                                                      (X0, Y0)
                                                                      (X1,Y1)
                                                                                         (X3, Y3)
 (Xc,Yc)
                  N2
                              RHO"; LIN(1)
5088
                                  DISP
                                                      (X8, Y8)
                                                                      (X1, Y1)
                                                                                         (X3, Y3)
                              RHO"
 (Xc.Yc)
                  N2
5090
                           GOSUB Char
                        PRINT LIN(2)
5188
5110
                    RETURN
5128 Header_end: PRINT LIN(2)
5130
                          GOSUB Char
5140
                    RETURN
5158 Char: FOR Zz=0 TO 79
                    IF Zz=79 THEN PRINT CHR$(228)
IF Zz=79 THEN 5190
5160
5170
                 PRINT CHR#(228);
5188
5198
               NEXT Zz
              PRINT RPT$("=", 98)
5288
                                             ! THIS IS A LOT FASTER, BUT NOT AS PRETTY
5210
            RETURN
5220
       Finished: DISP "FINISHED"
5238
             EHD
5240
       SUB Slope(Y)
5250
         OPTION BASE 0
5260
         COM INTEGER I, J, Curve, Np, Nn, Ns, Nr, REAL Aneg(*), Apos(*), A(*), 21, 23, 24 COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2 COM N1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
5278
5288
5298
5300
5318
         CON INTEGER Y0_loop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_total
5329
5338
        DEC
5340 IF Surf_no=2 THEN Two
5350 One: Alpha2=Alpha
5360
             Norm=Alpha2-98
5370
         SUBEXIT
5398 Two: IF YO THEN Negative
5390 Positive: Tan_m2=0
                                               ! SLOPE WRT Y-AXIS [dx/dy]
                    FOR I=1 TO No
5488
5419
                    Tan_m2=Tan_m2+1*Apos(I)*Y^(I-1)
NEXT I
5428
                    H2=ABS(ATN(Tan_m2)) ! THE ANGLE IS POSITIVE CH WRT 'Alpha2=98-M2 ! THE ANGLE IS POSITIVE CCH WRT X-AXIS
                                               ! THE ANGLE IS POSITIVE CW WRT Y-AXIS
5430
5448
5450
                    Norm=Alpha2-90
3468
             SUBEXIT
5478 Hegative: Tan_m2=6
5486 FOR I=1 TO Nn
                    Tan_m2=Tan_m2+1=fineg(1)+Y^(I~1)
NEXT I
5490
3500
                    M2=RBS(ATN(Tan_m2))
3510
3520
                    A1pha2=98-M2
3530
                    Tnorm=-1/TAN(Alpha2)
3540
                    Horm=ATH(Tnorm)-188
3550
                 SUBEND
3568 SUB Snell(X,Y)
3570
         OPTION BASE 0
3580
3590
         COM INTEGER I, J, Curve, Np, Nn, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4
3600
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2
COM N1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
3610
5620
         COM INTEGER Y0_loop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_total COM INTEGER Linecount, Linemax COM INTEGER Pselect, Hpib
5630
5640
5650
3660
3670
         COM REAL Hmin, Hmax, RO_max
        -COM Ray traces, Digitizes, Grins, Gs, Grincs, Plots, Dates COM X(+), Y(+), Xc(+), N(+), R(+)
5488
5698
```

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```
5788
5710
        IF Surf_no=2 THEN Two
5720
5730 One: Hn1=H1
5748
          Nn2=N2
5750
           Thetai=98-(Alpha+ABS(Rho))
5760
             CALL Slope(Y)
5778
             IF Thetai<8 THEN Neg_thetai
5788
          GOTO Same
5790 Neg_thetai: Flag=5
5888
                  Thetai=ABS(Thetai)
5818
                  Sip=N1/N2#Sin(Thetai)
5929
                    IF ABS(Sip)>1 THEN Wrong
5030
                  Thetar=ASN(Sip)
5848
                  Sho=Norm-Thetar
                     IF (ABS(Rho)<89.99999) OR (ABS(Rho)>90.00001) THEN Trho=TAN(R
5850
ha)
                    IF (ABS(Rho))89.99999) AND (ABS(Rho)(=90) THEN Trho=-9999999
5860
                     IF (ABS(Rho)>90) AND (ABS(Rho)<90.00001) THEN Trho=9999999
5876
               SUBEXIT
5888
5898 Tuo: Nn1=N2
5900
          Nn2=N3
5910
             IF YOU THEN Negative
5928
             CALL Siope(Y)
5930
           Thetai=98-ABS(Rho)-A1pha2
             IF Thetai(0 THEN Neg thetai2
IF (G$="Y") OR (G$="y") THEN GOSUB Grin
5940
5950 Same:
           Sin_iprime=Nn1/Nn2*SIN(Thetai)
IF ABS(Sin_iprime)>1 THEN Hrong
Thetar=ASN(Sin_iprime)
5969
5978
5988
5990
                                      ! USE ALPHA2 INSTEAD OF NORM BECAUSE THE
            Rho=Alpha2+Thetar-98
6000
                                      ! SIGN OF THE ANGLE IS DESIRED
6818
            Trho=TAN(Rho)
           Phi=Alpha-Rho
                               ! USED FOR GRIN
6829
6636
         SUBEXIT
6040 Neg_thetai2: Thetai=ABS(Thetai)
6050
                   Sip=Nn1/Nn2+SIN(Thetai)
6060
                     IF Abs(Sip)>1 THEN Wrong
6979
                   Thetar=ASN(Sip)
6888
                   Rho=Norm-Thetar
                     IF ABS(Rho)>=90 THEN Skip
                                                  ! THE RAY WILL NOT INTERCEPT
6898
                                                    ! THE IMAGE PLANE
6100
                     IF ABS(Rho)(89.99999 THEN Trho=TAN(Rho)
6110
                      IF (ABS(Rho)>89.99999) AND (ABS(Rho)<98) THEN Trho=-9999999
6129
               SUBEXIT
6130
6146 Skip: Flag=15
6150 IF ASS(Rho)>=90,000001 THEN Trho=TRH(Rho)
6160
              IF A35(Rho)<90.000001 THEN Trho=9999999
6170
            Rhop=188-ABS(Rho)
6180
            Trhop=TAN(Rhop)
            Xc(Y@_loop)=X-Y/Trhop
6190
       SUBEXIT
6218 Mrong: Flag=18 ! TOTAL INTERNAL REFLECTION AT THE SECOND SURFACE
6220
       SUBEXIT
6238 Negative:
                  CALL Slope(Y)
                Thetai=90+ABS(Rho)-Alpha2
6248
6250
                Sip=Nn1/Nn2+SIN(Thetai)
6260
                  IF ABS(Sip>>1 THEN Hrong
6270
                Thetar=#SN(Sin)
6280
                Rho=Norm-Thetar
6290
                Trho=TAN(Rho)
6300
              SUBEXIT
     Grin: N2=6
6310
6320
              IF (Grin#="P") OR (Grin#="p") THEN P
           CALL Index c(X,Y)
N(Y@_1oop)=N2
6330 C:
6340
```

```
IF Surf_no=1 THEN Nn2=N2
IF Surf_no=2 THEN Nn1=N2
6350
6360
6378
                RETURN
               CALL Index_p(X,Y).
N(Y0_loop)=N2
IF Surf_no=1 THEN Nn2=N2
IF Surf_no=2 THEN Nn1=N2
6388 P:
6390
6400
6410
6428
                RETURN
6438 SUBEND
6440 SUB Binary
                      _search(X,Y)
6450
          OPTION BASE 0
6468
         COM INTEGER I, J, Curve, Np, Nn, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4 COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2 COM N1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
6478
6488
6498
6588
6518
          COM INTEGER Ye_loop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_total
6520
          COM INTEGER Linecount, Linemax
6538
          COM INTEGER Pselect, Hpib
6540
6550
          COM REAL Nmin, Nmax, RO_max
         COM Ray traces, Digitizes, Grins, Gs, Grincs, Plots, Dates COM X(+), Y(+), Xc(+), N(+), R(+)
6568
6579
6588
6590
         COM Rho(+), Phi(+), C(+), Y3(+), Hit(+)
6600
6610
        DEG
        DEF FNA(X,Y)=X-Y/Trho
6628
        DEF FNA: (X,Y)=X-Y/Talpha
6630
                                                    ! FINDS THE INTERCEPT OF THE RRY AND Y=-Y 6
6649
        DEF FNXn(A)=A-Y_bullet/Trho
ullet
6650
        R=1
6660 IF Surf_no=1 THEN One
6670 IF Surf_no=2 THEN Two
6680 IF Surf_no=3 THEN Three
6690 Four: By=(Z4-X)+Trho
               Y=Y+Dy
6710
               X=24
6720
            SUBEXIT
6738 Three:
                  IF (Y>0) AND (Trho>0) THEN Skip !THE RAY WILL NOT CROSS THE X-AXIS
6748
                Xc(Y@_loop)=FNA(X,Y)
6750 Back: Dy=(Z3-X)+Trho
               Y=Y+Dy
6768
6778
               X=23
6788
            SUBEXIT
6798 One:
                CALL X1pos(X,Y)
            SUBEXIT
6800
6818 Two: R=FNA(X,Y)
6820
                 IF Flag=5 THEN Search2 ! Theta I < 0 FROM SHELL
6830
              F1 ag=0
6840
              F1ag2=0
                 IF (GS="Y") OR (GS="y") THEN Grin
IF ACZI THEN Negative ! THIS IS A SEPARATE AND UNRELATED TEST
6850
6860
6879
              GOTO Positive
                                                  ! FROM THAT PERFORMED IN SEARCH 2
6888 Search2: !
                         THIS ROUTINE IS ENTERED WHEN THE ANGLE OF INCIDENCE ON THE
                      FIRST SURFACE IS < 0 DEGREES.

THIS MEANS Thetal HAS DECREASED FROM ITS AXIAL VALUE TO 0
(ie. NORMAL TO THE FIRST SURFACE) THEN CONTINUED TO ROTATE PAST
THE NORMAL. THIS CORRESPONDS TO A TARGET AT OR NEAR CLOSEST
6898
6900
6918
6920
                      POINT OF APPROACH (CPA).
6936
                         MMEN THIS HAPPENS RHO(1) CAN BE LARGE ENOUGH TO CAUSE THE RAY
6940
                      TO MISS THE FIRST AND SECOND SURFACE.
THE ROUTINE FIRST CHECKS TO SEE IF THE RAY CROSSES THE SECOND
6950
6960
                      SURFACE. IF SO, CONTROL SHITCHES TO FASTER BISECTION POUTINE. IF NOT THEN THE ROUTINE MARCHES SLOWLY DOWN THE RAY TO FIND THE
6978
6988
6990
                    ! INTERCEPT (IF ANY).
7888 !
```

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```
7010
                  IF A>Z1 THEN Positive
7020 !
7030
                Delta-.01
7949
                X12=X
7959
                 Y12=Y
            EVEN THOUGH THE X-INTERCEPT APPEARS TO BE < Z1, THE SECOND SURFACE
7969
7070 ! COULD BE IRREGULAR ENOUGH TO CAUSE THIS SIMPLE CHECK TO BE DECEIVING. 7880 ! THE RAY IS ASSUMED TO HAVE INTERCEPTED THE SECOND SURFACE IF THE
7890 | DIFFERENCE BETHEEN THE RAY POSITION AND THE SECOND SURFACE < TOLERANCE
7100 March: Beltax=Belta+COS(Rho)
7110
              Deltav=Delta+SIN(Rho)
7120
              X12=X12+Deltax
              Y12=Y12+Beltay
7130
7140
                IF Y124 THEN Missed ! YOU HAVE REACHED THE X-AXIS
7150
              X2=0
7160
                CALL X2pos(X2, Y12)
              Xsave=X12-X2
7178
7180
                 IF ABS(Xave) (=Tol THEN Done1
                                                      ! FOUND THE SURFACE WITHIN TOL
7198
                 IF Xsave(8 THEN March
                                                      ! KEEP LOOKING
                 IF Xsave>8 THEN Found it
                                                      ! THE RAY CROSSED X2POS
7200
7218 Bone1: X=(X2+X12)/2
7220
              Y=Y12
7230
            SUBEXIT
                            ! THE RAY HAS MISSED THE POS AND NEG SURFACES
7248 Missed: X=A
                            I DRAW THE RAY TO THE X-AXIS
               Ywa
7250
7260
               GOTO Blind
                                  ! THE RAY HAS CROSSED THE SECOND SURFACE. GO TO THE
7270 Found_it: Xmid=X12
                                  ! BISECTION ROUTINE FOR SPEED
7288
                  Xlast=Xmid
7298
                  Yaid=Y12
7386
                  Ylast=Ymid
7310
                  Xsave=8
7320
                  GQTO Recurse_p
7330 Positive: X1=0
7340
                  X2=0
7350
                    CALL Xipos(X1,Y)
7360
                    CALL X2pos(X2,Y)
7379
                    IF X2<=X1 THEN Hoops
                                THE RAY HAS CROSSED THE X-AXIS BEHIND THE SECOND THE RAY HAS CROSSED THE X-AXIS BEHIND THE SECOND SURFACE. THEREFORE Y>0 AT THE INTERCEPT
7388
                  Xmid=A
                  Xmid=R
7398
7499
                  Xlast=Xmid
7410
                  Ynid=8
7428
                  Ylast=Ymid
7430
                  Xsaue=8
7448 Recurse_p: Xmid=(X+R+Xmid)/(1+R)
                   Ymid=(Y+R+Ymid)/(1+R)
7450
7460
                   X2=0
7478
                     CALL X2pos(X2, Ymid)
7488
                   Xsaue=X2-Xaid
                     IF Xsave(0 THEN First
IF Xsave>0 THEN Second
IF Xsave=0 THEN Done
                                                     ! INTERCEPT IS BEHIND THE HIDPOINT
                                                     ! INTERCEPT IS AMEAD OF THE MIDPOINT ! INTERCEPT IS THE MIDPOINT
7300
7518
7528 Recurse_n: Xmid=(X+R+Xmid)/(1+R)
                   Ymid=(Y+R+Ymid)/(1+R)
7530
7540
7556
                   X2=0
                     CALL X2neg(X2,Ymid)
7560
                   Xsave=X2-Xmid
                     IF Xsave<8 THEN First
IF Xsave>8 THEN Second
IF Xsave=8 THEN Done
7570
                                                     ! INTERCEPT IS BEHIND THE HIDPOINT
7580
                                                     ! INTERCEPT IS AHEAD OF THE MIDPOINT
                                                      INTERCEPT IS THE MIDPOINT
7596
7600 First:
                 IF ABS(Xsave)(Tol THEN Done
7610
              Xlast=Xmid
7620
              Ylast=Ymid
              IF Flag=1 THEN Recurse_n
GOTO Recurse_p
7630
7640
7639 Second:
                 IF ABS(Xxave)(To) THEN Done
7448
               X=X=1d
7678
```

· inter

Y=Ypid

```
7680
                 Xmid=X1ast
7690
                 Ymid=Ylast
7700
                   IF Flag=1 THEN Recurse n
                 GOTO Recurse_p
7710
7728 Negative: X1=8
7739
                   X2=8
                   Xc(Y@_loop)=A
CALL Xineg(Xi,Y)
7740
 7758
 7760
                      CALL X2neg(X2,Y)
                   IF X2<=X1 THEN Hoops

Flag=1 ! THE RAY CROSSES THE X-AXIS AHEAD OF THE SECOND

Y11=-Y bullet ! SURFACE AND COULD POSSIBLY INTERCEPT X2NEG.

X=A ! THE SAME TYPE OF TESTS DESCRIBED ABOVE
! IN SEARCH 2 ARE PERFORMED HERE.
 7779
 7780
 7798
 7800
 7810
 7929
                   Y=0
 7838
                   Deltas. 81
 7848 Search: X11=FHXn(A)
 7850
                 X2=8
 7860
                   CALL X2neg(X2,Y11)
 7879
                   IF X11>X2 THEN Ok ! X11 > X2max
 7880
                 X11=A
 7890
                 Y11=6
7900
                 Deltay=Delta+SIN(Rho)
 7918
                 Deltax=Delta=COS(Rho)
 7920 Search_n:
                     IF ABS(Y11)>=Y_bullet THEN Missed2 ! THE SECOND SURFACE WAS MI
 SSED
 7930
                   X11=X11+Deltax
                   Y11-Y11+Deltay
 7940
 7950
                   X2=8
 7968
                      CALL X2neg(X2,Y11)
 7970
                   Xsave=X11-X2
                      IF ABS(Xsave)<=Tol THEN Victory ! FOUND THE SURFACE IF Xsave>=0 THEN Ok ! " " "
 7980
 7990
                      IF Xsave(8 THEN Search n ! KEEP LOOKING
NXn(A) ! DRAN THE RAY UNTIL Y= -Y_bullet
 ....
                                                         ! KEEP LOOKING
 8018 Missed2: X=FNXn(A)
                  Y=-Y_bullet
GOTO Blind
8828
 1030
8848 Victory: Flag2=1
 4656
                  X=(X11+X2)/2
8868
8878
                  Y#Y11
               SUBEXIT
 8680 Ok: Flag2=1
                                  THE INTERCEPT OF THE RAY AND X2NEG HAS BEEN FOUND.
 1878
           Xmid=X11
                             ! GO TO THE BISECTION ROUTINE FOR SPEED.
 0100
            X1ast=Xmid
.110
            Ymid=Y11
1120
            Ylast=Ymid
0130
           GOTO Recurse n
8146 Bone: X=(X2+Xm1d)/2
8156 Y=Ym1d
8160 SUBEXIT
8178 Skip: Xc(Y0 loop)=0
8180 GOTO Back
9180 Blind: IF Flag=1 THEN Blind_n
               F1ag=20
0210
               X=A
8228
               Y-0
0230
               Xc(Y@_1oop)=#
8240
             SUBEXIT
8258 Blind_n: Flag=28
               Xc(Y@_loop)=A
SUBEXIT
8260
8270
$266 Hoops:
                 F1ag=36
                                    ! THE SECOND SURFACE HAS DENT AND CROSSED THE FIRST
9290
9300
               X=X2
                                 ! STOP THE RAY TRACE
               Y=Y
0310
               SUBEXIT
8320 Grin: A1=23
              Y=(A-A1)+(Talpha+Trho)/(Trho-Talpha) ! INTERCEPT OF THO LINES
```

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```
X=A+Y/Trho
8348
8350
             Xc (Y8_100p)=A
                             ! REQUIRED FOR DRAWING PURPOSES
2368
           SUBEND
8378 SUB Graph
2380
        OPTION BASE 0
8398
8499
        COM INTEGER I, J, Curve, Np, Nn, N, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4
        COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2
COM N1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
8418
8429
8430
        COM INTEGER Y0_loop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_total COM INTEGER Linecount, Linemax
8448
8450
8468
        COM INTEGER Pselect, Hpib
8478
8488
        COM REAL Hain, Nmax, RO_max
        COM Ray traces, Digitizes, Grins, Gs, Grincs, Plots, Dates
COM X(*), Y(*), Xc(*), N(*), R(*)
8498
8588
2519
8529
        COM Rho(+), Phi(+), C(+), Y3(+), Hit(+)
8536
2548
8556
       DEG
       PRINTER IS 16
8568
         IF (Grine = "Y") OR (Grine = "y") THEN Grine
8578
         IF (Digitizes="Y") OR (Digitizes="y") THEN Digit
8588
8598 Draw axes:
                      CALL Plot
8688 First_surf: FIXED 2
8618
                    LINE TYPE 8
                    Y=Y_bullet
MOVE 6,0
9629
8638
8648
                    X=Y/Talpha
8658
                    DRAW X,Y
2660
                    DRAH 100, Y
8678
                    MOVE 8,8
8688
                    DRAH X,-Y
                    DRAH 188,-Y

IF (G$="Y") OR (G$="y") THEN Grin_image
8690
8788
8718 X2pos: MOVE Apos(8),8
              FOR Y=0 TO Y_bullet STEP .01+Y_bullet
8730
                X2pos=0
8748
                   FOR I=0 TO Np
8750
                     X2pos=X2pos+Apos(I)#Y^I
8760
                   HEXT I
8778
                DRAH X2pos,Y
              HEXT Y
2710
8790 X2neg: MOVE Apos(0),8
              FOR Y=0 TO -Y_bullet STEP -.01*Y_bullet X2neg=0
2000
0010
                  FOR I=0 TO No.
9820
0030
                     X2neg=X2neg+Aneg(I)+Y^I
8848
                  NEXT I
                DRAM X2neg, Y
8858
9869
              NEXT Y
8878
              EXIT GRAPHICS
2220
              Y$="H"
              INPUT "DO YOU WANT A HARD COPY OF THE PLOT WITHOUT RAYS ? Y/N", YS IF (YS="Y") OR (YS="Y") THEN GOSUB Dump_is
6890
2900
2916
              GRAPHICS
8928 First_image: LINE TYPE 5
8990 Grin_image: LINE TYPE ?
                    Ym=-Y_bullet+.SeY_bullet
```

- 1

```
9818
                        Xm=Z3+Ym/Talpha
9028
                           MOVE Xm, Ym
9030
                        Ymm-Ym
9848
                        Xm=Z3+Ym/Talpha
9058
                           DRAH Xm, Ym
9060 REM DRAW THE RAYS
                   LINE TYPE 1
CLIP 8,188,-Y_bullet,Y_bullet
9079 First_:
9000
9898
                    1-0
                    FOR Ray_first=1 TO Nray
MOVE X(1),Y(1)
9188
9110
9120
                       DRAW X(I+1),Y(I+1)
9130
                       1=1+5
9146
                   NEXT Ray first
9150 Second_: I=1
                    FOR Ray_second=1 TO Nray
HOVE X(I),Y(I)
DRAW X(I+1),Y(I+1)
9160
9178
9188
9190
                       1=1+5
         NEXT Ray_second
IF (Gs="Y") OR (Gs="y") THEN Hait_
9200
9210
9220 First_image_p: I=2
9230
                            FOR Ray image=1 TO Mray
Mr=Nr+3
9240
9258
                               MOVE X(I),Y(I)
9268
9270
                                  IF X(I)<>0 THEN OK
                               I=I+5
9280
                               GOTO Next_ray_image
IF X(I+1)=0 THEN Reflect
9290
9300 Ok:
                               DRAW X(1+1), Y(1+1)
9310
9320
                               1=1+5
9338 GOTO Next_ray image
9340 Reflect: ! IF THE ANSWERE TO THE QUESTION IS NO, THE RAY WAS TOTALLY
                    ! REFLECTED AND DO NOT DRAW A LINE
! IF A LINE IS DRAWN, THEN ABS(RHO) > 90 DEGREES
    IF (Xc(Ray_image)=0) OR (Rho(Nr)=0) THEN 9400
    Trho=-1*Y(I)/(Xc(Ray_image)-X(I))
    DRAW X(I)-(Y(I)+Y_bullet)/Trho,-Y_bullet ! RHO > 90 DE
9356
7368
9378
9388
9390
GREES
9486
9418 Next_ray_image: HEXT Ray_image
9420 Decision: HAIT 2000
9430
                     EXIT GRAPHICS
9448
9450
                     Y$="H"
9440
                     INPUT "DO YOU HANT TO PLOT TO THE SECOND IMAGE PLANE ? Y/N", YS
9478
                     GRAPHICS
9400 IF (Tam:
9490 Second_image_p: I=3
Mage
                       IF (YS="N") OR (YS="n") THEN Hait_
7500
9510
                             FOR Ray_image2=1 TO Hray
Hr=Nr+3
9520
                                HOVE X(I),Y(I)
IF X(I)<>0 THEN 0k2
9530
                                GOTO Next_ray_image2
IF X([+1)=0 THEN Reflect2
9578 Ok2:
                                DRAW X(1+1), Y(1+1)
9590
                                1-1+5
                               GOTO Next_ray_image2

IF (Xc(Ray_image2)=0) OR (Rho(Nr)=0) THEN 9640

Trhom-1*Y(I)/CXc(Ray_image2)-X(I))

BRAN X(I)-(Y(I)+Y_bullet)/Trho,-Y_bullet ! RHO > 90 DE
9600
9610 Reflect2:
9620
9630
GREES
                               1=1+5
9650 Hext_ray_image2: HEXT Ray_image2
```

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9660
                              GOTO Hait_
9679 Grinc:
                   CALL Plot
9688
                R1=C(1)/(H(1)+SIN(Phi(1)))
                   MOVE R1,C(1)
HOVE R(1),C(1)
9690
9788
9710
                 FOR 1=2 TO Hray
9728
                   R=C(I)/(H(I)+SIN(Phi(I)))
9730
                   DRAH R,C(1)
9740
                   DRAW R(I),C(I)
9758
                HEXT I
9760 Hait_:
                                                          THIS ROUTINE PRESENTS THE PLOT TO THE
                ! SETGU
9770
                LINE TYPE 1
                                                ! OPERATOR TO STUDY UNTIL READY TO CONTINUE
9780
9790
                LDIR . 6
                MOVE 2,2
                CSIZE 2
LABEL "PRESS CONT"
9666
9810
9828
                CSIZE 15/4.54
9839
                SETUU
9840
                BEEP
                HAIT 258
9858
9860
                BEEP
9070
                PAUSE
3886
                EXIT GRAPHICS
3690
              SUBEXIT
       Digit: GRAPHICS
9900
                POINTER Z3.8
7910
7920
                 DIGITIZE Z3,Y
7930
                LINE TYPE 5
                   MOVE Z3,Y_bullet
DRAH Z3,-Y_bullet
9940
9950
7760
7770
7780
7780
10000
                SETGU
                LDIR .
                LINE TYPE 1
LORG 5
                CSIZE 2.5
                Centerx=72.5
                                      ! CHANGE IN Laxes also
10020
                   HOVE 1.5+Centerx,5
10030
                 LABEL USING 18848; 23
10040
                 IMAGE "Image Plane : ", DD. BB, " inches"
10050
10060
10070
10080
10090
                SETUU
                CSIZE 15/4.54
                HAIT 2500
EXIT GRAPHICS
            SUBEXIT
10100 Dump_it:PRINTER IS 0
10110
                   PRINT CHR$(27)&"&100T"
10120
                   DUMP GRAPHICS
10130
                   PRINT CHR#(27)&
10140
                   PRINTER IS 16
10150
                RETURN.
LOLGO SUDEND
19176 SUB Plot
19180 OPTION
          OPTION BASE .
10190
         CON INTEGER I, J, Curve, Np, Nn, Ns, Nr, REAL Aneg(*), Apos(*), A(*), Z1, Z3, Z4 COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2 COM H1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
16266
10210
10220
10230
         COM INTEGER YO loop, Mray, Add_ray, Surf_no, Flag, Flag2, M_increment, Hit_total COM INTEGER Linecount, Linemax COM INTEGER Pselect, Hptb
10240
10250
10260
10270
         COM REAL Mmin, Mmax, Re_max
COM Ray traces, Bigitizes, Grins, Gs, Grincs, Plots, Bates
COM X(**), Y(**), Xc(**), N(**), R(**)
10200
10290
10300
10310
10320
         CON Rha(+), Phi(+), C(+), Y3(+), His(+)
```

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10336
10346
           THE ORIGINAL VERSION OF THIS ROUTINE IS LOCATED IN THE HP-9845
10350
           LIBRARY TAPE No. THE SER: .09845-18285 PROGRAM "REGPLT
10360
18378
18328
            FHMAX AND FRMIN HAVE BEEN MADE INTO SUBROUTINES
19399
      Set_up: IF (Plots="P") OR (Plots="p") THEN P9872a Crt: PLOTTER IS 13, "GRAPHICS"
10400
10410
18428
            GOTO 19449
10430
       P9872a: PLOTTER IS Pselect, Hpib, "9872A"
19449
                GCLEAR
10450
                                               ! ALL UNITS IN MILLIMETERS
                LIMIT 0,184,0,140
                LINE TYPE 1
LDIR 0
19468
10470
10480
                LORG 5
10490
                DATA -2,-1,1,2
10500
                READ Um, Dm, Md, Mu
DATA .39794, .69897, .87504
18518
10520
10530
                READ Log2, Log5, Log?
10540
10550
                  IF (Grinc*="Y") OR (Grinc*="y") THEN Grinc
                  IF (G$="Y") OR (G$="Y") THEN Grin
IF (Digitize$="Y") OR (Digitize$="y") THEN Digit
IF (Ray_trace$="Y") OR (Ray_trace$="y") THEN Ray
19569
18579
18588
18590
18688 Ray: Xmin=Xorg=Yorg=$
10610
           Xmax=10
           Ymax=Y_bullet
19630
           Ymina-Yaav
           PRINT PAGE," Xwax is the maximum length along the GLM axis which you"
18648
10650
           PRINT "want to be displayed."
10660
                             A rule of theumb is to pick a typical value of Xc (the
 X-inter
18678
           PRINT "from the printed output for the ray trace and add one inch to"
           PRINT that value. For example: if the majority of the Xc values liste
19689
18698 PRINT "have values around 5.6, then key in 6.6 and PRESS CONT."
18788 Ray1: INPUT "MMAT IS THE VALUE OF Xmax (BEFRULT VALUE IS 18.8 INCHES > ?", X
18718
              IF Xmax<=Xmin THEN DEEP
             IF Xmax(=Xmin THEN DISP "Xmax MUST BE > Xmin = 0. PLEASE RE-ENTER
18728
Xmax. "
19730
              IF Xmax(=Xmin THEN WAIT 2500
19740
             IF Xmax (=Xmin THEN Ray1
10750 Ray_scale: LOCATE 15,139,25,100
                                                         I ALL UNITS IN GDU'S
18768
                      GOSUS Same
19770
                   SCALE Xmin-.5*Xfudge, Xmax+.5*ABS(Ytic), -Y_bullet-.25*ABS(Ytic),
 builet+. 25+ABS(Ytic)
                   SCALE Xmin-.5+ABS(Ytic), Xmax+.5+ABS(Ytic), -Y_bullet-.25+ABS(Yti
c), Y_bullet+.25#ABS(Ytic)
                    CLIP Xmin-.5-Xfudge, Xmax+.5+ABS(Ytic), -Y_bullet-.25+ABS(Ytic),
Y bulles+, 25+ABS(YE1c)
1666 CLIP
                    CLIP Xmin-. 84A38(Ytic), Xmax+. 54A38(Ytic), -Y_bullet-. 254A38(Yti
c),Y_bullet+.25+R38(Ytic)
                   GOSUB Same_axes
CLIP Xmin,186,-Y_bullet,Y_bullet
10620
10030
                 SUBEXIT
10040 Digit: LOCATE 0,130,30,100
                                               ! ALL UNITS IN GBU'S
19050
               Xmax=Y_bullet
Xmin==Xmax
               Xorg=Yorg=0
10000
               Yeax-1
10070
               Ymin=0
                GOSUS Same
18918 Bigiti_scale: SCALE -Y_bulles-.15+ABS(Ytic),Y_bullet+.15+ABS(Ytic),-.15+AB
```

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$(Ytic), 1+.15+AB$(Ytic)
                        CLIP -Y_bullet-.15+ABS(Ytic),Y_bullet+.15+ABS(Ytic),-.15+AB
10926
$(Ytic), 1+.15+AB$(Ytic)
                         GOSUS Same_axes
18938
10940
                      SUBEXIT
18958 Grin: GOTO Ray
10960 Grinc: LOCATE 18,133,28,191
                                              ! ALL UNITS IN GDU'S
10970
               Xorg=Yorg=6
                 GOSUB Hin c
10900
18999
11000
               Ymin=Chin=Hinc
11010
               Ymax=Cmax=Maxc
11020
                 GOSUB Min_r
11839
                 GOSUS HAX T
11840
               Xmax=Haxr
11958
               Xmin=Hinr
11060 Grinc_scale: GOSUB Same
11979
                      SCALE Xmin, Xmax+ABS(Xtic), Ymin, Ymax+ABS(Ytic)
                       CLIP Xmin, Xmax+ABS(Xtic), Ymin, Ymax+ABS(Ytic)
11080
                        GOSUB Same_axes
11090
11100
                    SUDEXIT
11110 Same: Lx=LGT(Xmax-Xmin)
             Ly=LGT(Ymax-Ymin)
11120
11130
              Xfudge=, 26+(Xmax-Xmin)
11140
              Yfudge=.20=(Ymax-Ymin)
11150 Ticmarks: Testxtic=FRACT(Lx)+(Lx<0)
11160
                  Testytic=FRACT(Ly)+(Ly(0)
11170
                  Xtic=18^(INT(Lx)-1)*(1+1.5*((Testxtic>Log2) AND (Testxtic(Log5))
+4*((Testxtic)=Log5) AND (Testxtic(=Log7))+6.5*(Testxtic)Log7))
11180 Ytic=18^(IHT(Ly)=1)*(1+1.5*((Testytic)Log2) AND (Testytic(Log5))
11180
+4*((Testytic)=Log5) AND (Testytic(=Log7))+6.5*(Testytic)Log7))
11190
                RETURN
11200 Same_axes: CALL Laxes(Xtic,Ytic,Xorg,Yorg,Xmaj,Ymaj,Hinticsize,Xmin,Xmax,
Ymin,Ymax,Hinn,Haxx)
11210
               RETURN
11220 Min_r: Minr=R(8)
              FOR I=1 TO Hray
Hinr=HIN(Hinr,R(I))
11230
11248
11250
               NEXT I
11268
            RETURN
11276 Max_r: Maxr=R(8)
               FOR I=1 TO Hray
11200
11290
                 Maxr=MAX(Maxr,R(I))
11300
              HEXT I
11310
            RETURN
11320
      Min_c: Minc=C(0)
               FOR I=1 TO Hray
11330
11340
                 Mine=MIN(Mine, C(I))
11350
               HEXT I
11360
            RETURN
11370 Max_c: Maxc=C(0)
            FOR I=1 TO Hray
Haxc=HRX(Haxc,C(I))
11390
11390
            NEXT I
11410
           RETURN
          SUBEND
11420
11438 SUB Laxes(Xtic, Ytic, Xorg, Yorg, Xmaj, Ymaj, Hinticsize, Xmin, Xmax, Ymin, Ymax, Hin
n, Maxx)
11440
         OPTION BASE &
11450
11466
         COM INTEGER I, J, Curve, Np, Nn, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4
         COM Alpha, Talpha, Rho, Trho, Rho initial, Trhoi, Phi, Tol, Norm, Alpha2 COM NI, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
11470
11460
11490
11500
         COM INTEGER Y0_100p, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_tota
11510
         COM INTEGER Linecount, Linemax
```

```
11520
          COM INTEGER Pselect, Hpib
11530
11540
          COM REAL Main, Mmax, RO_max
          COM Ray_traces, Digitizes, Grins, Gs, Grincs, Plots, Dates
11550
11560
          CON X(+), Y(+), Xc(+), N(+), R(+)
11570
11500
          COM Rha(+), Phi(+), C(+), Y3(+), Hit(+)
11590
11610
          LINE TYPE 1
11620
          LDIR 0
          LORG 5 ... IF (Xmin)=Xmax) OR (Ymin)=Ymax) THEN SUBEXIT
11630
11646
          GRAPHICS
11650
          Xfudge=.02*(Xmax-Xmin)
Yfudge=.02*(Ymax-Ymin)
11660
11678
11680
          Xma.i=1
11690
          Yeai=1
11700
          Minticsize=2
11710
             IF (Grinc$="Y") OR (Grinc$="y") THEN Grinc
IF (G$="Y") OR (G$="y") THEN Grin
IF (Bigitize$="Y") OR (Bigitize$="y") THEN Bigit
11720
11730
11746
             IF (Ray_traces="Y") OR (Ray_traces="y") THEN Ray
11750
11760
11778 Grinc: LINE TYPE 3
                 GRID Xtic, Ytic, Xorg, Yorg, Xmaj, Ymaj, 20Minticsize
LINE TYPE 1
11788
11790
11800
                 FRAME
                 GOTO Labelx_grinc
11818
11828 Grin: GOTO Ray
11838 ! Digit: AXES .1,.1,0,8,1,1,2
11840 Bigit: AXES Xtic,.1,8,8,1,1,2
11850 GOTO Labelx_d
11860 Ray: AXES Xtic, Ytic, Xorg, Yorg, Xmaj, Ymaj, Minticsize
11876 Labelx: LDIR 98
11000
                  LORG 8
11090
                  FOR A=Xorg TO Xmax STEP ABS(Xtic)
                     MOVE A, Yorg-Yfudge
IF A=0 THEN LABEL USING 11920; A
11900
11910
                        IMAGE .,K
11920
                     IF A=0 THEN GOTO 11960
LADEL USING 11950; A
IMAGE DDD.D,K
11930
11940
11960
                  NEXT 6
11978 Labely: LDIR
11900
11990
12000
                   LORG 8
                   FOR A -- Y_bullet TO Y_bullet STEP ABS(Ytic)
                     MOVE XORG-Xfudge,A
IF A=0 THEN LABEL USING 11920;A
IF A=6 THEN GOTO 12048
12010
12020
12030
                     LABEL USING 11950; A
12040
                   HEXT A
12050
                   GOTO Label_
12060
12070 Labelx_d: LBIR 90
12000
                     LORG 8
                     FOR A--Y_bullet TO Y_bullet STEP .1
FOR A--Y_bullet TO Y_bullet STEP ABS(Xtic)
HOVE A, Yorg-Yfudge
IF A-0 THEN LABEL USING 11920; A
IF A-0 THEN GOTO 12150
12100
12116
12120
12130
                        LABEL USING 11950; A
12140
                     HEXT A
12150
12160 Labely_d: LBIR 0
12170
12100
                     FOR REG TO YMAX STEP .1
```

```
MOVE Xorg-Xfudge,A
IF A=0 THEN LABEL USING 11920;A
IF A=0 THEN GOTO 12230
12198
12290
12210
12228
                        LABEL USING 11950; A
12230
                      NEXT A
12240
                     GOTO Label_
12250
12260 Labelx_grinc: LDIR 90
12278
                           LORG 8
                          FOR R=Xorg TO Xmax+RBS(Xtic) STEP RBS(Xtic)

MOVE A, Yorg-Yfudge

LABEL USING 12310; R

IMAGE #,K
12289
12290
12300
12310
12320
                           NEXT A
12330
        Labely_grinc: LDIR 0
12349
                           LORG 8
12350
                           FOR A=Yorg TO Ymax+ABS(Ytic) STEP ABS(Ytic)
12360
                                MOVE Xorg-Xfudge, A
12379
                             LABEL USING 12310; A
12380
                           NEXT A
12399
12400 Label_: LDIR 0
12410
                   LORG 5
12420
                     MOVE -18+Xmax, 9
                   LABEL "RESET CR/LF"
12439
12440
                   SETGU
12458
                   CSIZE 2.5
                     IF (Grincs="Y") OR (Grinc$="y") THEN Grinc_label
12460
                     IF (GF="Y") OR (GF="Y") THEN Grin_label
IF (GF="Y") OR (GJ="Y") THEN Grin_label
IF (Ray_tracef="Y") OR (Ray_tracef="y") THEN Ray_label
12479
12480
12490
12580
12519 Ray_label: Centerx=72.5
                                              ! CHRNGE IN Graph ALSO
12528
                       Centery=62.5
12530
                         MOVE 1.5+Centerx, 13
                      LABEL USING 12550; Nray
IMAGE "Number of Rays: ",K
12540
12558
                      HAVE .SeCenterx,9
LABEL USING 12500; Rho_initial
IMAGE "Incident Ray Angle : ",30.00," deg"
MOVE .SeCenterx,5
12560
12570
12580
12590
                      LABEL USING 12610; N2 IMAGE "n2 : ", D. DDDDD
12688
12619
12629
                         MOVE 1.5=Centerx,9
                       LABEL USING 12640; Aperture IMAGE "Aperture: ", D. DDD, " inch'
12639
12640
12650
                      MOVE Centerx, 20
LABEL "Distance Along the GLM fixis (inches)"
12668
12679
12680
                      CSIZE 3
                      MOVE .5=Centerx,13
LABEL USING 12710;Curve
IMAGE "Curve Number: ",K
12690
12700
12710
12720
12730
                         MOVE 1.5, Centery
12740
                       LABEL "Radial Distance From the fixis (inches)"
12750
                       LBIR 0
12760
                       CSIZE 15/4.54
                       GOTO Label_end
12780
12790 Digit_label: Centerx=65
12000
                         Centery=65
12010
                            MOVE 1.5+Centerx, 13
12020
                         LABEL USING 12550; Nray
12030
                            HOVE .5+Centerx,9
12840
                         LABEL USING 12850; HIS_total
```

```
12858
                          IMAGE "Number of Hits on the Image Plane : ",K
12868
                            MOVE 1.5+Centerx, 9
                          LABEL USING 12880; Percent image
IMAGE "% of Rays to Image Plane : ",3D.DD
12879
12888
12890
                            MOVE 1.5+Centerx,5
12900
                          LABEL USING 12918; 23
12918
                          IMAGE "Image Plane : ", DDB. DD, " inches"
12928
                            MOVE .5*Centerx,5
                          LABEL USING 12940; M increment
IMAGE "Number of Increments [0,1.1]: ",K
12930
12948
12950
12960
                         CSIZE 3
12978
                            MOVE Centerx, 20
                         LRBEL "Normalized Number of Hits US Distance from the Axis" MOVE .5*Centerx,13
12988
12998
                         LABEL USING 12710; Curve IMAGE, "Curve Number ; ", K
13000
13018
13020
                         GOTO Label_end
13030
13848 Grin_label: Centerx=72.5
13056
                        Centery=62.5
13060
                        CSIZE 2.5
13070
                          MOVE .5+Centerx, 13
                        LABEL USING 13090; H1
IMAGE "n1: ", DD. DDDDD
MOVE .5*Centerx, 9
13886
13898
13166
                        LABEL USING 13120; N3
IMAGE "n3: ", DB. DDDDD
13110
13120
                        MOVE 1.5-Centerx,13
LABEL USING 13150;Alpha
IMAGE "Alpha: ",DD.DD," degrees"
13130
13140
13150
13160
                          MOVE 1.5+Centerx,9
13170
                         ABEL USING 13180; Nray
                        IMAGE "Number of Rays : ",K
13188
13190
                        CRIZE 3
                        MOVE Centerx, 28
LABEL "GRIN TRACE"
13200
13218
                        LDIR 90
13228
                        HOVE 1.5, Centery

LABEL "Radial Distance From the Axis ( inches )"
13230
13248
13250
                        GOTO Label_end
13260
13270 Grinc_label: CSIZE 3
                         LORG 5
13286
13290
                         LDIR 0
13300
                         Centerx=74
13310
                         Centery=64
13320
                            MOVE Centerx,5
                         LABEL "Radius From the Origin (inches)"
13330
13340
                         MOVE 1.5, Centery
LABEL "Gradient Index Constant : C(r) (inches)"
13350
13360
13370
13300 Label_end: CSIZE 15/4.54
13390
                      LDIR 90
13460
                      LORG 5
13410
                      SETUU
13420
                    SUBEND
13436 SUB X1pos(X,Y)
          OPTION BASE &
13440
13450
13460
          COM INTEGER I, J, Curve, Np, Nn, N, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4 COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2 COM N1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
13470
13480
13490
          COM INTEGER YO_loop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_tota
13500
```

0

```
13518
13528 DEG
13538 DEF FNY1(Y)=Y+Talpha/(Talpha-Trho) ! FINDS THE Y-VALUE OF THE INTERCEPT
13540
                                                  OF THE RAY AND THE FIRST SURFACE
13550 DEF FNX1(Y)=Y/Talpha
                                  I FINDS THE X-VALUE OF THE INTERCEPT OF THE RAY
13560
                                   ! AND THE FIRST SURFACE
13570
              IF Surf_no=2 THEN Hoops
13580
            Y=FNY1(Y)
13590 Woops:X=FHX1(Y)
13600
            SUBEND
13618 SUB XIneg(X,Y)
         OPTION BASE &
13626
13638
13648
         COM INTEGER I, J, Curve, Np, Nn, Ns, Nr, REAL Aneg(*); Apos(*), A(*), Z1, Z3, Z4
         COM Alpha, Talpha, Rho, Trho, Rho_initial, Trho, Phi, Tol, Norm, Alpha2 COM NI, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet . . .
13650
13660
13679
13688
         COM INTEGER Y0_loop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_tota
13698
13700 DEG
13710 Alphan=-1+Alpha
13726 Talphan=TAN(Alphan)
13739 DEF FNY1(Y)=Y*Talphan/(Talphan-Trho) ! FINDS THE Y-VALUE OF THE INTERCEPT
                                                  ! OF THE RAY AND THE FIRST SURFACE
13748
13758 DEF FHX1(Y)=Y/Talphan ! FINDS THE X-VALUE OF THE INTERCEPT OF THE RAY
                                  I AND THE FIRST SURFACE
13760
            IF Surf_no=2 THEN Hoops Y=FHY:(Y)
13770
13780
13790
      Hoops:X=FNX1(Y)
13000 SUBEND
13819
      SUB Dialogue
13820
         OPTION BASE 0
13830
         COM INTEGER I, J, Curve, Np, Nn, N, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4 COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2
13848
13850
13868
         COM N1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
13878
13080
         COM INTEGER Y0_loop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_tota
13898
         COM INTEGER Linecount, Linemax
13900
         COM INTEGER Pselect, Hpib
13910
13920
         COM REAL Nain, Naax, RO_max
         COM Ray traces, Digitizes, Grins, Gs, Grincs, Plots, Dates
CON X(*), Y(*), Xc(*), N(*), R(*)
13930
13940
13958
13960
         COM Rho(+), Phi(+), C(+), Y3(+), Hit(+)
13970
13900 DEG
13990 Initialize_top:Alpha=21
14000
                         Talpha=TAN(Alpha)
14010
                        Rho_initial=0
14928
                         Trho_i=TAN(Rho_initial)
14030
14040
                         To1=.00001
14450
                         23-24-58
14968
                         H1=H3=1
14070
                         N2=1.5
                        Nray=10 ! IN ORDER TO OUTLINE THE APERTURE AN EXTRA RAY Add ray=0 ! MUST BE ADDED IF Ya # 0 Ya=0
14000
14898
14180
14110
14120
                         Yb=Y bullet
14136
                         Aperiure=Ya-Yb
14140
14150
                         Y_bullet=1.1
```

```
14168
                        N_increment=100
14170
14180
                        Linecount=0
14190
                        Linemax=46
14200
14210
                        Naax=4
14229
                        Nain=2
                        Ym2=(1.05+Y_bullet/2)^2 ! THE 1.05 IS A FUDGE FACTOR TO 
Xm2=(1.05+Y_bullet/(2+Talpha))^2 !PREVENT THE RADIUS FROM 
R0_max=SQR(Xm2+Ym2) ! BECOMING TOO SMALL AND CAUSING A
14230
14240
14250
                                             NUMERICAL ERROR IN THE INDEX SUBROUTINES
14260
14279
                        Pselect=7
14286
                        Hpib=5
14299
14300
                        Grins="C
                        G$="H"
14310
14320
                        Grinc#="N"
14330
                        Plots="C"
14340
                        Digitizes="H"
14350
                        Dates ...
14368 REH *** TEMP ***
14370
        GOTO Alpha
14380 REM --- TEMP ---
14390 Begin: PRINT PAGE,"
                                The following drawing illustrates the optical proble
14400
              PRINT "which this program attempts to solve; foccusing monochromati
              PRINT "light rays through a conical lens for a Gun-Launched-Missile
14418
 (GLM)."
                         The picture is also labeled showing the various quantitie
14428
.
14430
              PRINT "Please study the picture and become familiar with it. The va
riables'
              PRINT "will be explained as they appear in the program." PRINT LIN(2), "PRESS CONT"
14448
14458
14468
               PAUSE
14470
                 CALL Picture
               PRINT PAGE," Z1 is the intercept of the second surface and the PRINT "the GLM-axis. Therefore, the value of Z1 is APOS(0)."
14480
14498
14500
               PRINT LIN(1), "NOTE: Apos(0) is the constant term in the polynomia
1 used"
14518
               PRINT .
                             to describe the second surface of the lens in the "
              PRINT "
14528
                             upper half-plane.
              PRINT " The (min, max) values of 21 are [0, infinity] inches."
PRINT LIN(2), "PRESS CONT"
14538
14548
14558
               PAUSE
               PRINT PAGE."
                                There are two planes used as image planes. The first
14568
 18
14570
               PRINT "located at X=23 (default value = "; 23; "inches). This locatio
14586
               PRINT "is programmable, according to the needs of the particular pr
oblem."
               PRINT "You key in the new location when locating the position of "
14598
14600
               PRINT "maximum ray density, or when a new run is begun. Directions
will "
14618
               PRINT "be provided at the appropriate time."
              PRINT LINCED,"
14628
                                  The second image plane is permanent, located at X=
24 = "; 24;
             nches.
14630
              PRINT LIN(2), "PRESS CONT"
14640
               PAUSE
                                This program will trace mochromatic light rays which
14650
              PRINT PAGE."
 arrive'
14660
               PRINT "at the first surface parallel or at an angle to the GLM axis
               PRINT "Non-axial rays approach the GLM from 'above', for all rays a
14678
re "
```

74.78

0

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14688
               PRINT "initiated in the upper half of the meridian plane."
               PRINT LIN(2), "PRESS CONT"
14690
14786
               PAUSE
              PRINT PAGE," The program uses Snell's Law without approximation." PRINT "The appropriate variables are:"
14718
14720
14738
               PRINT LIN(1),"
                                   1) Norm = dY/dX = slope of the normal to the s
urface
14748
              PRINT "
                            2) Thetai = angle of incidence with respect to the surf
ace normal."
14750
              PRINT .
                            3) Thetar = angle of refraction with respect to the sur
face normal.
               PRINT "
                            4) Rho = angle of the ray with respect to the GLM-axis"
               PRINT "
14779
                                       (subscripts indicate the region the ray is in)
14788
              PRINT LIN(2), "PRESS CONT"
14790
              PAUSE
14888
       PRINT PAGE, "The sign convention is :"
14818
       PRINT LIN(1),"
                              1) the origin is placed at the vertex of the first su
rface.
14828 PRINT "
                      2) distances: (a) positive to the right of the origin.
        PRINT "
14838
                                      (b) positive above the origin (Y-axis)."
(c) positive out of the meridian plane (screen
14849
        PRINT
14850
        PRINT "
                                       (ie. a right hand system.)
14868
        PRINT "
                      3) angles: slope = Alpha2 is POSITIVE for counter-clockwise"
        PRINT "
                                            rotation from the GLN-axis to the ray"
14879
14880
        PRINT "
                      4) symbols: unprimed = object space."
       primed = image space."
PRINT LIN(2), "PRESS CONT"
PRINT LIN(2)
14898
14900
14916
       PAUSE
14928 Alpha:PRINT PAGE,"
                                Alpha is the angle of inclination of the "
             PRINT "FIRST surface with respect to the GLM-AXIS"
PRINT LIN(3)," The current value of ALPHA is"; Al
14938
14948 PRINT LIN(3)," The current value of ALPHA is"; Alpha; "degrees"
14959 INPUT "WHAT IS THE NEW VALUE OF ALPHA (DEGREES)?", Alpha
14960 Index: PRINT PAGE," The lens system is assumed to be operating in air."
         PRINT "Therefore the first index of refraction = ni= 1.00000"
14970
14988
         PRINT LIN(1),"
                             It is assumed that n1 < n2 for the homogeneous and gra
dient cases.
14998
        PRINT LIN(1)," You are free to choose any values for n2 and n3 for the
 homogeneous case.
15900
         PRINT LIN(2), "PRESS CONT"
15010
         PAUSE
15029
         PRINT PAGE."
                         The program has the capability to use a gradient index of
 refraction (GRIH)."
        PRINT "Two GRIN subroutines are available:"
PRINT LIN(1)," 1) Parabola : the index of region 2 (the lens) v
15030
15849
---
15050
         PRINT "
                                            as a parabola from a min at the vertex"
                                            to a maximum (at a radius specified by yo
15060
         PRINT "
u) "
15078
         PRINT "
                                            then down to a value determined by the
15000
         PRINT "
                                            top of the GLH"
15090
         PRINT "
                                            The equation is (n(r) = k + r^2)
         PRINT LINCED,"
15100
                                    2) Circle : the index varies as a circle whose c
enter
      is located"
15116
         DOINT "
                                          at a specified radius from the origin"
         PRINT "
                                          The equation is [ n(r) = SQR( R8_max^2 + r^
15120
2 > 14
         PRINT LIN(1). "The radius (for circle) has a minimum value which is half
 the
15148
         PRINT "length of the first surface: approximately ":R0 max;" inches."
15150
                           You are free to choose any value for n3 for the GRIN ca
se."
15160
         PRINT LIN(2), "PRESS CONT"
15170
         PAUSE
15100
         G#="N"
15190
         INPUT "ARE YOU GOING TO USE GRIN ? Y/N",G#
```

```
15200
            IF (G$="N") OR (G$="n") THEN N2
         PRINT " of refraction ( default = "; Nmin;")"
15218
15220
15238
15248
          PRINT "
                             2) Nmax = maximum value of the index (not required for
circle.
15250
         PRINT "
                                         ( Default = ":Hmax:")"
15268
         PRINT "
                              3) RO_max = radius from the origin at which the maximum
15279
         PRINT "
                                            value of the index occurs. ( MINIMUM = ";R8
_max;")"
15286
         INPUT "HHICH ONE : CIRCLE (C) OR PARABOLA (P) ( DEFAULT * C ) ? C/P", Gri
n$
15290
         INPUT "WHAT IS Nain ?", Nain
15390 IF (Grins="C") OR (Grins="c") THEN N3
15310 INPUT "WHAT IS Nmax ?", Nmax
15320 INPUT "WHAT IS R0 max ?", R0 max
15330 N2: INPUT "WHAT IS n2 ?", N2
15340 N3: INPUT "WHAT IS n3 ?", N3
             IF (G#="N") OR (G#="n") THEN Rho_initial
15350
15368
             PRINT LIN(2), "NOTE: When the parameter data is printed, the values
of "
15378
             PRINT "
                            the index at the first surface intercept will be "
             PRINT "
                            printed in the following manner:
15388
             PRINT *
15398
                              n(8) = 2.3543
                                                   n(9) = 2.3567
                                                                       n(10) = 1.9876"
             PRINT "
15400
                            The subscript indicates the number of the ray intercepti
ng"
             PRINT " the first surface."
PRINT LIN(2), "PRESS CONT"
15418
15420
15430
             PAUSE
15440 Rho_initial:PRINT PAGE,"
                                      The rays incident on the first surface are "
15450
                     PRINT "initially assumed to be parallel to the X-axis.
                     PRINT LIN(2),"
15469
                                       If you want to trace rays which are at an ang
15478
                     PRINT "other than zero (8) degrees with respect to the X-axis.
15498
                     PRINT "then key in the value of the angle (in degrees) with "
15498
                     PRINT "respect to the X-axis.
                     INPUT "RHO ?", Rho initial Rho initial =-1+ABS(Rho initial)
15300
15518
                     Trhoi=TAN(Rho_initial)
FINT PAGE. The GLM is assumed to be assumed to be symmetric
15520
15530 Y_bullet: PRINT PAGE,"
about the
15548
                   PRINT "longitudinal axis. The maximum value of the GLM radius is
15550
                   PRINT "called Y_bullet whose default value is ";Y_bullet;" inche
15360
                  PRINT LIN(2), " If your design requires a different value, plea
...
15570
                   PRINT "enter that value now."
15500 INPUT "Y_BULLET (INCHES) ?",Y_bullet
15500 Yb=Y bullet
15600 Aperture: PRINT PAGE," The aperture is the d
                                    The aperture is the difference in radial distance
 from the GLM axis'
15619
                  PRINT "projected onto the first surface, into which light is allo
wed to enter"
                  PRINT "the GLM optical system. The parameters are :"
PRINT LIN(1)," 1) Ya : the minimum Y-value of the aperture"
15620
                  PRINT LIN(1),"
15630
15646
                                       (default value =";Ya; "inch )"
15658
                  PRINT "
                                 2) Yb : the maximum Y-value of the aperture"
                  PRINT "
                                       (default value =";Yb; "inch) and is < Y_bulle
15668
...
                  IMPUT "WHAT IS YA (INCHES) ?",YA
IMPUT "WHAT IS YB (INCHES) ?",YB
15678
15688
                    IF Ya>=Yb THEN BEEP
IF Ya>=Yb THEN PRINT "Ya must be < Yb. Please enter again."
15690
15700
15710
                     IF Ya>=Yb THEN GOTO 15678
```

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15720
                  Aperture=Yb-Ya
                     IF YaC THEN Add_ray=1
15730
15748 Hray: PRINT PAGE,"
                              The program will trace"; Nray; " rays through the syste
m usless
15758
            PRINT "you specify another value"
15760
            INPUT "
                      How many rays do you want the program to trace?", Nray
15770
            Nray=IHT(ABS(Hray))
15788
               IF Nray(1 THEN Hray=10
15798 IF (Gs="Y") OR (Gs="Y") THEN Date 15999 Digitize_: PRINT PAGE," The interval between (8 \leq Y \leq ;";Y_bullet;")
and (-";Y_builet;" ( Y < 0) have been divided"

5810 PRINT "into";N_increment;" increments to determine ray density.
15810
15829
                   PRINT LIN(1), "If you want to change the number of increments, p
lease do so now."
                   PRINT LIN(2), "The amximum number of increments is 1980."
INPUT "NUMBER OF INCREMENTS ?", N_increment
N_increment=INT(ABS(N_increment))
IF N_increment(1 THEN N_increment=188
15838
15849
15858
15868
15876 Date: PRINT PAGE
15888
            INPUT "What is today's date ?", Dates
                 IF (G$="Y") OR (G$="y") THEN Gymnastics
15890 Start:
15900
               PRINT PAGE.
                                The second surface must be input as polynomial of de
gree "
15918
               PRINT "16 or less, defined as a function of Y C x=f(y) for (x,y) sy
sten 3"
15928
               PRINT "If you have not fit a curve to your data, then go to the uti
lities '
               PRINT "library, tape two and load REGD. "
15938
               PRINT "NOTE: 1) Use printer code 0 for a hard copy"
PRINT " 2) Invert the X and Y values for the positive branch"
15949
15950
               PRINT " 3) Key in (Y,-X) for the negative branch"
PRINT LIN(1), "NOTE: The negative branch is the second surface in
15960
15970
15980
               PRINT "
                                        the lower half plane"
15990
               PRINT LIN(1),"
                                  If this is the case, then PRESS STOP, then REWIND
T15 "
16888
               PRINT "fit your curve using the utilties library."
               PRINT LIN(1)," If not, then PRESS CONT."
16010
16828
               PALICE
16030 Coef_data: PRINT PAGE
                                        ! THE FOLLOWING DATA ARE ARRANGED AS FOLLOWS:
                                          DATA CURVE No.
16848
                                          DATE HP, NN, N
DATE HP, NN, N
DATE RPOS COEFICIENTS X=F(Y) FOR Y>0
DATE RNEG COEFICIENTS X=F(Y) FOR Y<0
16858
16060
16070
                                          DATA Y=F(X) COEFICIENTS
16000
16090
16190
                               ! CURVE No. DHE
16110
16120
                    DATA .5003067966,1.15219319,3.0130759,-3.4182912,1.39217781
16130
                    DATA .5003067966,-1.15219319,3.0130759,3.4182912,1.39217781
16140
                    DATA -.45216186,1.18544887,-.66358797,.25854923,-.834174838
16158
16160
16178
                    DATA 2
                              ! CURYE No. 16
16188
                    BATA 3.3.3
                    DATA 1.5193756399,2.27918152,-2.5238983,1.63847831
14190
                    DATA 1.5193756399,-2.27918152,-2.5238983,-1.63847831
16280
                    BATA 3.3554752, -5.6849365, 2.959523, -.4412978
16210
16220
16230
16240
                    DATA 3
                                  ! CURVE No. 11
16250
                    DATA 6,6,3
16260
                    DATA 2.006223634,.30397,12.96206,-62.1508,125.7966,-114.0765,38
. 96194
16279
                    DATA 2.006223634.-.30397.12.96206.62.1508.125.7966.114.0765.30.
04104
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16288
                                      DATA -11.205773,13.18159,-5.328168,.767801
 16298
 16300
 16310
                                      DATA 4
                                                                    ! SURFACE NR 1 FOR n2=4. F=4 INCHES
                                      DATA 2,2,2
 16329
 16330
                                      DATA .3184601721,2.7548136449,-.3640728143
 16340
                                      DATA .3184601721,-2.7540136449,-.3640728143
 16359
                                      DATA -.1071362125,.3341667828,.02751837081
 16368
 16379
16398 Explain: PRINT " Since this program is intended to be used to evaluate 16398 PRINT "various second surfaces a method of labeling the current"
                                 PRINT "design surface has been incorporated into the algorithm."
 16488
                                 PRINT "
                                 PRINT " The program will ask you for a curve number. At that"
PRINT "time, key in any number (integer or real) you wish to use"
PRINT "identify the surface."
PRINT LIN(2), "PRESS CONT"
 16418
 16428
 16430
 16448
 16450
                                 PAUSE
                                     PRINT PAGE, "The current values of Curve and Np (the degree"
 16460 Coef_pos:
                                      PRINT "of the positive branch x = f(y) ) are:
 16478
                                      READ Curve, Np, Nn, N
PRINT LIN(1), "
PRINT "
 16489
 16490
                                                                                          Curve = "; Curve
 16589
                                                                                 Np = ":Np
                                      INPUT "HHICH CURVE ARE YOU USING (CURVE No.) ?", Curve INPUT "HHAT IS THE DEGREE OF THE POLYNOMIAL FOR THE POSITIVE BR
 16510
16528
ANCH (Np) ?", Np
16538
                                     PRINT LIN(2)
16340 Quick_loop p: PRINT "NOTE: These are the current values of the positive branch coefficients:"
 16350
                                            PRINT
 16560
                                            FOR I=9 TO Np
 16570
                                                READ Apos(1)
                                                 PRINT USING 16598; I, Apos(I)
 16589
 16590
                                                 IMAGE "Apos("4D") = ",K
 16690
                                            HEXT I
 16610
                                            PRINT
                 Z1=Apos(8)
16629
16630
                  Anuse"NONE"
                  INPUT "ARE YOU GOING TO CHANGE ANY OF ALL OF THE COEFICIENTS? SOME/ALL/
16648
HONE
16650
                      IF (Anys="NGNE") OR (Anys="name") THEN Name_p
16669
                      IF (Anys="SOME") OR (Anys="some") THEN Some_p
             All_p:PRINT
 16679
 16680
                            PRINT "Please key in the coeficients, beginning with the constant:"
                            FOR I=0 TO Np
INPUT "", Apos(I)
 16690
 16700
 16716
                                 PRINT USING 16598; I. Apos(1)
16720
                            NEXT I
 16730 None_p: PRINT
14748
                               Y4="N"
                               INPUT "DO YOU NEED TO MAKE ANY CORRECTIONS ? Y/H",Y#
16750
16790 INPUT "NO THEM TO THEM FOR THE CORRECTIONS : TO THE CORE OF 
                               Y$#"Y'
16000
                              INPUT "IS THAT ALL",Y#

IF (Y#="y") OR (Y#="y") THEN Coef_neg

IF (Any#="SOME") OR (Any#="some") THEN Some_p
16010
 16020
16030
                              GOTO Some_p
16848
16850 Coef_neg: PRINT PRGE, "The current values of Curve and Hn (the degree"
16869
                                  PRINT "of the negative branch x = f(-y) > are:"
16070
                                  PRINT LIN(1),"
                                                                              Curve = ";Curve
Nn = ";Nn
16888
                                  PRINT
16890
                                  INPUT "MHAT IS THE DEGREE OF THE NEGATIVE BRANCH POLYHOMIAL (Nn)
  ?", Nn
16900 Guick_loop_n:PRINT LIN(2), "NOTE: These are the current values of the neg
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ative branch coeficients:
16918
                          PRINT
                          FOR I=0 TO No
16920
                            READ Aneg(I)
16930
                            PRINT USING 16950; I, Aneg(I)
IMAGE "Aneg("4D") = ",K
16948
16950
                          NEXT I
16968
                          PRINT
16979
           Anys="NONE"
16988
           INPUT "ARE YOU GOING TO CHANGE ANY OF ALL OF THE COEFICIENTS ? SOME/ALL/
16998
NONE ", Any*
             IF (Any = "NONE") OR (Any = "none") THEN Hone_n
17900
              IF (Anys="SOME") OR (Anys="some") THEN Some_n
17618
17920 ATT_n:PRINT
                  PRINT "Please key in the coeficients, beginning with the constant:"
17838
                  FOR I=0 TO Nn
INPUT "", Aneg(I)
17848
 17058
                    PRINT USING 16950; I, Aneg(I)
 17868
                  HEXT I
 17979
17888 None_n: PRINT
17198 TANNO YOU NEED TO MAKE ANY CORRECTIONS ? Y/N", Y8
17108 IF (Y$="N") OR (Y$="n") THEN Gymnastics
17110 IF (Y$="N") OR (Y$="n") THEN COEFICIEINT ? (B,1,2, etc)", Nnn
17120 INPUT "KEY IN THE CORRECT VALUE, THEN CONT", Aneg(Nnn)
 17898
                    PRINT USING 16958; Nnn, Aneg(Nnn)
 17140
 17150
                    Y45"Y"
                    INPUT "IS THAT ALL",Y$

IF (Ys="y") OR (Ys="y") THEN Gymnastics

IF (Anys="SOME") OR (Anys="some") THEN Some_n
 17170
 17180
                    GOTO Some_n
 17170
 17288 Gymnastics: SUBEND
 17210
 17220
                                         SUR Char
 17230
 17248
                FOR I=8 TO 79
                     IF 1=79 THEN PRINT CHR$(228)
IF 1=79 THEN 17280
 17250
 17260
                   PRINT CHR#(228);
 17279
                HEXT I
 17288
           SUBEND
 17290
 17368 SUB X2pos(X2,Y)
            OPTION BASE 0
 17310
            COM INTEGER I, J, Curve, Np, Nn, N, Ns, Nr, REAL Aneg(+), Apas(+), A(+), 21, 23, 24
 17320
  17330
  17340
            FOR I=8 TO Np
  17350
               X2=X2+Apos(1)+Y^I
  17360
            HEXT I
  17370
         SUBEND
  17388 SUB X2neg(X2,Y)
17388 OPTION BASE 8
  17390
            COM INTEGER 1, J, Curve, Np, Nn, N, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4
  17400
  17410
  17420
             FOR I=8 TO No
  17430
              X2=X2+Aneg(I)+Y^I
  17440
             HEXT I
  17450
          SUBEND
          SUB Index_p(X,Y)
OPTION BASE 0
  17460
  17470
            COM INTEGER I, J, Curve, Np, Nn, Ns, Nr, REAL Aneg(+), Apos(+), R(+), Z1, Z3, Z4 COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2 COM NI, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
  17490
  17510
  17520
             COM INTEGER Y@_1oop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_tota
  17530
```

The second second

COM INTEGER Linecount, Linemax

17540

**(**)

```
COM INTEGER Pselect, Hpib
17550
17568
17579
         COM REAL Mmin, Mmax, RO_max
17588
         DEG
17598
          Xm2=.68/Talpha
                                     + FRQM y=mx + b AND Ymax = 1.2
17600
17610
          Ym2=Xm2+Taipha
            IF RO_max(SQR(Xm2^2+Ym2^2) THEN Ro_max=SQR(Xm2^2+Ym2^2)
17628
          Radius=SQR(X^2+Y^2)
17630
          R2=R0_max^2
17640
17650
          K=(Hmax-Hmin)/R2
17660
          B=(Radius-R0_max)^2
17678
          N2=Hmax+K+B
17680
       SUBEND
       SUB Index_c(X,Y)
OPTION BASE 0
17690
17798
17710
         COM INTEGER I, J, Curve, Np, Nn, N, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4
COM Alpha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2
COM N1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
17728
17738
17748
17758
17768
          CON INTEGER YS_loop, Nray, Rdd_ray, Surf_no, Flag, Flag2, N_increment, Hit_tota
17770
          COM INTEGER Linecount, Linemax
17780
          COM INTEGER Pselect, Hpib
17790
17888
          COM REAL Hmin, Hmax, R6_max
17819
17929
          DEG
                                     ! FROM y=mx + b AND Ymax = 1.2
17839
          Xm2=.68/Taipha
          Ym2=Xm2+Talpha
17840
          TF Re_max(SQR(Xm2^2+Ym2^2) THEN Ro_max=SQR(Xm2^2+Ym2^2) Radius=SQR(Xm2+Y^2)
17850
17866
          AmRe_max^2
B=(Radius=Re_max)^2
17878
          C2=A-B
17890
          N2=Nain+SQR(C2)
17910
       SUBEND
17928 SUB Density
17930
          OPTION BASE 0
17940
          COM INTEGER I, J, Curve, Np, Nn, N, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4
17950
          COM Ripha, Talpha, Rho, Trho, Rho_initial, Trhoi, Phi, Tol, Norm, Alpha2
COM N1, N2, N3, Percent_image, Ya, Yb, Aperture, Y_bullet
 17960
 17970
 17900
          COM INTEGER YO_loop, Nray, Add_ray, Surf_no, Flag, Flag2, N_increment, Hit_tota
17990
          COM INTEGER Linecount, Linemax COM INTEGER Pseict, Hpib
12000
10010
10020
18030
          COM REAL Hain, Haax, RO_max
          CON Ray traces, Bigitizes, Grins, Gs, Grincs, Plots, Bates
10050
          CON X(+), Y(+), Xc(+), N(+), R(+)
 10070
          COM Rho(+), Phi(+), C(+), Y3(+), His(+)
          INTEGER Inc, K, L, M, Lines
 10100
           ! THIS ROUTINE COMPUTES THE RAY DENSITY IN ONE DIMENSION.
 16116
           I ASSUMPTIONS:
 18120
                  1) THE POINT OF MAXIMUM RAY DENSITY HAS BEEN FOUND VIA A
 10130
                     DIGITIZE STATEMENT.
 18148
                  2) THE VALUES OF Y3 HAVE NOT BEEN CHANGED TO REFLECT THE NEW VALUE OF Z3
 10150
 18160
 10170
 18180
          PRINTER IS 16
 18190 Initialize_: Nr=-I
```

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```
18299
                     Ns=-3
18218 Re_draw: FOR I=1 TO Nray
18228
                   MesMes3
18238
                   Hs=Ns+5
18248
                   Anxe(1)
18258
                   X=X(Ns)
18260
                   Y=Y(Ns)
18279
                   Rho=Rho(Nr)
18288
                   Trho=TAN(Rho)
18290
                     IF ACZ1 THEN Negative
                     IF Rho=8 THEN Hext_i
18388 Positive:
                                               ! TOTAL INTERNAL REFLECTION AT X2POS
                   GOTO Same
18328 Negative:
                     IF Y(=-Y_bullet THEN Next_i ! Y2=-Y_bullet =>THE RAY MISSED
X2 POS/NEG
                    · IF Rho=0 THEN Next_i
18336
                                                ! TOTAL INTERNAL REFLECTION AT X2NEG
18348 Same:
                   Deltay=(Z3-X)+Trho
18350
                   Y3=Y+Deltau
18368
                   X(Ns+1)=23
18378
                   Y(Ns+1)=Y3
18388 Next 1: NEXT I
18398 Y3_array: J=6
18400
                  FOR I=1 TO Nray
10410
                    Y3(J)=Y(5+1-2)
18426
                    J=J+1
10430
                  HEXT I
18448 Hit_zero: MAT Hit=ZER(2881)
                                          I ZERO THE ARRAY
18458
                                          ! FIND THE NO. OF HITS IN THE
                  Ylast=-Y bullet ! INT:
Belta=Y_bullet/N_increment
Ynext=Ylast+Belta/2
18460
                                          ! INTERVAL ( -Y_BULLET, -Y_BULLET+DELTA/2)
18479
18490
18490
                  Hit(Inc)=8
18500
                  Jud
18518
                  FOR I=1 TO Nrau
18520
                      IF (Xc(I)(Z1) AND (Y3(J)=0) THEN Next_j ! IGNORES NEGATIVE
19530
                                                                      ! BRANCH RAYS
18546
                      IF (Y3(J)>=Ylast) AND (Y3(J)(Ynext) THEN Hit(Inc)=Hit(Inc)+1
18550 Next_j:
                    J=J+1
18560
                  HEXT I
18578 Hit_middle: ! FIND THE No. OF HITS IN THE INTERVAL
                     (-Y_BULLET+DELTA/2, Y_BULLET-DELTA/2)
18589
18598
                    FOR L=1 TO 2=N_increment-1
18600
                      Inc=Inc+1
18618
                      Hit(Inc)=@
18620
                      Ylast=Ynext
18630
                      Ynext=Ylast+Delta
18648
                      K=0
                         FOR I=1 TO Hray
                             IF (Xc(1)(Z1) RHB (Y3(K)=0) THEN Next k ! IGNORES ! NEGATIVE BRANCH RAYS
19600
                             IF (Y3(K)>=Ylast) AND (Y3(K)(Ynext) THEN Hit(Inc)=Hit(
Inc)+1
18690 Next_k:
                           K=K+1
                        NEXT I
18700
                      HEXT L
18710
18720 Hit_last: Inc=2*N_increment ! FIND THE No. OF HITS IN THE LAST INTERVAL
18730 Hit (Inc)=0 ! CY_BULLET-DELTA/2, Y_BULLET?
18740
                  Het
                  Ylast=Y_bullet=Belta/2
Ynext=Y_bullet
FOR I=1 TO Nray
18750
18760
10770
                      I=1 TO Mray

IF (Xc(I)(Z1) AND (Y3(M)=8) THEN Next = ! IGNORES

T NEGATIVE BRANCH RAYS
18780
18790
10000
                      IF (Y3(H)>=Ylast) RNB (Y3(H)(=Ynext) THEN Hit(Inc)=Hit(Inc)+
18010 Hext_m:
                    M=H+1
18826
                  NEXT I
18830 Hormalize: Hit_total=0
                                                    ! HORMALIZE THE No. OF HITS ON THE
```

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```
FOR I=0 TO 2+N increment ! IMAGE PLANE Hit total=Mit_total+Hit(I) ! No. OF HITS MEXT I
                                                        ! IMAGE PLANE (23) TO THE TOTAL
12242
18656
10060
18876
                    IF Hit_total=0 THEN None
FOR I=0 TO 2*N_increment
Hit(I)=Hit(I)/Hit_total
18280
18898
18900
                    NEXT I
18910
                                                             ! % OF RAYS THAT ARRIVE AT THE
                    Pct=Hit_total/Nray
Percent_image=Pct+188
18928 Hone:
                                                             IMAGE PLANE
18930
                                                             ! PLOT AND LABEL THE AXES
18948 Graph:
                  CALL Plos
18950
                       IF Hit_total=8 THEN Label_
                                                             ! DRAW THE HISTOGRAM
18968 First_bar:
                    Xlast=-Y_bullet
                    Xnext=Xlast+Delta/2 ! INTERVAL [-Y_BULLET, -Y_BULLET+DELTA/2)
18970
18988
                    Inc=4
                    IF Hit(Inc)=0 THEN Hiddle_bars
CLIP Xlast, Xnext, 0, Hit(Inc)
18998
19000
19010
                    FRAME
19828 GOSUB Belt
19838 Middle_bars: FOR I=1 TO 2+N_increment-1
                                                           ! INTERVAL
                                                 ! [-Y_BULLET+DELTA/2, Y_BULLET-DELTA/2)
                         Inc=Inc+1
19848
19050
                         Xlast=Xnext
19860
                         Xnext=Xlast+Delta
                         IF Hit(Inc)=0 THEN Next i m
CLIP Xlast, Xnext, 0, Hit(Inc)
19070
19080
19090
                         FRAME
19100
                         GOSUB Delt
IF Hit(Inc)=0 THEN Label
CLIP Xlast, Xnext, 8, Hit(Inc)
 19156
19160
                   FRAME
19170
                   GOSUB Delt
19188
19190 Label : LDIR 0
19200 LORG 2
 19210
                 SETGU
                 MOVE 2,2
 19220
                 CSIZE 2.5
 19238
                 LABEL "PRESS CONT"
 19248
 19250
                 SETUU
 19260
                 CSIZE 15/4.54
 19270
                 BEEP
 19200
                 HAIT 258
 19290
                 MEEP
                 PAUSE
 19300
                 EXIT GRAPHICS
 19310
               SUBEXIT
 19326
 19338 Delt:
              Lines=10
               Delt=(Xnext-Xlast)/Lines
 19340
 19350
               X=X1ast-Belt
               FOR Jel TO Lines
 19360
                 X=X+Delt
 19370
                 HOVE X,8
BRAW X,Hit(Inc)
 19300
 19390
               NEXT J
 19400
 19410
            RETURN
 19420
          SUBEND
 19430 SUB Picture
 19448 Scale_: GCLEAR
                 PLOTTER IS 13, "GRAPHICS"
 19450
                 GRAPHICS
 19460
19470 LIMIT 0,184,0,140
19480 SCALE -20,152,4,-55,55
19490 AXES 5,5,0,0,10,10
19500 Label_: MOVE 20,45
```

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```
19510 LABEL "THE PROBLEM"
19520 MOVE 20,44
19530 DRAW 50,44
19540 Draw_body: MOVE 0,0
19550 DRAW 74,30
19560 DRAW 184,30
                                     HOVE 0,0
DRAH 74,-30
  19578
  19580
  19590
                                     DRAH 184,-38
 19600 Draw_inlet: MOVE 78,35
19610 DRAW 88,38
19620 DRAW 184,31
19630 MOVE 78,-31
                                       DRAW 184,38
MOVE 78,-35
 19648
                                       DRAH 80,-38
DRAH 184,-38
 19660 Second_surf: MOVE 30,0
19670 DRAW 35,5
19680 DRAW 40,9
                                         DRAW 45, 13
 19690
                                         DRAW 50,15
DRAW 74,30
  19710
  19720
                                         HOVE 39,8
 19730
19740
19750
19760
19770
                                         DRAW 35,-5
                                         DRAH 48,-9
                                         DRAH 45,-13
                                         DRAH 50,-15
                                         DRAH 74,-38
 19776
19788 Ray: MOVE 0,15
19790 DRAW 40,15
 19800 DRAM 45,13
19810 DRAM 184,-14
19820 Image_plane: MOVE 80,38
 19630
                                        LINE TYPE 4
 19840
                                        DRAN 80,-38
 19858 Label_picture: HOVE 65,-58
19868 LINE TYPE 1
19878 LABEL "5/54 GLH"
 19060
19070
19080
19090
                                            HOVE 85,15
LABEL "IHAGE PLANE"
HOVE 15,2
LABEL "ALPHA"
 19900
 19910
                                            LABEL "HEPA"
HOVE 18,8
DRAM 8,2.5
HOVE 5,18
LABEL "INCIDENT RAY"
 19920
 19930
 19940
 19950
                                             MOVE 35,2
19970
19900
19990
20000
                                            LABEL "Z1"
                                            HOVE 35,2
                                            DRAH 30,0
HOVE 113,2
20000
20010
20020
20030
20040
20050
20060
20070
20000
20000
                                            LABEL "Xc"
                                           HOVE 113,2
DRAH 110,0
HOVE 92,2
LABEL "23"
HOVE 82,2
                                            DRAH 80,8
HOVE 130,3
LABEL "C"
                                           HOVE 131.5,1.5
LABEL "L"
HOVE 5,-10
LABEL "n1"
HOVE 30,-10
LABEL "n2"
20100
20110
20120
20130
20140
20150
                                            HOVE 30,-18
20160
```

```
LABEL "n3"
20170
20100 Finished: HOVE 15, -55
20190 ! LABEL "PRESS CONT"
20200 BEEP
                    HAIT 250
20210
                    BEEP
20220
                    PAUSE
20230
                    EXIT GRAPHICS
20240
20250
            SUBEND
20260 SUB X2p(X,Y)
20278
          OPTION BASE 0
28288
          COM INTEGER I, J, Curve, Np, Nn, N, Ns, Nr, REAL Aneg(*), Apos(*), A(*), Z1, Z3, Z4
20290
28300
20318
          DEG
          FOR 1=0 TO N
Y=Y+A(1)+Y^1
20320
20330
          NEXT I
20340
20350
         SUBEND
20360 SUB X2n(X,Y)
20370 OPTION BASE 6
20390
          CON INTEGER I, J, Curve, Np, Nn, Ns, Nr, REAL Aneg(+), Apos(+), A(+), Z1, Z3, Z4
20400
 20420
             CALL X2p(X,Y)
             Y=-1+Y
 28448
          SUBEXIT
 20450 SUB Min(Xm(+),X,INTEGER M)
20460 OPTION BASE 0
 20470
 29488 ! DIM Xm(H)
 20490
          X=Xm(0)
 20510
          FOR I=1 TO M
X=Min(X,Xm(I))
 20530
          HEXT I
 20540
         SUBEND
 28556 SUB Max(Xm(+),X,INTEGER H)
 20560
          OPTION BASE 9
 20570
 20500 ! DIH Xm(H)
 20590
 20610
20610
20620
20630
20640
           X=Xm(B)
          FOR I=1 TO M
X=MIN(X,Xm(I))
           NEXT I
         SUBEND
```

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### APPENDIX C

## POLYNOMIALS USED FOR THE SECOND SURFACE

### A. INTRODUCTION

The following discussion compares the attributes of three analytic expressions, in polynomial form, used as second surfaces for a conical lens. The lenses are compared in terms of the individual lens ability to cause some or all of the incident light rays to converge to a point. The points of ray convergence are referred to as "focal" points although they are not focal points in the standard usage of the term. Lens designers have developed a system of standards used as figures of merit to compare one lens to another. These standards include spherical abberation, coma, tilt, astigmatism and others. The figures of merit have not been calculated because the three curves discussed in this appendix are known to be completely unsatisfactory to use as refracting surfaces. The purpose of the thesis is to discover which properties of a curve to investigate in order to lead to usable design. Therefore an intuitive comparison of ray diagrams, histograms of ray distributions and the set of basic design criteria described in chapter III are the basis for the discussion of curves A, B and C in this appendix.

### B. CURVE A

curve A, shown in figure C-1 was the first analytic expression used as a second surface to produce a ray diagram.

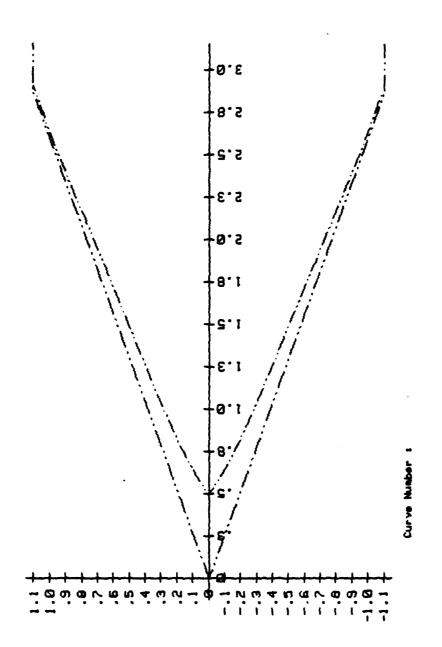


Figure C-1. Conical Lens with the Second Surface Defined by Curve A.

The curve was calculated by otaining the data listed in Table C-1 from an arbitrary hand drawn curve. These data were used as the input to a regression analysis routine in the HP-9845B utilities library. Since TRACE requires the second surface to be expressed as a polynomial function of y, three curves were fit to the data. Table C-II contains the coefficients for each of the polynomials. The first polynomial relates the radial distance from the GLM axis to the distance along the GLM axis, i.e. radius = f (distance along the GLM axis). The remaining two are required by TRACE for ray tracing and graphics purposes. The second expression relates the distance along the GLM axis to the radius from the axis in the upper half-plane; i.e. distance along the GLM axis = f(radius). The third expression relates the distance along the GLM axis to the radius in the lower half-plane; i.e. distance along the GLM axis = f(-radius). All linear dimensions are in inches.

TABLE C-I
DATA POINTS FOR CURVE A

THE WAY

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 $C^i$ 

y = f(x)*	x = f(y)*	x = f(-6) *
(Ordinate, Abscissa)	(Ordinate, Abscissa)	(Ordinate, Abscissa)
Ø.5ØØ,Ø.ØØ	Ø.ØØØ,Ø.5ØØ	Ø.ØØØ,Ø.5ØØ
Ø.6ØØ,Ø.Ø69	Ø.Ø69,Ø.6ØØ	-Ø.Ø69,Ø.6ØØ
Ø.7 <b>ØØ</b> ,Ø.138	Ø.138,Ø.7ØØ	-Ø.138,Ø.7ØØ
Ø.8ØØ,Ø.188	Ø.188,Ø.8ØØ	-Ø.188,Ø.8ØØ
Ø.9ØØ,Ø.238	Ø.238,Ø.9ØØ	-Ø.238,Ø.9ØØ
1.000,0.281	Ø.281,1.ØØØ	-0.281,1.000
1.500,0.500	ø.5øø,1.5øø	-0.500,1.500
2.000,0.731	8.731,2.000	-9.731,2.000
2.500,0.938	Ø.938,2.5ØØ	-0.938,2.500
2.900,1.100	1.100,2.900	-1.100,2.900

<sup>\*:</sup> For x = distance along the GLM axis and y = radial distance from the GLM axis.

TABLE C-II

POLYNOMIAL COEFFICIENTS FOR CURVE A

Coefficier Number a <sub>i</sub>	y = f(x)*	Positive Branch x = f(y)*	Negative Branch x = f(-y)*
a <sub>o</sub>	<b>-Ø.</b> 45216186	Ø.5ØØ3Ø67966	Ø.5ØØ3Ø67966
a <sub>i</sub>	1.18544007	1.15219319	-1.15219319
a <sub>2</sub>	-Ø.66358797	3.Ø138759	3.Ø138759
a <sub>3</sub>	ø.25ø54923	-3.4182912	3.4182912
<b>a</b> 4	-Ø.Ø34174838	1.39217781	1.39217781

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<sup>\*:</sup> For x = distance along the GLM axis and y = radial distance from the GLM axis.

A ray diagram using TRACE, which is shown in figure C-2, demonstrates that curve A has the ability to focus some of the rays to a point near the wall of the GLM at a distance of 21.18 inches along the GLM axis. Figure C-3 is the histogram of the ray distribution for figure C-2 and shows a maximum at 1.08 inches. If this distribution were rotated about the GLM axis, the two dimensional distribution would be a set of concentric rings centered on the GLM axis with the most intense ring at a radius of 1.08 inches. Although this ray pattern is unsatisfactory, the fact that some rays converged to a focus was encouraging.

The converging rays were coming from the middle region of the curve. The slope of the middle region of the curve is slightly larger than the slope of the first surface. The slope of the regions above and below the middle region have slopes which are approximately the same as and greater than the slope of the first surface respectively. The ability of the middle region to focus light rays suggested the existence of a range of slopes which would cause convergence of light rays. The light rays which intercept the second surface in the lower half-plane are totally internally reflected because of the large angle of incidence. Total internal reflection occurs when Snell's Law  $\sin\theta_R = (n_2/n_3)\sin\theta_I$  results in  $\sin R \ge 1$ . The critical angle of incidence  $\theta_C$  is where  $\sin\theta_R = 1$  and any angle greater than  $\theta_C$  results in total internal reflection. The range appears to be in a narrow

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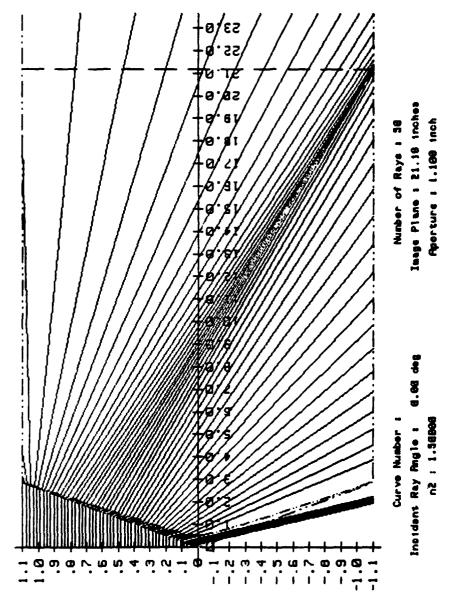


Figure C-2. Ray Diagram for a Conical Lens Using Curve A as the Second Surface.

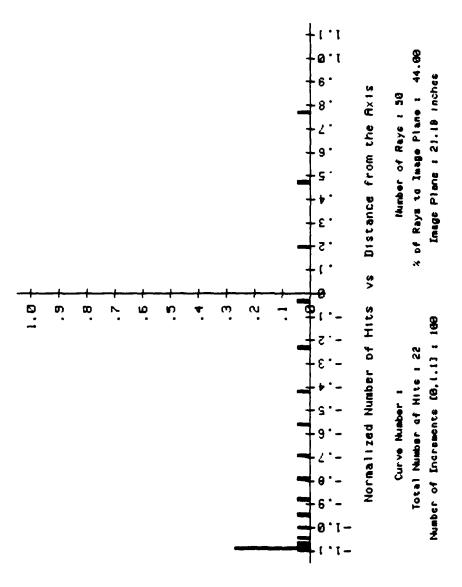


Figure C-3. Histogram of the Ray Distribution on the Image Plane Shown in Figure C-2.

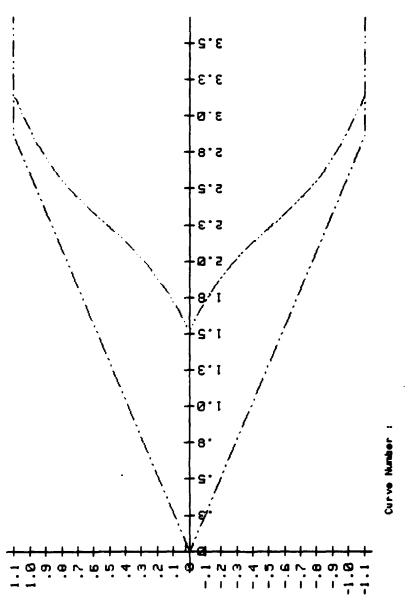
band with the minimum value greater than the value of the cone angle,  $\alpha$ . Since the curve is concave with respect to the first surface, the next step of the investigation was to study curves with the appropriate slope comparable with curve A and regions concave and convex with respect to the first surface. These two criteria were the basis for choosing curves B and C for further investigation.

## C. CURVE B

Curve B, shown in figure C-4 was chosen because the analytical expression which describes the curve exhibits regions similar to those discussed for curve A. The shape of curve B is smooth with an inflection point providing regions concave and convex with respect to the first surface. The data used to generate the analytical expression for the curve are listed in Table C-III. Three analytic expressions were calculated as for curve A. The coefficients for the three polynomials describing curve B are listed in Table C-IV.

The ray diagram in figure C-5 demonstrates the ability of curve B to cause some of the light rays to converge to a "focal" point. A ray diagram with an image plane located at the point of maximum ray density is shown in figure C-6. Although this ray distribution is not satisfactory the distribution of rays is relatively better than the ray distribution for curve A shown in figure C-2.

The ray distribution of curve B is better than that for curve A because the point of ray convergence is closer to



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Conical Lens with the Second Surface Defined by Curve B. Figure C-4.

TABLE C-III

DATA POINTS FOR CURVE B

y = f(x) *	x = f(y) *	x = f(-y) *
(Ordinate, Abscissa)	(Ordinate, Abscissa)	(Ordinate,Abscissa)
1.500,0.000	Ø.ØØØ,1.5ØØ	g.ggg,1.5gg
1.700,0.075	Ø.Ø75,1.7ØØ	-0.075,1.700
1.999,9.299	Ø.2ØØ,1.9ØØ	-Ø.2ØØ,1.9ØØ
2.100,0.394	g.394,2.1gg	-9.394,2.189
2.300,8.569	Ø.569,2.3ØØ	-Ø.569,2.3ØØ
2.500,0.744	ø.744,2.5ØØ	-9.744,2.589
2.700,0.888	Ø.888,2.7ØØ	-ø.888,2.7øø
2.900,1.000	1.000,2.900	-1.888,2.988

<sup>\*:</sup> For x = distance along the GLM axis and y = radial distance from the GLM axis.

TABLE C-IV

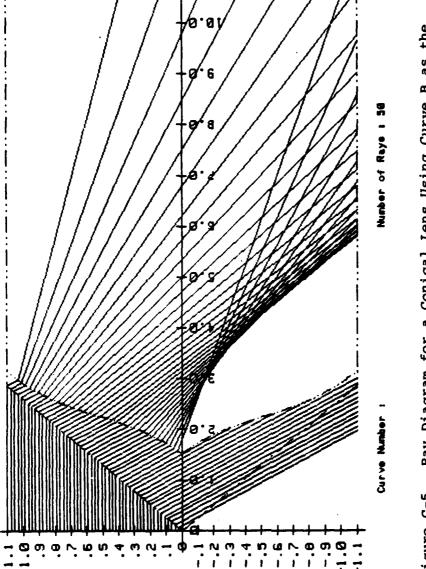
POLYNOMIAL COEFFICIENTS FOR CURVE B

Coefficient Number a	y = f(x)*	Positive Branch x = f(y)*	Negative Branch x = f(-y)*
a <sub>o</sub>	3.3554752	1.5193756399	1.5193756399
a <sub>i</sub>	-5.6849365	2.279198152	-2.279198152
<b>a</b> 2	2.959523	-2.523Ø983	-2.523Ø983
<b>a</b> 3	-Ø.4412878	1.63047031	-1.63047031

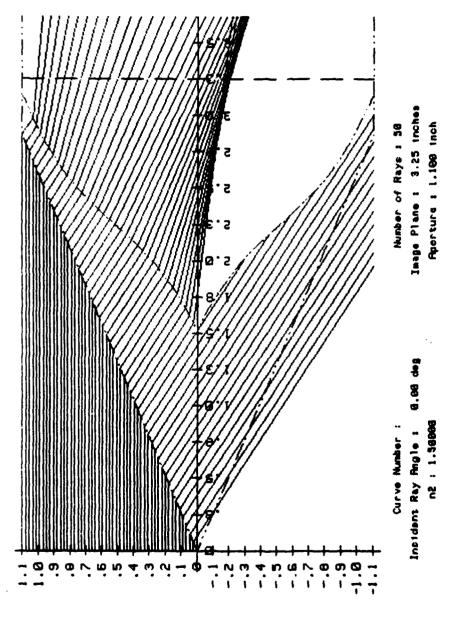
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<sup>\*:</sup> For x = distance along the GLM axis and

y = radial distance from the GLM axis.



Ray Diagram for a Conical Lens Using Curve B as the Second Surface. Figure C-5.

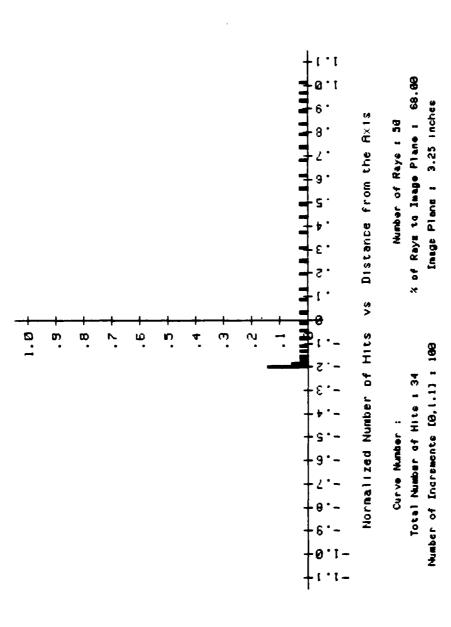


Ray Diagram Using Curve B with Image Plane at 3.25 Inches. Figure C-6.

both the lens and the GLM axis. The histogram for curve B in figure C-7 shows the point of maximum ray density is located at a radius of approximately 0.2 inch from the GLM axis. The point of maximum ray density for curve A is at a radius of approximately 1.08 inch from the GLM axis. Although curve A causes more of the rays which strike the image plane to focus than curve B does, the ability to achieve a short focal length is more desirable and therefore curve B is judged to be better than curve A. A second factor which must be taken into account is the fraction of rays transmitted through the lens. Curve A transmits 84% (42 of 50) of the incident rays through the lens. Curve B transmits 68% (34 of 50) of the light rays through the lens. The fraction of transmitted rays could be increased by moving the second surface forward and making the lens thinner.

The ray diagram and histogram for curve B in figures C-6 and C-7 reveal the absence of a large number of rays in the lower half-plane near the lens. Rotating the histogram about the GLM-axis would generate a set of concentric rings with the most intense at a radius of 0.2 inch from the GLM axis.

Using the ray diagram and histogram for curve A in figures C-2 and C-3 as baseline design figures for the GLM lens curve B is judged to be the superior curve of the two due to the capability of curve B to cause light rays to converge in a region relatively close to the lens and near the GLM axis.



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Histogram of the Ray Distribution and the Image Plane in Figure C-6. Figure C-7.

Curve A exhibited one convex region and one focal point.

The rays intercepting the second surface in the lower halfplane were totally internally reflected as they were for
curve A.

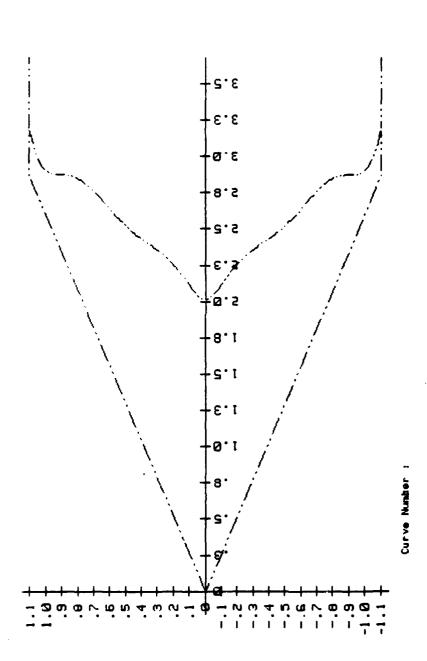
The investigation was now directed to probe the ability of a convex surface to cause convergence of the light rays at a shorter distance along the GLM axis than a concave region. Curve C was chosen because the analytic expression is a higher order polynomial with several inflection points.

#### D. CURVE C

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Curve C shown in figure C-8 was chosen because the higher order polynomial contains several inflection points. The inflection points provide regions of concave and convex surfaces. If the results for curve B are valid then curve C should cause rays to converge to several focal points, one for each convex region. The data points for curve C listed in Table C-V were obtained and the polynomial coefficients in Table C-VI were generated in the same manner as for curve A.

The ray diagram in figure C-9 show two distinct areas where rays exiting the lens from a convex region converge. The focal points possess the same characteristics as those of curve B. The focal points are located in a region close to the lens and are formed from rays emerging from a convex portion of the surface. Light rays refracted from concave regions of the lens do cross other light rays, but do not



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Figure C-8. Conical Lens with the Second Surface Defined by Curve C.

TABLE C-V
DATA POINTS FOR CURVE C

A SECTION AS

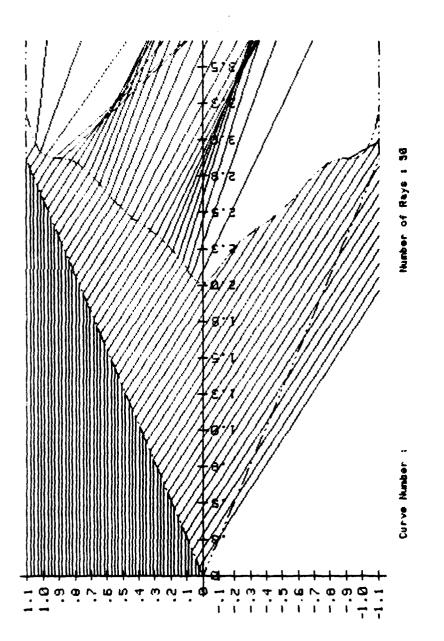
y = f(x)*	x = f(y)*	x = f(-y)*
(Ordinate, Abscissa)	(Ordinate, Abscissa)	(Ordinate, Abscissa)
2.000,0.00	Ø.ØØØ,2.ØØØ	Ø.ØØØ,2.ØØØ
2.100,0.081	Ø.Ø81,2.1ØØ	-Ø.Ø81,2.1ØØ
2.200,0.175	Ø.175,2.2ØØ	-Ø.175,2.2ØØ
2.300,0.244	Ø.244,2.3ØØ	-Ø.244,2.3ØØ
2.400,0.331	Ø.331,2.4ØØ	-Ø.331,2.4ØØ
2.500,0.500	Ø.5ØØ,2.5ØØ	-0.500,2.500
2.600,0.600	Ø.6ØØ,2.6ØØ	-\$.6\$\$,2.6\$\$
2.700,0.612	Ø.612,2.7ØØ	-Ø.612,2.7ØØ
2.800,0.744	Ø.744,2.8ØØ	-Ø.744,2.8ØØ
2.850,0.8125	Ø.8125,2.85Ø	-Ø.8125,2.85Ø
2.900,1.000	1.000,2.900	-1.000,2.900

<sup>\*:</sup> For x = distance along the GLM axis and y = radial distance from the GLM axis.

TABLE C-VI
POLYNOMIAL COEFFICIENTS FOR CURVE C

Coefficient Number <sup>a</sup> i	y = f(x)*	Positive Branch x = f(y)*	Negative Branch x = f(-y)*
a <sub>o</sub>	-11.205773	2.ØØ3622364	2.003622364
<b>a</b> 1	13.18159	ø.3ø397	-0.3Ø397
<b>a</b> 2	-5.328168	12.96206	12.96206
<b>a</b> 3	Ø.7678 <b>Ø</b> 1	-62.15Ø8	62.15Ø8
a <sub>4</sub>	Ø.ØØ	125.7966	125.7966
a <sub>5</sub>	ø.øø	-114.0765	114.0765
a <sub>6</sub>	Ø. ØØ	38.96194	38.96194

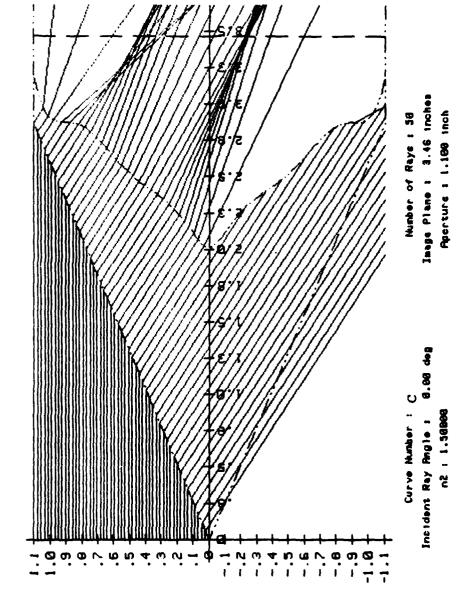
<sup>\*:</sup> For x = distance along the GLM axis and y = radial distance from the GLM axis.



the Ray Diagram for a Conical Lens Using Curve C as Second Surface. Figure C-9.

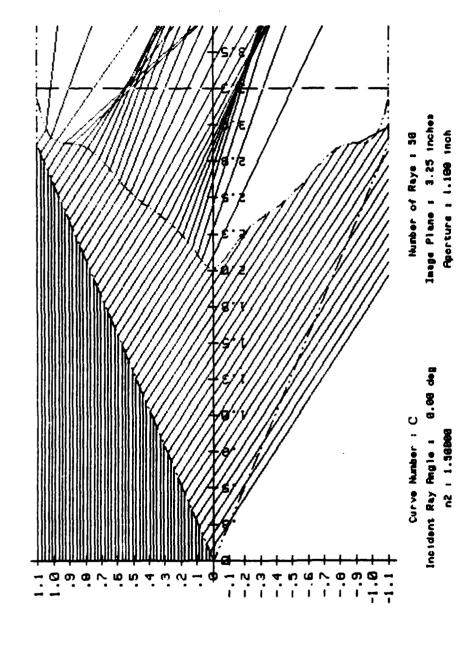
converge as a group as do the light rays from the convex regions.

Comparing the focal points caused by curve C shown in figures C-10 and 11 with figure C-1 for curve A shows that the focal point caused by curve A is located at a point 21.18 inches along the GLM axis and at a radius of -1.08 inches (21.18, - 1.08) inches. The focal points for curve C are positioned at approximately (3.46, -0.25) inches and (3.25, 0.54) inches. If the histogram in figure C-12, drawn for the image plane in figure C-10 was rotated about the GLM axis a set of concentric rings would be formed. The most intense rings would be located at radii of 0.25, 0.34 and 0.44 inch. Rotating the histogram in figure C-13 drawn for the image plane in figure C-ll would produce a similar set of rings, the most intense located at radii of 0.16 and 0.54 inch. Comparing the number of rays transmitted reveals curve A transmits 84% (42 of 50) of the incident rays and curve C transmits 58% (29 of 50) of the incident rays. However, since curve C causes light rays to converge in a region closer to the lens than does curve A, curve C is judged to be better than curve A. Also, all but one ray which intercepted the second surface of the lens using curve C in the lower half-plane experienced total internal reflection at the second surface.



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Ray Diagram Using Curve C with the Image Plane at 3.46 Inches. Figure C-10.

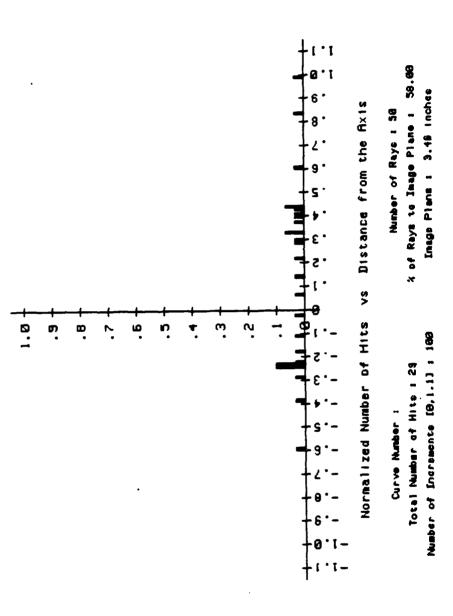


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Ray Diagram Using Curve C with the Image Plane at 3.25 Inches. Figure C-11.



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Histogram of the Ray Distribution on the Image Plane in Figure C-10. Figure C-12.

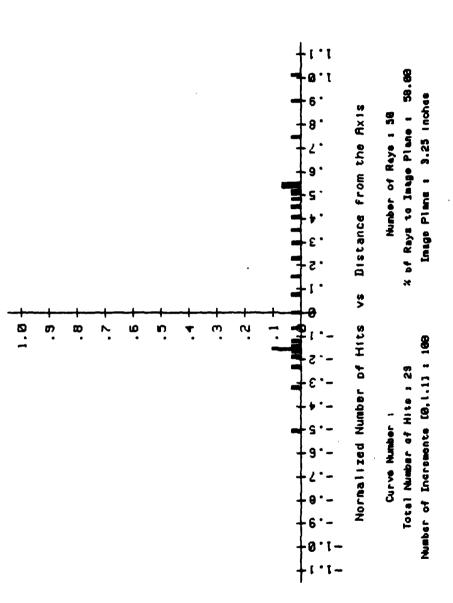


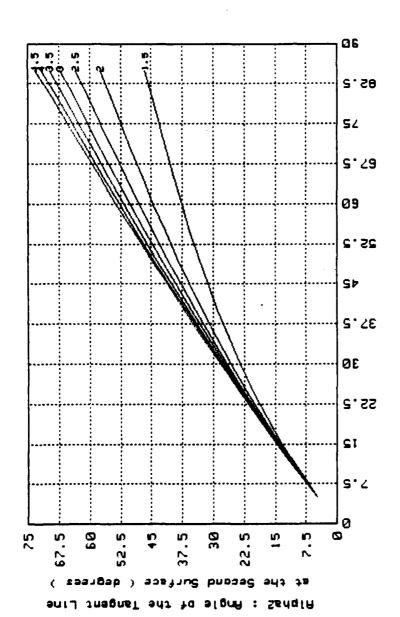
Figure C-13. Histogram of the Ray Distribution on the Image Plane in Figure C-11.

# E. CONCLUSIONS

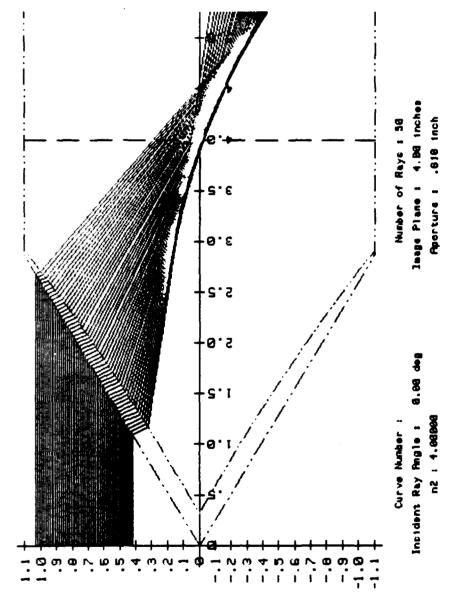
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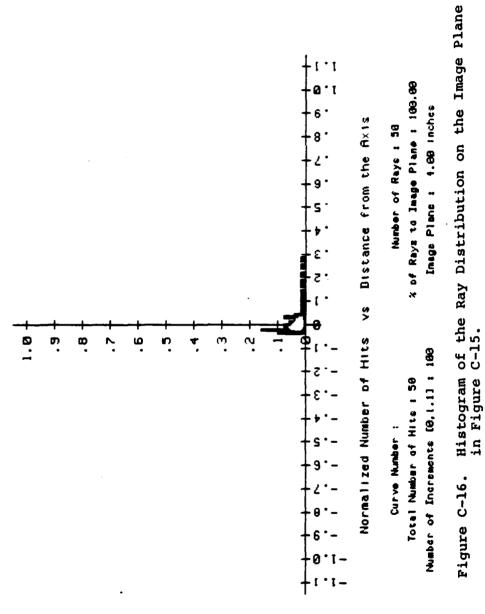
Three conclusions are drawn from the comparison of curves A, B and C. First, a range of slopes for the second surface exists which will enable the second surface to refract light to a focal point. The ray diagrams for curve A, B and C shown in figures C-2, C-5 and C-9 illustrate this relationship as well as the fact the rays which intercepted the second surface in the lower half-plane were almost all totally internally reflected. The relationship between the slopes of the first surface tana and the second surface tana2 is shown in figure C-14. Rays are refracted in the region where  $\alpha_2$  > the functional value for a given index of refraction; rays experience total internal reflection when  $\alpha_2$  < the functional value for a given index of refraction. The second conclusion is that a second surface which is convex with respect to the first surface causes light rays to converge in a region much closer to the lens than a concave lens. The third conclusion is that a single polynomial used to describe the second surface of a lens does not satisfactorily refract rays to a focus. CHART calculated surface D shown in figure C-15 for eleven rays. This is surface number one, illustrated in figure 17. A parabola was fitted to the eleven points using the HP-9845B Utilities Package. The fit appears to be quite good, especially when figure C-15 is compared to figure 17. However, when 50 rays are traced through the lens the ray diagram in figure C-15 is the result. The associated



**5** The Angle of the Tangent Line of the Second Surface as a Function of the Angle of the Tangent Line at the for Total Reflection at the Second Alpha : Angle of the Tangent Line at the First Surface (degrees) First Surface Surface. Figure C-14.



Ray Diagram for a Conical Lens Using Curve D as the Second Surface. Figure C-15.



histogram in figure C-16 shows the ray distribution on the image plane at the design focal point of 4.00 inches.

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## APPENDIX D

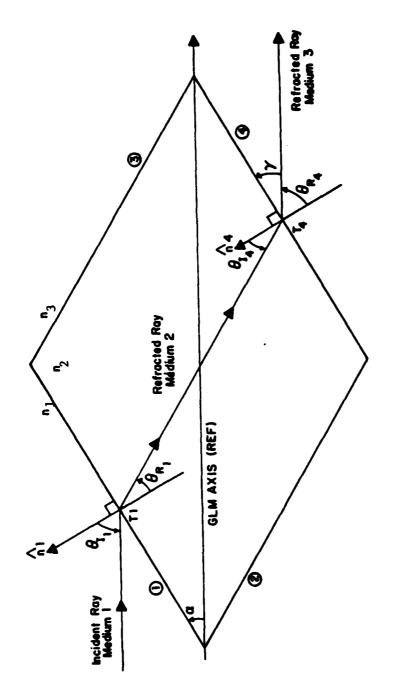
# THE USE OF A GENERAL BLOCK OF MATERIAL AS A LENS

LCDR C.L. Burmaster, Naval Postgraduate School, suggested the use of a rhombus shown in figure D-l as a refracting lens because this type of lens should transmit light without aberration. The following discussion applies Snell's Law to this lens with the following boundary conditions:

- 1) Side (1) is parallel to side (4).
- 2) Side ② is parallel to side ③ and symmetrical to the GLM axis.
- 3) The ray in medium 3 is parallel to the incident ray in medium 1.
- 4) the index of refraction of the lens is related to the indices of media 1 and 2 in the following manner:

 $n_1 < n_2$  and  $n_2 > n_3$ 

The incident ray in medium 1 makes an angle of incidence  $\theta_{\rm I}$  with  $\hat{\rm n}_{1}$  the normal to the first surface. The ray is refracted into the lens at an angle of refraction,  $\theta_{\rm R_{1}}$  with respect to  $\hat{\rm n}$ , according to the relation  $\sin\theta_{\rm R_{1}}=({\rm n_{1}}/{\rm n_{2}})\sin\theta_{\rm I}$  Snell's Law. The ray traverses the lens and forms the angle of incidence  $\theta_{\rm I_{4}}$  with the normal to surface 4. The ray is refracted according to  $\sin\theta_{\rm R_{4}}=({\rm n_{3}}/{\rm n_{2}})\sin\theta_{\rm I_{4}}$  noting that since surface  $\Phi_{\rm I_{4}}$  is parallel to surface  $\Phi_{\rm I_{4}}$ . Since the ray in medium 3 is parallel to the incident ray in medium 1  $\theta_{\rm R_{4}}=\theta_{\rm I}$ ,



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Figure D-1. Rhombus Lens.

and applying Snell's Law at surface number 1  $\sin \theta_{I} = \frac{n_{2}}{n_{1}} \sin \theta_{R_{1}}$ 

and again at surface number 4

$$\sin\theta_{R_4} = \frac{n_2}{n_3} \sin\theta_{I_4}$$

therefore equating  $\theta_{I_1}$  and  $\theta_{R_4}$ 

$$\frac{n_2}{n_1} = \frac{n_2}{n_3}$$

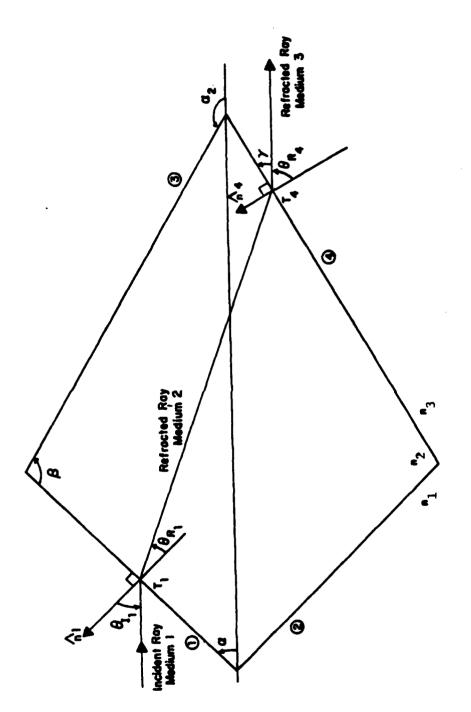
therefore  $n_1 = n_3$ .

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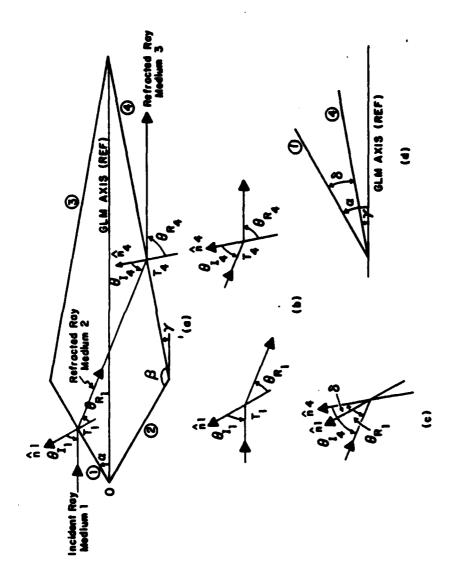
The conclusion for this lens is that the indices of refraction for media 1 and 3 must be equal. The lens causes inversion of the image because the rays are incident in the upper half-plane and exit in the lower half-plane.

A more general lens is shown in figure D-2 which does not have boundary conditions 1) and 2) above. All other boundary conditions apply and in addition the lens is symmetric about the GLM axis.

The incident ray in medium 1 forms an angle of incidence  $\theta_{I_1}$  with  $\hat{n}_1$ , the normal to surface ①. The ray is refracted according to  $\sin\theta_{R_1}=(n_1/n_2)\sin\theta_{I_1}$  and traverses the medium, forming the angle of incidence  $\theta_{I_4}$  with  $\hat{n}_4$ , the normal to surface ②. The ray is refracted into medium 3 according to  $\sin\theta_{R_4}=(n_2/n_3)\sin\theta_{I_4}$  parallel to the incident ray in medium 1. Noting the angular relationship between  $\hat{n}_4$ , and  $\hat{n}_4$  in figure D-3 such that  $\theta_3=\theta_2+\delta$  and  $\delta=\alpha-\gamma$ , then  $\theta_3=\alpha-\gamma$  where  $\alpha$  and  $\gamma$  are the angles of sides



Shape, Geometry and Symbol Definition for a General Block Lens. Figure D-2.



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Angular Relationships for the General Block Lens in Figure D-2. Figure D-3.

① and ④ with the GLM axis, respectively.

Now 
$$\theta_{R_4} = \frac{\pi}{2} - \gamma$$

Hence 
$$\theta_{R_A} = \frac{\pi}{2} - (\alpha - \gamma)$$

Similarly 
$$\theta_{I_4} = \theta_{R_1} + \delta = \theta_{R_1} + \alpha - \gamma$$

From Snell's Law applied at side 4 is

$$\sin\theta_{R_4} = \frac{n_2}{n_3} \sin\theta_{I_4}.$$

Noting that 
$$\theta_{1_4} = \theta_{R_1} + \delta$$
,  $\delta = \alpha - \gamma$  and  $\gamma = \frac{\pi}{2} \theta_{R_4}$ 

$$\sin \theta_{R_4} = \frac{n_2}{n_3} \sin(\theta_{R_1} + \alpha + \theta_{R_4} - \frac{\pi}{2})$$

Simplifying by trigonometric expansions for sine and cosine yields

$$\tan \theta_{R_4} = -\left[\frac{n_3 + n_2 \sin(\theta_{R_1} + \alpha)}{n_2 \cos(\theta_{R_1} + \alpha)}\right]$$
 (D-1)

with 
$$\theta_{I_1} = \arcsin \left[ \frac{n_1}{n_2} \sin \theta_{I_1} \right]$$
.

Equation (D-1) is a necessary but not sufficient condition for the ray in medium 3 to emerge from surface 4 parallel to to the incident ray in medium 1. The final condition relates the angles of surfaces 1 and 4 and  $\theta_{\text{I}_4} = \theta_{\text{R}_1} + \delta$  as shown in figure D-3.

Applying Snell's Law at surface (4) and using trigonometric expansions yields

$$\tan \gamma = \left(\frac{n_2 \sin(\theta_{R_1} + \alpha) - n_3}{n_2 \cos(\theta_{R_1} + \alpha)}\right) \tag{D-2}$$

with  $\theta_{R_1} = \arcsin \left[ (n_2/n_1) \sin \theta_{I_1} \right]$ .

With equations (D-1) and (D-2) rearranged to relate the  $\tan(\theta_{R_1} + \alpha)$  as the independent variable the equations become  $\tan(\theta_{R_1} + \alpha) = -\left(\tan\theta_{R_4} + \frac{n_3}{n_2}\right)$  (D-3)

and

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$$\tan(\theta_R + \alpha) = -\left(\frac{n_3}{\cos(\theta_{R_1} + \alpha)} + \tan\delta\right)$$
 (D-4)

Since equation (D-3) equals equation (D-4) and solving for tany yields

$$\tan \gamma = \tan \theta_{R_4} + \frac{n_3}{\cos (\theta_{R_1} + \alpha)} + \frac{n_3}{n_2}$$
 (D-5)

With the condition that  $\gamma + \theta_{R_A} = \frac{\pi}{2}$  and noting that

$$\theta_{I_1} = \frac{\pi}{2} - \alpha$$
,  $\delta - \alpha - \gamma$  and  $\theta_{I_4} = \theta_{R_1} + \delta$ 

$$\theta_{R_1} = \arcsin \left[ \frac{n_1}{n_2} \sin \left( \frac{\pi}{2} - \alpha \right) \right]$$

and

$$\theta_{R_4} = \arcsin \left[ \frac{n_3}{n_2} \sin (\theta_{R_1} + \alpha - \gamma) \right]$$

Equation (D-5) is recognized as a transcendental equation of the form  $\tan\gamma = \tan\left\{\arcsin\left[\frac{n_3}{n_2} \sin\left(\theta_{R_1} + \alpha - \gamma\right)\right]\right\} + \frac{n_3}{\cos\left(\theta_{R_1} + \alpha\right)} + \frac{n_3}{n_2} \quad \text{(D-6)}$  which must be solved iteratively. The constraints on the solution are that  $(\theta_{R_1} + \alpha) < \frac{\pi}{2}$  and  $(n_3/n_2) \sin\left(\theta_{R_1} + \alpha + \gamma\right) \le 1 \quad \text{and} \quad \theta_{R_4} + \gamma = \frac{\pi}{2} \; .$ 

The appearance of the configuration of this lens in 3-dimensions would be two cones fit base to base. The image formed would be inverted with the center missing; i.e. an annulus. Therefore a substantial amount of energy could be lost in the image if the energy distribution of the object is Gaussian with the maximum at the center of the object. Therefore equations (D-1) and (D-6) are necessary and sufficient conditions to insure the incident ray in medium 1 is parallel to the exit ray in medium 3. If the condition that  $\theta_{R_2} = \theta_{I_1}$  then the general lens reduces to the rhombus of figure D-1, or that of a parallelopiped in figure D-4. The position a block lens would occupy in the GLM is shown in figure D-5.

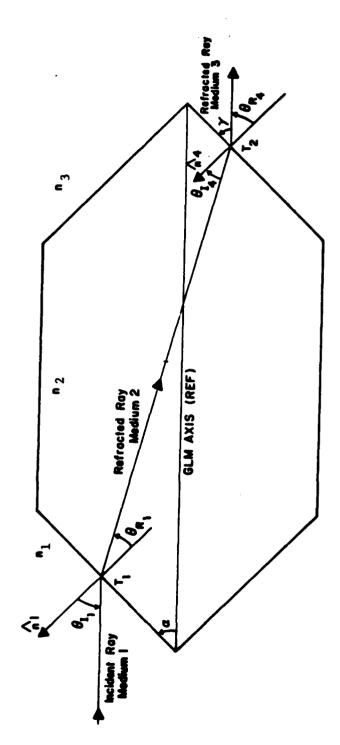


Figure D-4. Parallelopiped Block Lens.

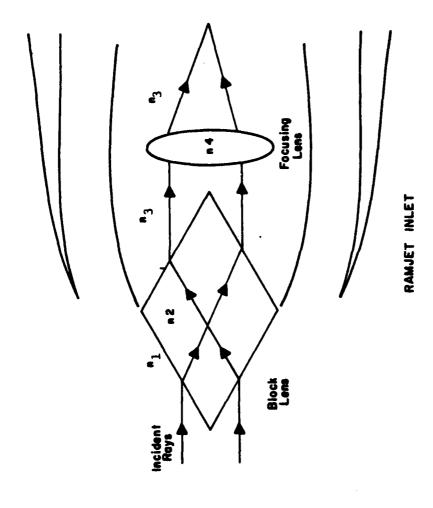


Figure D-5. Position of a Block Lens in the GLM.

#### APPENDIX E

### GRADIENT INDEX OPTICS

The development of material which exhibits a continuous change in the optical index of refraction over distance has opened a new area in the field of optics. Gradient index (GRIN) material has been applied in the field of fiber optics communications and integrated circuits with expanding numbers of applications. GRIN has the effect of replacing individual lenses in an optical system. Theoretically GRIN material has the ability to refract light because of the continuous change in index of refraction in the medium. Practically the amount of refraction is proportional to the change in the relative index from macroscopic region to macroscopic region.

GRIN material is produced with one of three types of gradients in the index of refraction referenced to the optical axis:

- 1. Axial
- 2. Cylindrical
- 3. Spherical

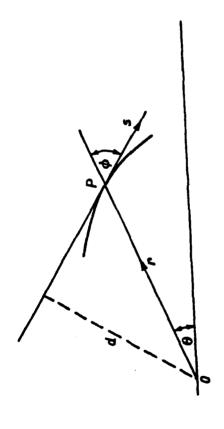
Axial GRIN varies the index of refraction along the optical axis. Cylindrical GRIN varies the index of refraction radially from the optical axis. Hence, in three dimensions the surfaces of constant index form concentric cylinders centered on the optical axis. Spherical GRIN varies the index of refraction radially from the origin. The surfaces of constant index form a set of concentric spheres [8].

$$\sin \phi = \frac{r(\phi)}{\sqrt{r^2(\phi) + \left(\frac{dr}{d\theta}\right)^2}}$$
 (E-1)

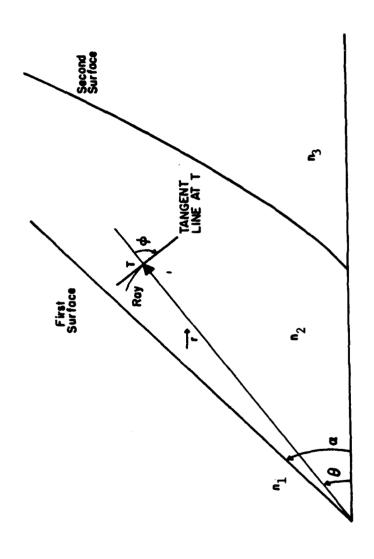
where  $dr/d\theta = (r/c)\sqrt{n^2r^2 - c^2}$ ;  $\theta$  is the angle between two consecutive radii and c is Bouguer's constant. In three dimensions using spherical coordinates the relation for the change in  $\theta$ , illustrated in figure E-3, over a range of radius is given by

$$\theta - \theta_0 = c \int_{r_0}^{r} \frac{dr}{\sqrt{n^2 r^2 - c^2}}$$
 (E-2)

Given a sphere of GRIN material shown in figure E-4 with a spherical gradient, a GLM lens can be selectively cut from the material. The lens can be customized with an index of refraction profile suitable for the application. A possible profile for the GLM conical lens, is shown in figure E-5, with a minimum and maximum located at a specific radius from the origin. Hence the ability to customize the GLM lens



Illustrating Bouguer's Formula nd = constant, for Rays in a Medium with Spherical Symmetry. Figure E-1.



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Figure E-2. Illustration of Bouguer's Formula in the GLM Conical Lens.

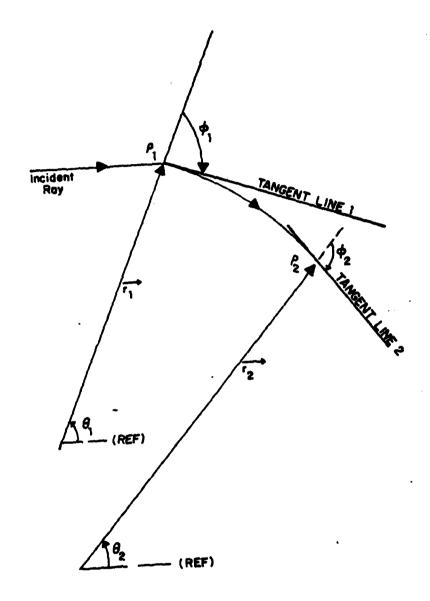
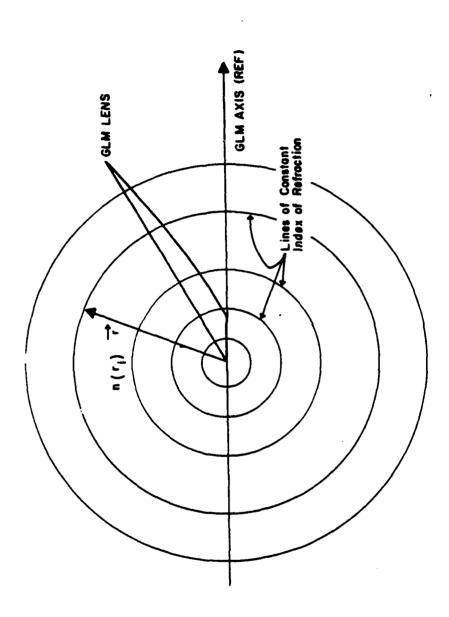


Figure E-3. Illustration of the Relationship Between  $\hat{\tau}$  and  $\phi$  Between Adjacent Rays in the GLM GRIN Lens.

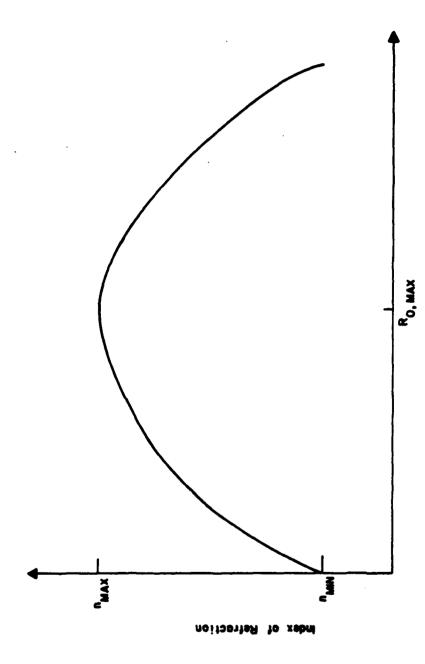
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Illustration of a GLM Lens as a Section of GRIN Material Exhibiting Spherical Symmetry. Figure E-4.



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Figure E-5. Index of Refraction Profile as a Function of Radius from the Origin.

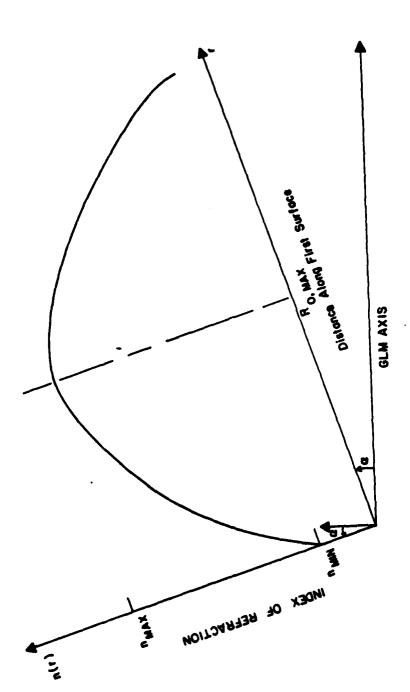
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enables the lens designer to place the maximum value of the index of refraction at the desired location. The profile shown in figure E-5 can be applied to the GLM conical lens with the index profile varying along the first surface shown in figure E-6.

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Bouguer's constant, defined by the relation nrsin $\phi$  = c is a function of the radius, index of refraction at that radius and the angle  $\phi$  defined earlier. However, once the ray enters the GRIN medium, the constant is invariant along the ray. Therefore the constant can theoretically be determined explicitly at any point. Practically, two points exist at which the constant can be determined. These are at the intercept of the incident ray and the first surface and the intercept of the ray in the conical lens and the second surface. The most convenient position to calculate c is the first surface because n, r and  $\phi$  can all be determined explicitly on the first surface. Table E-I is a tabulation of values of Bouguer's constant c. Figure E-7 shows the relationship between the constant c and the radius from the origin along the first surface of the GLM.

Calculating the ray paths through a conical lens composed of GRIN material must be accomplished by solving equation (E-2) at each point in the lens. A complete algorithm was not written because of the time constraints, but TRACE can calculate the value of Bouguer's constant and refract the ray at the first surface shown in figure E-8 using the value of



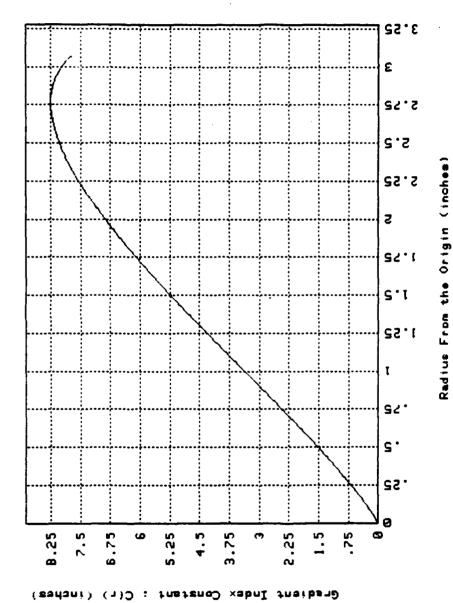
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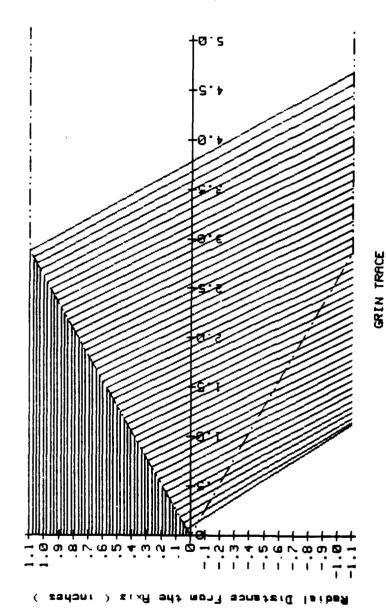
Index of Refraction as a Function of Distance Along the First Surface of the GLM Lens. Figure E-6.

TABLE E-I
BOUGUER'S GRIN CONSTANT

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I	n(I)	r(I)	Phi(I)	\$in(Phi)	c+ I)
1	2.4406	. 9614	67.5096	.9239	. 138
2	2.6170	. 1228	69.8997	.9342	. 300
3	2.7491	. 1842	70.1402	. 9405	.476
4	2.8551	. 2456	70.9137	. 9450	.662
5	2.9461	. 3069	71.5251	. 9485	. 957
6	3.0254	. 3683	72.0263	.9512	1.060
7 8	3.0956	. 4297	72.4472	.9534	1.268
9	3.1583 3.2147	.4911 .5525	72.8067 73.1174	.9553 .9569	1.481 1.699
10	3.2656	.6139	73.3882	.9583	1.921
ii	3.3116	. 6753	73.6258	.9594	2.145
12	3.3534	.7367	73.8352	.9605	2.372
13	3.3911	.7981	74.0200	.9614	2.601
14	3.4252	. 8595	74.1834	. 9621	2.832
15	3.45 <b>60</b>	. 92 <b>08</b>	74.3277	. 9628	3.064
16	3.4835	. 9822	74.4549	. 9634	3.296
17	3.5081	1.0436	74.5664	. 9639	3.529
18 19	3.5298 3.5488	1.1050 1.1664	74.6637 74.7477	. 9644 . 9648	3.761 3.993
20	3.5651	1.2278	74.8193	.9651	4.224
21	3.5789	1.2892	74.8792	.9654	4.454
22	3.5902	1.3506	74.9279	. 9656	4.682
23	3.5991	1.4120	74.9659	.9658	4.907
24	3.6055	1.4733	74.9935	. 9659	5.131
25	3.6096	1.5347	75.0109	. 9660	5.351
26	3.6114	1.5961	75.0184	. 9660	5.568
27 28	3.6108 3.6079	1.6575 1.7189	75.0159 75.0034	.9660 .9659	5.781 5.990
29	3.6026	1.7993	74.9809	. 9658	6.194
30	3.5949	1.8417	74.9482	.9657	6.393
31	3.5849	1.9031	74.9049	. 9655	6.586
32	3.5723	1.9645	74.8506	. 9652	6.773
33	3.5573	2.0259	74.7858	. 9649	5.953
34	3.5396	2.0072	74.7073	. 9646	7.126
35	3.5193	2.1486	74.6168	. 9642	7.290
36	3.4962	2.2100	74.5125	.9637	7.446
37 38	3.4701 3.4410	2.2714 2.3328	74.3933 74.2578	. 9631 . 9625	7.591 7.726
39	3.4006	2.3942	74.1842	.9618	7.846
40	3.3727	2.4556	73.9304	. 9609	7.958
41	3.3330	2.5179	73.7338	. 9600	8.053
42	3.2892	2.5784	73.5100	. 9589	8.131
43	3.2408	2.6397	73.2573	. 9576	8.192
44	3.1872	2.7011	72.9675	. 9561	8.231
45	3.1278	2.7625	72.6337	. 9544	3.246
46	3.0615	2.8239	72.2454	.9524	8.233
47 48	2.9870 2.9822	2.8853 2.9467	71.7973 71.2357	. 949 <b>9</b> . 9468	8.18 <b>6</b> 8.097
49	2.8039	3.0081	70.5519	.9429	7.953
50	2.6864	3.0695	69.6639	.9377	7.731





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ni : 1.00000 Number of Rays : 46

Ray Diagram Showing the Change in Refracted Ray Angle at the First Surface of the GLM Lens Using GRIN Material for the Lens. Figure E-8.

the index of refraction at that point. The calculated data for the ray diagram is tabulated in Tables E-II and E-III.

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# TABLE E-II .

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### INITIAL PARAMETER VALUES

n2(4) = 2.86301	2.62297 2.95465 3.16790 3.32137	n2(	3> = 6> =	
n2(1) = 2.44494 $n2(2) = 2.86301$ $n2(5) = 2.86301$ $n2(5) = 2.86301$ $n2(6) = 2.86301$ $n2(8) = 2.86301$ $n2(1) = 2.86301$	2.95465 3.16790 3.32137	n2(	6> =	
n2(4) = 2.86301	2.95465 3.16790 3.32137	n2(	6> =	
n2(7) = 3.10497	3.16790 3.32137		-	3.0344
n2(10) = 3.27535	3.32137	n2<	<b>a</b> -	
n2(13) = 3.40051 $n2(14) =$			7, =	3.2244
		n2(1	2> =	3.3629
n2(16) = 3.49189  n2(17) =	3.43436	n2<1	5) =	3.4647
	3.51596	n2(1	8) =	3.5371
n2(19) = 3.55543 $n2(20) =$	3.57106	n2<2	1) =	3.5840
n2(22) = 3.59449 $n2(23) =$	3.60241	n2<2	4) =	3.6078
n2(25) = 3.61983 $n2(26) =$	3.61138	n2(2	7) =	3.6094
$n2(28) = 3.60516 \qquad n2(29) =$	3.59836	n2<3	<b>a</b> ) =	3.5890
$n2(31) = 3.57723 \qquad n2(32) =$	3.56280	n2(3	3) =	3.5456
n2(34) = 3.52582  n2(35) =	3.50309	n2(3	6) =	3.4773
	3.41619	n2(3	9) =	3.3803
n2(40) = 3.34060  n2(41) =	3.29663	n2(4	2) =	3.24790
n2(43) = 3.19407 $n2(44) =$	3.13415	n2<4	5) =	3.0672
$n2(46) = 2.99185 \qquad n2(47) =$	2.90593	n2(4	8) =	2.8061
n2(49) = 2.68635 $n2(50) =$	2.68635	n2(5	1) =	0.0000
0_max = 1.61147 inches				

TABLE E-III

RAY DIAGRAM DATA CALCULATED FOR FIGURE E-8

(X0,Y0)	(X1,Y1)	(X3,Y3)	(Xc,Yc)	N2	RHQ
0.00 .02	.06 .02	4.06 -4.20	.08 0.00	2.44	-46.51
0.00 .04	.11 .04	3.96 -4.24	.15 0.00	2.62	-48.10
0.00 .07	.17 .07	3.91 -4.26	.23 0.00	2.75	-49.14
0.00 .09 0.00 .11	.23 .09 .29 .11	3.89 ~4.26 3.89 ~4.26	.30 0.00 .38 0.00	2.86 2.95	-49.91
0.00 .13	.34 .13	3.90 -4.26	.45 0.00	3.03	-50.53 -51.03
0.00 .15	.40 .15	3.92 -4.26	.52 0.00	3.10	-51.45
0.00 .18	.46 .18	3.94 -4.25	.60 0.00	3.16	-51.81
0.00 .20	.52 .20	3.97 -4.24	.67 0.00	3.21	-52.12
0.00 .22	.57 .22	4.00 -4.22	.74 0.00	3.27	-52.39
0.00 .24 0.00 .26	.63 .24 .69 .26	4.03 -4.21 4.07 -4.20	.82 0.00	3.31	-52.63
0.80 .29	.69 .26 .75 .29	4.11 -4.18	.89 0.00 .96 0.00	3. <b>35</b> 3.39	-52.84 -53.02
8.88 .31	.80 .31	4.15 -4.16	1.03 0.00	3.43	-53.18
0.00 .33	.86 .33	4.19 -4.15	1.11 0.00	3.46	-53.33
0.00 .35	.92 .35	4.24 -4.13	1.18 0.00	3.48	-53.45
0.00 .37	.97 .37	4.29 -4.11	1.25 0.00	3.51	-53.57
0.00 .48	1.03 .40	4.33 -4.09	1.32 0.00	3.53	-53.66
0.00 .42 0.00 .44	1.09 .42	4.38 -4.08 4.43 -4.06	1.40 0.00 1.47 0.00	3.55	-53.75
0.00 .46	1.20 .46	4,49 -4.04	1.54 0.00	3.57 3.58	-53.82 -53.88
0.00 .48	1.26 .48	4.54 -4.02	1.61 0.00	3.59	-53.33
0.00 .51	1.32 .51	4.59 -4.00	1.69 0.00	3.60	<b>-5</b> 3.97
0.00 .53	1.38 .53	4.65 -3.97	1.76 0.00	3.61	-53.99
0.00 .55	1.43 .55	4.70 -3.95	1.83 0.00	3.61	-54.01
0.00 .57 0.00 .59	1.49 .57 1.55 .59	4.76 -3.93 4.82 -3.91	1.91 0.00	3.61	-54.02
0.00 .62	1.55 .59 1.60 .62	4.88 -3.89	1.98 0.00 2.05 0.00	3.61 3.61	-54.02 -54.00
0.00 .64	1.66 .64	4.93 -3.86	2.13 0.00	3.60	-53.98
0.00 .66	1.72 .66	5.00 -3.84	2.20 0.00	3.59	-53.95
9.00 .68	1.78 .68	5.06 -3.82	2.27 0.00	3.58	-53.90
0.00 .70	1.83 .70	5.12 -3.79	2.35 0.00	3.57	-53.25
0.00 .73 0.00 .75	1.89 .73 1.95 .75	5.18 -3.77 5.25 -3.74	2.42 8.00	3.56	-53.78
0.00 .77	2.81 .77	5.31 -3.72	2.50 0.00 2.57 0.00	3.54 3.52	-53.71 -53.62
0.00 .79	2.06 .79	5.38 -3.69	2.65 0.00	3.50	-53.52 -53.51
0.00 .81	2.12 .81	5.45 -3.67	2.73 0.00	3.47	-53.39
0.00 .84	2.18 .84	5.52 -3.64	2.80 0.00	3.44	-53.26
9.00 .86	2.24 .96	5.59 -3.61	2.88 0.00	3.41	-53.10
<b>9.00</b> .88 9.89 .90	2.29 .88 2.35 .98	5.66 -3.58	2.96 0.00	3.37	-52.93
8.08 .92	2.35 .98	5.74 -3.55 5.82 -3.52	3. <b>04</b> 0.00 3.12 0.00	3.33 3.29	-52.73 -52.51
0.00 .95	2.46 .95	5.90 -3.49	3.20 0.00	3.29	-52.51 -52.26
0.00 .97	2.52 .97	5.99 -3.46	3.28 0.00	3.19	-51.97
0.00 .99	2.58 .99	6.07 -3.43	3.36 0.00	3.13	-51.63
0.00 1.01	2.64 1.01	6.17 -3.39	3.45 0.00	3.06	-51.25
0.00 1.03	2.69 1.03	6.27 -3.35	3.54 0.00	2.99	-50.79
9.00 1.06 9.00 1.08	2.75 1.06 2.81 1.09	6.38 -3.31 6.51 -3.26	3.63 0.00	2.90	-50.24
0.00 1.10	2.87 1.10	6.65 -3.26	3.73 0.00 3.83 0.00	2.80 2.69	-49.55 -48.66

#### APPENDIX F

### SECUND SURFACE GENERATION: ITERATIVE SOLUTION

#### A. INTRODUCTION

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One of the conclusions reached as a result of the investigation of curves A, B and C in Appendix C was that using a single polynomial to describe the second surface of a conical lens cannot satisfactorily refract light to a single, distinct focal point. Hence, a satisfactory image of an object cannot be formed.

Three options for further study remained. First, continue to try and find a suitable polynomial to describe the second surface. This option was not pursued because of the infinite number of trials which would be required to determine if such an analytic expression existed. The second option would be to attempt to optimize a given polynomial by manipulating the coefficients of that polynomial to change the refracting properties of the polynomial such that a single, distinct focal point could be formed. This option was pursued by using Control Program for Engineering Synthesis (COPES) developed by Dr. G.N. Vanderplaats, Naval Postgraduate School. The study was halted because of time constraints. However, initial results concurred with the previously mentioned results of Appendix C.

The third option was provided by an inquiry made by Dr. E.C. Crittenden, Naval Postgraduate School, concerning the capability of the TRACE program to draw rays backward;

i.e. could TRACE begin a set of light rays at a design focal point and draw them through the lens and into the medium ahead of the lens and emerging parallel to the GLM axis? Accomplishing the "backwards" ray trace would design the lens. Conceptually, at least two methods of generating the second surface of a conical lens exist and are available for investigation. The first method consisted of picking the initial point of the second surface to be the GLM axisintercept of a refracted ray in the lens medium, noting that the ray must be refracted along the GLM axis to pass through Therefore, the slope of the second surface at the first point must be equal to the slope of the first surface. The derivation of this relationship is performed in Appendix The second point on the surface is calculated by extending a straight line by using the slope at the first point to intercept the next ray in the lens. Since the second point is not on the GLM axis, the slope at the second point required to satisfy Snell's Law will not be equal to the slope of the first surface. This process was chosen as the preferred method and is discussed in Chapter III and Appendix A.

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The second method of generating a second surface for a conical lens is similar to the first method. The difference is that a parabola is used instead of a straight line to predict the second and succeeding points on the second surface. A different parabola is used for every pair of points. A nonlinear predictor is desired because the shape of the

second surface is nonlinear. The following discussion describes this method of second surface generation for a conical lens.

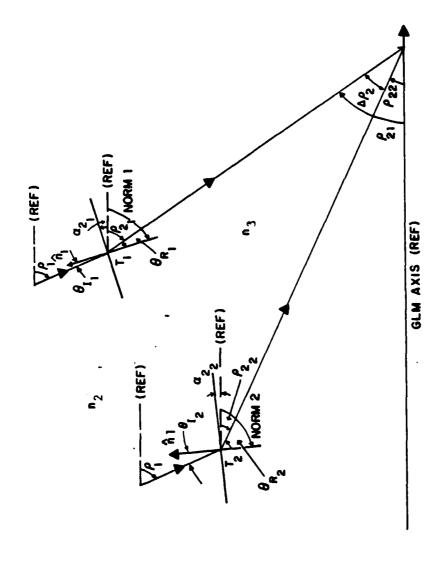
### B. ITERATIVE SOLUTION

# 1. Derivation of Expressions for $\theta$ I and $\alpha_2$

The iterative solution is motivated by the ability of a computer to perform a great many calculations in a small amount of time. Referring to figure F-1 for the geometry and symbol definitions, the most significant steps in the iterative solution are:

#### (1) Initialization:

- (a) Choose a focal point on the GLM axis.
- (b) Choose an initial lens point Tl.
- (c) Choose an initial change in  $\rho_2$ ,  $\Delta \rho_2$ .
- (2) Calculate the ray parameters  $\theta_{I}$ ,  $\rho_{2}$  and  $\alpha_{2}$  for the initial lens point by applying Snell's Law at T1.
- (3) Calculate the second lens point T2 by fitting a parabola through T1 and predict the coordinate values of T2. Iterate this prediction until the error is reduced below an acceptable tolerance. The error is defined to be the distance at which T2 intercepts the GLM axis.
- (4) Calculate the ray parameters  $\,\theta_{\,\hbox{\scriptsize I}}^{}\,,\ \, \rho_{\,\hbox{\scriptsize 2}}^{}\,$  and  $\,\alpha_{\,\hbox{\scriptsize 2}}^{}\,$  for T2.
- (5) Continue until the lens has been designed to the GLM axis.



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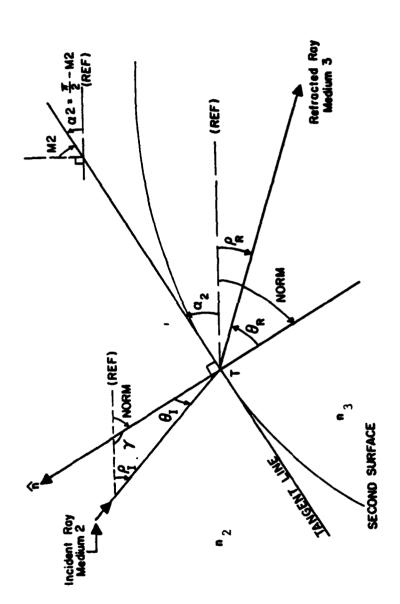
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Geometry and Symbol Definition Used for the Iterative Solution Method of Second Surface Generation. Figure F-1.

NOTE: All coordinate values are referenced to a right hand system. All angles are referenced to the GLM axis and are positive for counter-clockwise rotation from the axis to the point in question. The coordinate values (abscissa, ordinate) are referred to as (x,y) with  $x \equiv$  the distance along the GLM axis and  $y \equiv$  the radius from the GLM axis. The subscripts are either single or double. The single and the first subscript in the double subscripts, the number refers to the surface at which the application of Snell's Law occurred. If the subscript is a letter the subscript refers to the operation of Snell's Law; I for angle of incidence and R for angle of refraction. The second subscript refers to the point number in the lens. For example  $\alpha_2$  is the slope of the second surface at point number two. Any exceptions to this convention for subscripts will be made clear within the context of the discussion.

The investigation consisted of deriving the analytical expressions relating the quantities shown in figure F-2. The primary variables of interest are the angle of incidence  $\theta_{\rm I}$ ,  $\alpha_2$  the angle of the tangent line at T and  $\rho_2$  the refracted ray angle in medium 3. The assumptions made in the derivation are that the following quantities are known:

(1)  $\rho_1$ ; the ray angle in the lens medium, measured with respect to the GLM axis.



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Geometry and Symbols Used for Snell's Law in the Low Region as Applied to the Iterative Solution Methods for Second Surface Generation. Figure F-2.

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- (2)  $\rho_2$ ; the ray angle in medium 3 measured with respect to the GLM axis.
  - (3)  $n_2$ ; the index of refraction of the lens medium.
  - (4)  $n_3$ ; the index of refraction of medium 3.
  - (5) f; the design focal point on the GLM axis.
  - (6) (x,y); the coordinate values of the Point T.
  - (7) the ray is transmitted without loss in all media.
- (8) the ray is either refracted or totally reflected at the boundary of two media.

As discussed in Chapter III there exist two regions where the refracted ray in the lens can be refracted at point T. Point T is located in the low region as defined by the area below a line QP shown in figure F-3. In the low region  $|\rho_1|$  is always greater than or equal to  $|\beta|$ . Point T is located in the high region when  $|\rho_1|$  is less than  $|\beta|$  as shown in figure F-4.

Each point on the lens' second surface must satisfy Snell's Law  $\sin\theta_R = n_2/n_3 \sin\theta_I$  or be totally reflected at T. Therefore referring to figure F-2 the angle of incidence in the low region is

$$\theta_{T} = \left(\frac{\pi}{2} - \alpha_{2}\right) - \left|\rho_{1}\right| \tag{F-1}$$

and the ray angle in medium 3 is

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$$|\rho_2| = \frac{\pi}{2} - (\theta_R + \alpha_2) \tag{F-2}$$

Substracting equation (F-2) from (F-1) and substituting Snell's Law for  $\,\theta_{R}\,$  yields

$$\theta_{I} = |\rho_{2}| - |\rho_{1}| - \arcsin \left[\frac{n_{2}}{n_{3}} \sin \theta_{I}\right]$$
 (F-3)

Now  $\alpha_2 = \frac{\pi}{2} - (|\rho_2| - \theta_R)$  hence

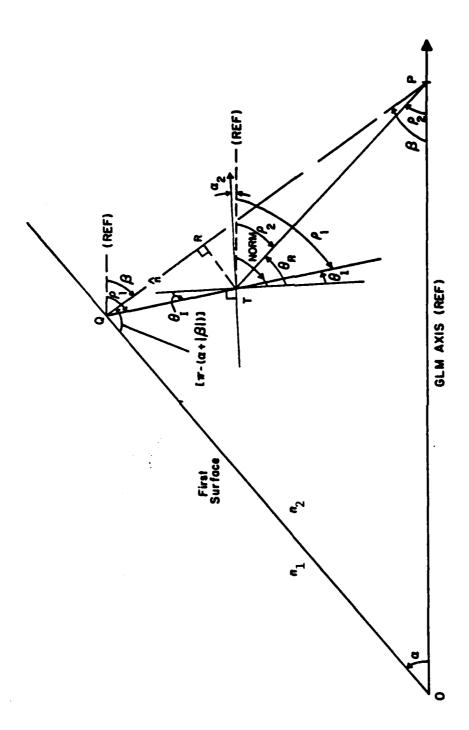
$$\alpha_2 = \frac{\pi}{2} - \left[ |\rho_2| + \arcsin\left(\frac{n_2}{n_3}\sin\theta_1\right) \right]$$
 (F-4)

Equation (F-3) is a transcendental equation in  $\theta_{\rm I}$  and therefore can be solved graphically or by numerical methods. Therefore, equations (F-3) and (F-4) must both be solved for each iteration of  $\theta_{\rm I}$  until a satisfactory value of  $\alpha_2$  is determined. Experience from using the CHART algorithm shows that an initial guess of  $\theta_{\rm I} = \theta_{\rm C} - 2^{\rm O}$  should allow the algorithm to converge quickly. The critical angle  $\theta_{\rm C}$  is the angle of incidence at which  $\sin\theta_{\rm R}$ =1. Changing equations (F-3) and (F-4) into a form suitable for a numerical algorithm yields

$$\theta_{I,n+1} = |\rho_2| - |\rho_1| + \arcsin \left[ \frac{n_2}{n_3} \sin \theta_{I,n} \right]$$
 (F-5)

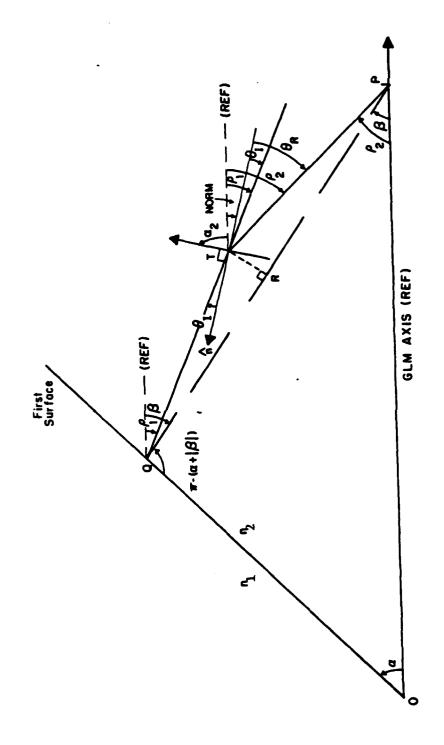
$$\alpha_{2_{1}} = \frac{\pi}{2} - \left[ |\rho_{2}| + \arcsin\left(\frac{n_{2}}{n_{3}} \sin\theta_{1_{n+1}}\right) \right] \quad (F-6)$$

for the angle of incidence and angle of the tangent line at Point T in the low region.



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Geometry and Symbols Used for Snell's Law in the Low Region as Applied to the Iterative Solution Method for Second Surface Generation. Figure F-3.



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Geometry and Symbols Used for Snell's Law in the High Region as Applied to the Iterative Solution Method for Second Surface Generation. Figure F-4.

As shown in figure F-4 the angle of incidence in the high region is

$$\theta_{\mathsf{T}} = |\rho_2| - |\rho_1| \tag{F-7}$$

and the ray angle in medium 3 is

$$\rho_2 = \frac{\pi}{2} - \alpha_2 + \theta_R \tag{F-8}$$

Adding equations (F-7) and (F-8) and substituting Snell's Law for  $\theta_{\mbox{\scriptsize R}}$  yields

$$\theta_{I} = \frac{\pi}{2} - (|\rho_{1}| + \alpha_{2}) + \arcsin\left(\frac{n_{3}}{n_{2}}\sin\theta_{I}\right)$$
 (F-9)

now  $\alpha_2 = \frac{\pi}{2} - |NORM|$ 

hence

$$\alpha_2 = \frac{\pi}{2} - |\rho_1| + \theta_T \tag{F-10}$$

Equation (F-9) is a transcendental equation in  $\theta_{\rm I}$  and must be solved graphically or by numerical methods. Therefore equations (F-9) and (F-10) must be solved for each iteration of  $\theta_{\rm I}$  until a satisfactory value of  $\alpha_2$  is determined. From the geometry in figure F-4 an initial guess for  $\theta_{\rm I} = 2 \ |\rho_1|$  should cause fast convergence to the desired value of  $\alpha_2$ . Changing equations (F-9) and (F-10) into a form suitable for numerical applications yields

$$\theta_{I_{n+1}=\frac{\pi}{2}-(|\rho_1| \alpha_{2_{1^n}}) + \arcsin\left(\frac{n_3}{n_2}\sin\theta_{I_{n}}\right)$$
 (F-11)

$$\alpha_{2,n+1} = \frac{\pi}{2} - |\rho_1| + \theta_{1,n+1}$$
 (F-12)

for the angle of incidence and angle of the tangent line at Point T in the high region.

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## 2. Predicting Succeeding Points on the Second Surface

The iterative solution method must involve a regression routine to use a parabola to predict the next point on the second surface. The regression routine solves a set of simultaneous equations consisting of the equation of the parabola and first derivative at  $T_1(x_1,y_1)$  and  $T_2(x_2,y_2)$  in the form

$$a + bx_1 + cx_1^2 = y_1$$
 $b + 2cx_1 = y_1^*$ 
 $a + bx_2 + cx_2^2 = y_2$ 
 $a + 2cx_2 = y_2^*$ 

The set of equations is nonlinear in x, but is linear in the coefficients. Therefore, the techniques of linear algebra can be used on equation (F-13). The method used here is the Gaussian-Jordan row-reduction technique discussed in Anton [10]. The first step is to form the augmented matrix whose determinant is set equal to zero

$$\begin{vmatrix}
1 & x_1 & x_1^2 & y_1 \\
0 & 1 & 2x_1 & y_1 \\
1 & x_2 & x_2^2 & y_2 \\
0 & 1 & 2x_2 & y_2
\end{vmatrix} = 0 (F-14)$$

The row-reduction technique diagonalizes the first three columns of determinant (F-14) with, in general, non-zero quantities in the fourth column in the form

$$\begin{vmatrix} 1 & 0 & 0 & A \\ 0 & 1 & 0 & B \\ 0 & 0 & 1 & C \\ 0 & 0 & 0 & \Delta \end{vmatrix} = 0$$
 (F-15)

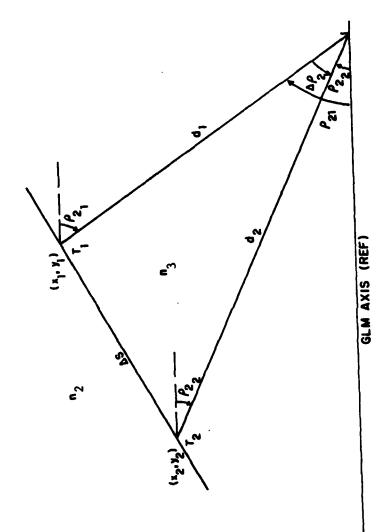
Since four equations have been used to determine the three coefficients a, b and c the determinant is over-specified and nonhomogeneous. Utilizing the fact that the expression represented by D at location (4,4) in (F-15) is equal to zero  $D = x_1y_2' - x_1y_1' + x_2y_2' - x_2y_1' - 2y_2 + 2y_1 = 0 \qquad (F-16)$ 

if  $x_2 \neq x_1$ , which is reasonable, since the problem demands that  $x_2 \neq x_1$ . Simplifying equation (F-16) and solving for

$$\frac{y_2 - y_1}{x_2 - x_1}$$
 yields

$$\frac{\Delta Y}{\Delta X} = \frac{Y_2 - Y_1}{X_2 - X_1} = \frac{Y_2^{1} + Y_1^{1}}{2}$$
 (F-17)

Equation (F-17) states that the slope of the straight line connecting Tl and T2 in figure F-5 is the average of the slope of the parabola used to predict T2 evaluated at Tl and T2. This result is very simple, yet provides a tool to use in predicting the value of T2. Experience gained in using CHART has shown that the second surface of the conical lens is a smooth convex surface with no discontinuities; compare



The second second

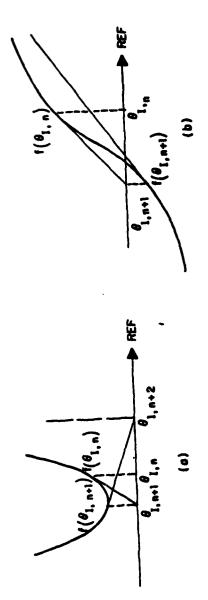
Illustration of the Result of the Solution of the Simultaneous Equations Used to Predict Point T2 on the Second Surface Using the Iterative Method. Figure F-5.

figures 14 and 20 in Chapter III. The exact shape of the second surface is a function of the cone half-angle  $\alpha$ , and the indices of refraction  $n_1, n_2$  and  $n_3$ . The first guess of where T2 is generated by coordinate values of the intersection of the ray in the lens and the ray in medium 3 is shown in figure F-1. The set of equations (F-13) is solved using  $(x_1, y_1)$  and  $(x_2, y_2)$  to find  $(\Delta Y/\Delta X)$  in equation (F-17). Since the slope at Tl is known the next guess of the actual location of T2 is aided by the experience of using CHART. The slope at T2 will increase as the first surface is approached. Therefore, calculating the slope of the line connecting T1 and T2 and comparing that value with the value from equation (F-17) will determine whether to increase or decrease  $\Delta \rho_2$  to predict the next position of  $T_2$ . This procedure is continued until the coordinate values of T2 are determined within a specified tolerance.

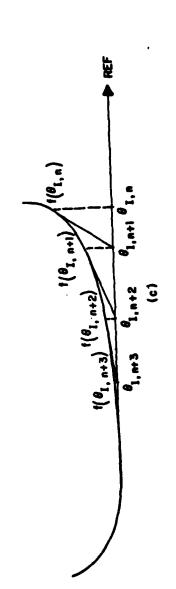
#### C. NEWTON'S METHOD

The recommended numerical method used to solve the transcendental equations for  $\theta_{\rm I}$  and  $\alpha_2$  in section B-1 is Newton's method. A detailed explanation of the technique is not provided here. Scores of texts on applied numerical methods exist and should be consulted for further study.

Newton's method is simple and converges quickly if the function does not have any of the characteristics illustrated in figure F-6. If the function describing  $\theta_{\rm I}$  exhibits a local minimum in the range of interest, Newton's method will



ĺ



Three undesirable Characteristics in Functions  $f(\theta_{\rm I})$  Which Cause Newton's Method to Diverge. Figure F-6.

diverge as illustrated in figure F-6a. If the function exhibits an inflection point, Newton's method will diverge as shown in figure F-6b. If the function has multiple roots in the range of interest, Newton's Method cannot determine which value is correct. The special case of a multiple root is shown in figure F-6c. Newton's method will approach the roots from one side then overshoot and oscillate back and forth, never converging on the desired value. A function which is "well behaved" is shown in figure F-7; compare the characteristics of the curve in figure F-7 and those of figure F-6.

The application of Newton's method as shown in figure F-7 involves the selection of a value of  $\theta_{\rm I}$  as the first guess  $\theta_{\rm I_1}$ , finding the functional value  $f(\theta_{\rm I_1})$  and the slope  $f'(\theta_{\rm I_1})$ . The prediction of the correct value of  $\theta_{\rm I_2}$  is via the relation

$$\theta_{I_2} = \theta_{I_1} - \frac{f(\theta_{I_1})}{f'(\theta_{I_1})}$$
 (F-18)

The process is repeated until the difference between two succeeding values of  $\theta_{\rm I}$ ,  $\left|\theta_{\rm I}-\theta_{\rm I}\right|$  is less than an acceptable tolerance. Transforming equation (F-18) into general form yields

$$\theta_{I_{n+1}} = \theta_{I_n} - \frac{f(\theta_{I_n})}{f'(\theta_{I_n})}$$
 (F-19).

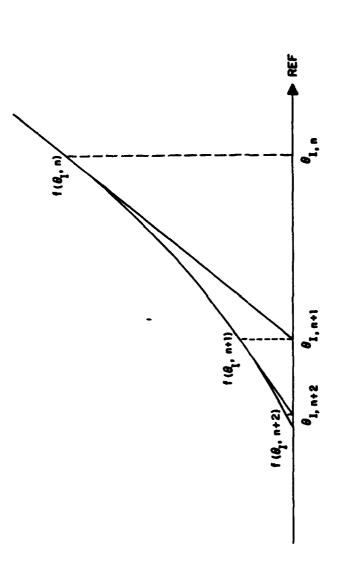


Figure F-7. A Desirable Function  $f(\theta_{\mathrm{I}})$  to Use with Newton's Method.

#### APPENDIX G

### LIMIT PROGRAM DESCRIPTION AND LISTING

The derivation of the relationship between the slopes encountered of the first and second surfaces of a GLM lens composed of homogenous material by the ray shown in figure G-1 is the subject of this appendix. The derivation is applicable to the case in which total reflection occurs at the second surface.

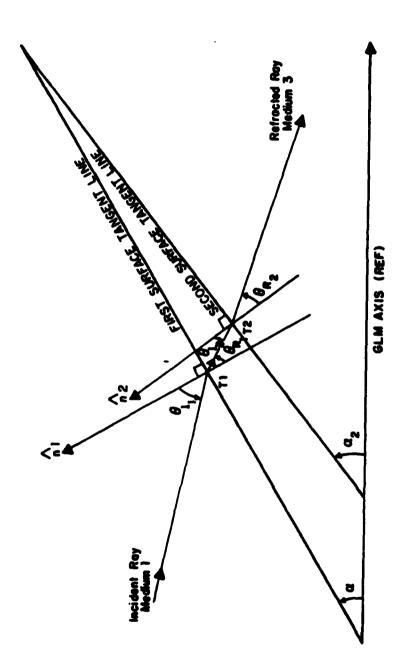
The incident ray in medium 1 forms an angle  $\theta_{1}$  with the first surface normal  $\hat{n}$ , at point Tl and is refracted according to Snell's Law  $\sin\theta_{R_1} = (n_1/n_2\sin\theta_{1})$ . The first surface normal  $\hat{n}$ , is defined as the normal to the tangent line at Tl. The angle which the tangent line makes with respect to the GLM axis is  $\alpha_2$ . The ray traverses the lens and intercepts the second surface at T2. The ray is refracted at T2 according to Snell's Law  $\sin\theta_{R_2} = (n_2/n_3)\sin\theta_{1_2}$ . For total reflection at T2

$$\sin\theta_{R_2} = 1 = \left(\frac{n_3}{n_2}\right) \sin\theta_{I_2} \tag{G-1}$$

Now the angular difference between  $\hat{n}_1$  and  $\hat{n}_2$  is  $(\alpha - \alpha_2)$  and therefore  $\theta_{I_2} = \theta_{R_1} + (\alpha - \alpha_2)$  Hence

$$\theta_{R_1} + (\alpha - \alpha_2) = \arcsin\left(\frac{n_3}{n_2}\right)$$
 (G-2)

The angle with respect to the GLM axis of the tangent line at T2,  $\alpha_2$ , is then defined by



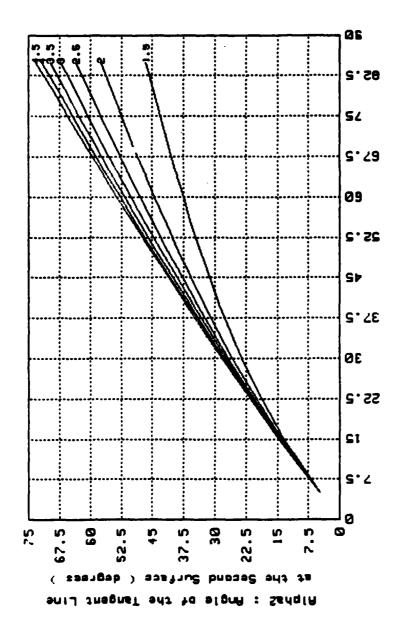
Geometry and Symbol Definition for the Relationship of the Slope of the Second Surface as a Function of the Slope of the First Surface. Figure G-1.

$$\alpha_2 = \arcsin\left(\frac{n_1}{n_2} \sin \theta_{I_1}\right) + \alpha - \arcsin\left(\frac{n_3}{n_2}\right)$$
 (G-3)

Noting that  $\theta_{I_1} = \frac{\pi}{2} - \alpha$  then

$$\alpha_2 = \arcsin \left[ \frac{n_1}{n_2} \sin \left( \frac{\pi}{2} - \alpha \right) \right] - \arcsin \left( \frac{n_3}{n_2} \right) + \alpha$$
 G-4

Equation (G-4) is illustrated in figure G-2.



The state of the s

the the Alpha i Angle of the Tangent Line at the First Burface ( degrees ) The Slope of the Second Surface as a Function of Slope of the First Surface for Various Values of Lens Index of Refraction and the Case of Total Reflection at the Second Surface. Figure G-2.

# LIMIT PROGRAM LISTING

```
20 PRINT ".
30 PRINT "+
                                                    LINIT
   PRINT ".
50 PRINT ************************
       DISP "THIS IS LIMIT"
HAIT 2508
        OPTION BASE &
90
        INTEGER I, Linecount, Linemax
100
        DEG
       FIXED 2
110
       PRINTER IS 16
120
       Linecount=8
140
        Linemax=48
        N1=1
160
        H3=1
170
        INPUT "DO YOU HANT A HARD COPY? Y/N", Y$
100
          IF YS="Y" THEN PRINTER IS 0
          GOSUS Header
190
200
          CALL Graph
       FOR N2=1.5 TO 4.5 STEP .5
210
220
          Alpha=5
230
          Thetai_1=98-Ripha
248
258
          Sin_thetarl=N1/H2+SIN(Thetai_1)
          Thetar 1=ASH(Sin thetar1)
Alpha2=Alpha+ASH(HI/N2+SIN(98-Alpha))-ASH(N3/N2)
260
          Thetai 2=Thetar 1+Alpha-Alpha2
IF Linecount>Linemax THEN GOSUB Header
270
289
          PRINT USING 410; N2, Thetai_1, Thetar_1, Thetai_2, Alpha, Alpha2
298
388
          Linecount=Linecount+1
310
            HOVE Alpha, Alpha2
           FOR Ripha=5 TO 85 STEP 5
Thetai_1=98-Ripha
320
338
340
350
              Sin_thetar1=H1/H2+SIH(Thetai_1)
              Thetar_1=ASN(Sin_thetar1)
Alpha2=Alpha+ASN(N1/N2+SIN(Thetai_1))-ASN(N3/N2)
360
            Thetai 2 Thetar 1+Alpha-Alpha2
If Linecount>Linemax THEN GOSUB Header
370
300
390
              PRINT USING 410; N2, Thetai_1, Thetai_1, Thetai_2, Alpha, Alpha2
400
            Linecount=Linecount+1
410
              IMAGE 5X, DD. DD, 5<5X, DDDD. DDD>
428
              BRAN Alpha, Alpha2
           HEXT Alpha
LDIR 0
430
448
           LORG 2
CSIZE 2.5
LABEL USING 488; N2
IMAGE K
450
460
470
              IF Linecount > Linemax THEN GOSUS Header
           PRINT
510
           Linecount=Linecount+1
520
530
540
550
         NEXT HZ
           GOSUB Header_end
         PRINTER IS 16
         PRINT LIN(2), "PRESS CONT"
950 PRINT LIN(2

960 BEEP

970 HAIT 250

980 BEEP

990 PAUSE

600 EXIT GRAPHI

610 GOTO Finished

620 Mandani II
         EXIT GRAPHICS
                 IF Linecount>Linemax THEN GOSUB Header end
IF Linecount>Linemax THEN PRINT PAGE;TAS(28);"TABLE I (CONT)";LIN(
628 Header:
630
2>
640
630
                 IF Linecount (=Linemax THEN PRINT PAGE; TAB(35); "TABLE I "; LIN(2)
               Linecount = 8
               PRINT LIN(2)
```

```
679
                  GOSUS Char
               PRINT LIN(1); SPA(5); " n2
                                                                           ThetaR(1)
                                                                                            Thetal(2)
                                                         Thetal(1)
    Alpha
                     Alpha2";LIN(1)
                  GOSUB Char
698
788
               PRINT LIN(2)
710
             RETURN
728 Char: FOR I=0 TO 79
                 IF I=79 THEN PRINT CHR$(228)
IF I=79 THEN 768
730
740
750
                PRINT CHR#(228);
760
            HEXT I
778
          RETURN
788 Header_end: PRINT LIN(2)
                       GOSUB Char
                   RETURN
818 Dump_it: PRINTER IS 0
                PRINT CHR#(27)&"&100T"
BUHP GRAPHICS
620
830
                PRINT CHR8(27)&"&136T"
848
850
                PRINTER IS 16
              RETURN
860
878 Finished: Dump_crts="N"
888 INPUT "BO YOU HANT A HARD COPY OF THE PLOT ? Y/N", Dump_crts
900
990
900
910
                  IF (Bump_crt4="Y") OR (Dump_crt5="y") THEN GOSUB Dump_it
DISP "FINISHED"
               END
928 SUB Graph
930
940
930
930
960
970
       OPTION BASE 6
       DEG
           THE EXPRESSIONS USED TO DERIVE THE TIC MARKS HERE OBTAINED FROM THE HP-9845D UTILITIES LIBRARY, TAPE NR 89645-18285, PROGRAM "REGPLT"
700
770
1000
1010
1020
1030
1040
        GCLEAR
        PLOTTER IS 13, "GRAPHICS"
        LDIR .
        LORG 5
1950
        LINIT 0,184,0,100
        DATA -2,-1,1,2
1979
       READ Um, Dm, Md, Mu
DRTR .39794,.69897,.87586
1100
        READ Log2, Log5, Log?
1120
1130
1140
       Xorg=Xmin=Yorg=Ymin=0
       Xnaxe90
        Yeares
1150 Alpha: INPUT "HHAT IS THE HAXIMUM VALUE OF ALPHA ( DEFAULT = 90 DEGREES> ?"
, Xeex
1160 Alpha2: INPUT "WHAT IS THE MAXIMUM VALUE OF ALPHA2 ( DEFAULT = 00 DEGREES)
7°,Ymax
          IF Xmax<=Xmin THEN BEEP
1190
1190
1200
           IF Xmax (=Xmin THEN DISP "ALPHA MUST BE > 0. PLEASE RE-ENTER ALPHA."
           IF Xmax<=Xmin THEN HALT 2500
           IF Xmax(=Xmin THEN Alpha
          IF YMAX<-YMIN THEM BEEP
IF YMAX<-YMIN THEM BISP "ALPHA2 MUST BE > 0. PLEASE RE-ENTER ALPHA2."
IF YMAX<-YMIN THEN HAIT 2500
IF XMAX<-XMIN THEN HAIT 2500
1210
1220
1230 IF Ym
1240 IF Xm
1250 GRAPHICS
1260 I
1270
1200
1290
1300
        LIMIT 0,194,0,140
LOCATE 20,132,20,100
        Lx=LGT(Xmax-Xmin)
        Ly-LGT (Ymax-Ymin)
```

```
1310
       Xfudge=.@2+(Xmax-Xmin)
       Yfudge=.02*(Ymax-Ymin)
1320
1330 Ticmarks: Testxtic=FRACT(Lx)+(Lx(0)
                     Testytic=FRACT(Ly)+(Ly(0)
Xtic=10+(INT(Lx)-1)+(1+1.5+((Testxtic>Log2) AND (Testxtic<Log5))+
1340
40((Testxtic>=Log5) AND (Testxtic(=Log7))+6.50(Testxtic)Log2) AND (Testxtic(Log5))+4.360 Ytic=100(INT(Ly)=1)+(1+1.50(Testxtic)Log2) AND (Testytic(Log5))+4.50(Testytic)Log2) AND (Testytic(=Log7))+6.50(Testytic)Log7))

1370 Scale: SCALE Xmin, Xmax+.250ABS(Xtic), Ymin, Ymax+.250ABS(Ytic)
1300
                  CLIP Xmin, Xmax, Ymin, Ymax
1390
                 LINE TYPE 3
1400
                 Xmaj=Ymaj=1
1410
                 Hinsicsize=4
1420
                 GRID Xtic, Ytic, Xorg, Yorg, Xmaj, Ymaj, Minticsize
                 LINE TYPE 1
1430
1448
                 FRAME
1458 Labelx: LDIR 98
1460
                  LORG &
1478
                  FOR A=Xorg TO Xmax STEP ABS(Xtic)
NOVE A, Yorg-Yrudge
LABEL USING 1570; A
1488
1490
1500 NEXT A
1510 Labely: LBIR 8
1520
                  LORG 8
1530
                  FOR A=Yorg TO Ymax STEP ABS(Ytic)
                     MOVE Xorg-Xfudge,A
LABEL USING 1570;A
1540
1550
                  HEXT A
1570 IMAGE #,K
1500 LABEL USING 1590; ""
1590 IMAGE /,K
1600 Label_: SETGU
1610
                  LDIR .
1620
                  LORG 5
1630
                  Centerx=72
1640
                  Centery=64
                  CRIZE 3
1660
                  MOVE Centerx, 18
1670
                  LABEL "Alpha: Angle of the Tangent Line at the First Surface ( deg
rees )"
1600
                  LDIR 96
1690
1700
1710
1720
                  HOVE 1.45, Centery
LRBEL "Alpha2 : Angle of the Tangent Line"
                     HOVE 6.45, Centery
                  LABEL "at the Second Surface ( degrees )"
1730
1740
1750
1760
                  LDIR 0
                  CSIZE 15/4.54
                  SETUU
              SUDEXIT
```

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